

# La graine, Terra Incognita?

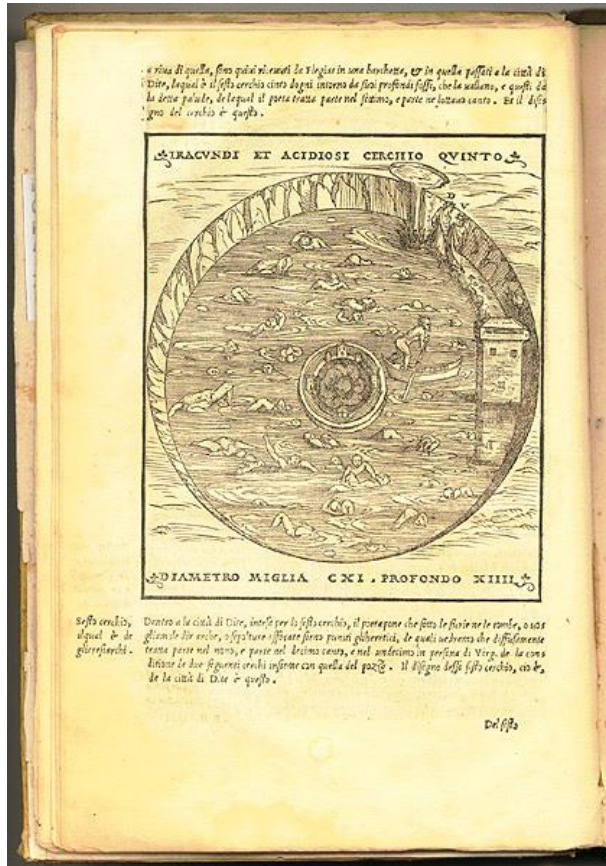
**L'impossible voyage au centre de la Terre ?  
Reconstituer et enseigner l'inaccessible intérieur de la Terre.**

Philippe Cardin  
Institut des Sciences de la Terre  
Grenoble, France

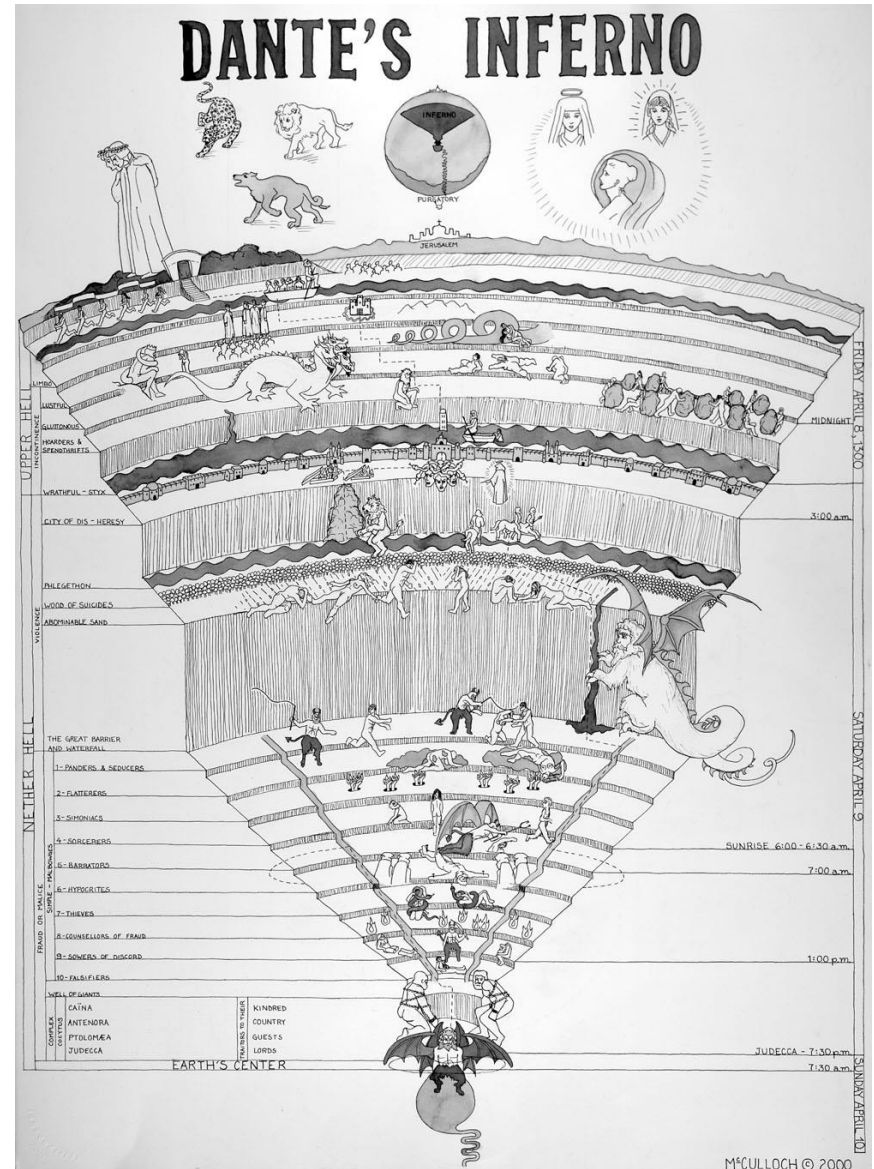
# Plan

1. Sismologie de la graine
2. Une graine en Fer ?
3. Formation de la graine
4. Dynamique de la graine
5. L'anisotropie de la graine

# L'intérieur de la Terre (1315)

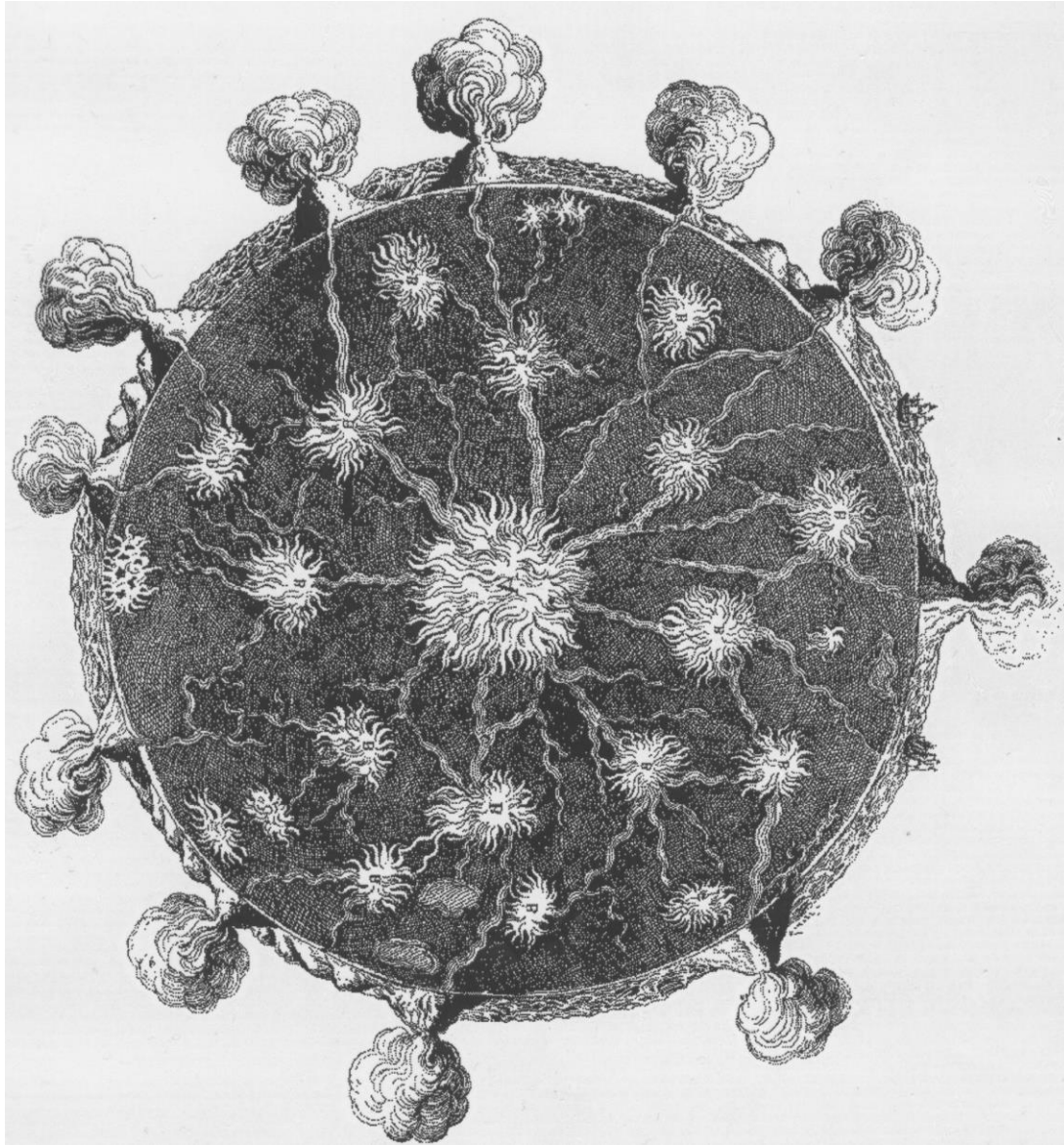


Vellutello, 1544



La graine terrestre

# Le feu central



Kircher, 1678

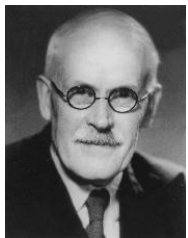
# Le noyau de la Terre



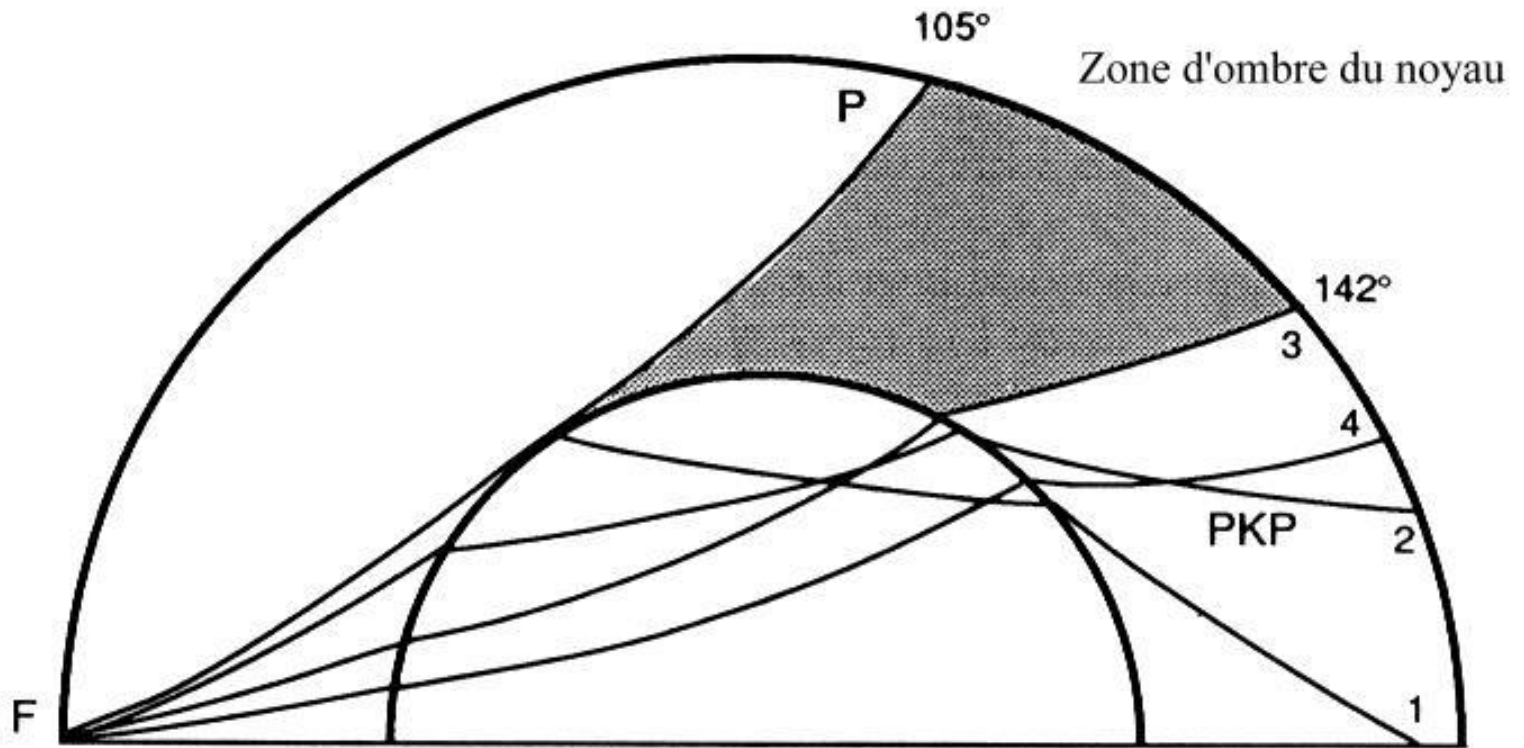
Oldham 1906



Gutenberg, 1914



Jeffreys 1926



# La découverte de la Graine – Inge Lehmann



(1888-1993)

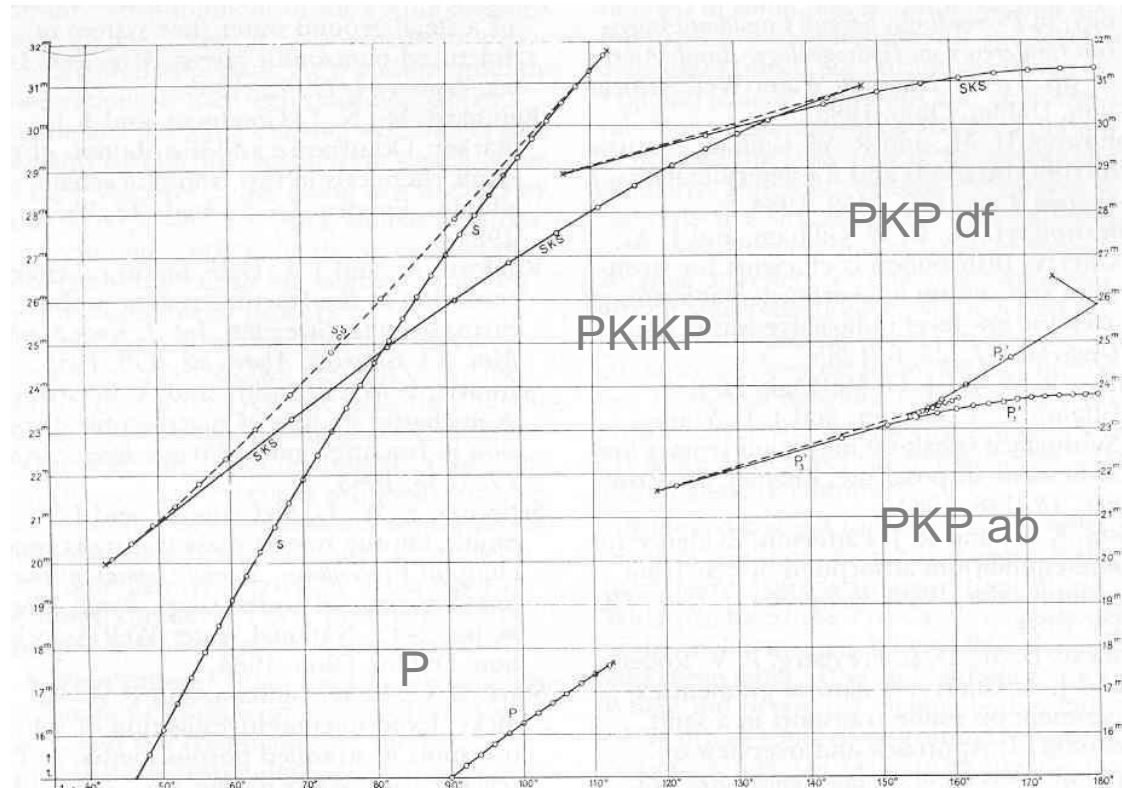
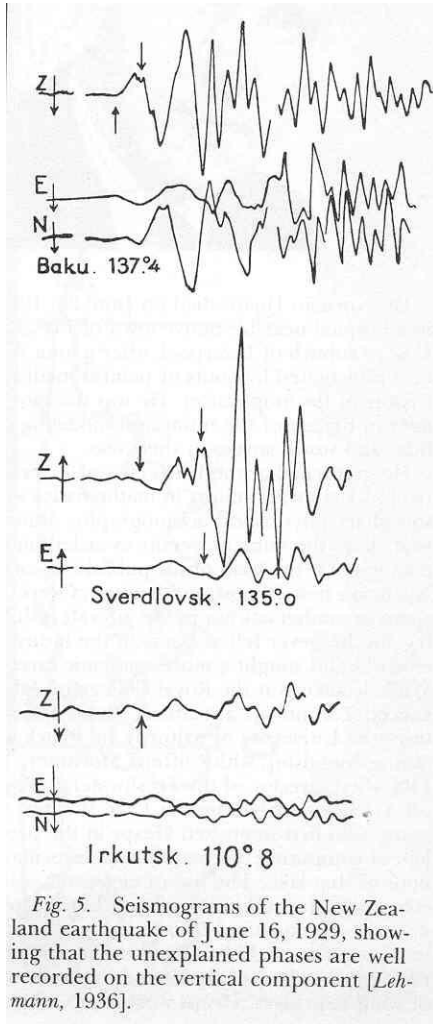
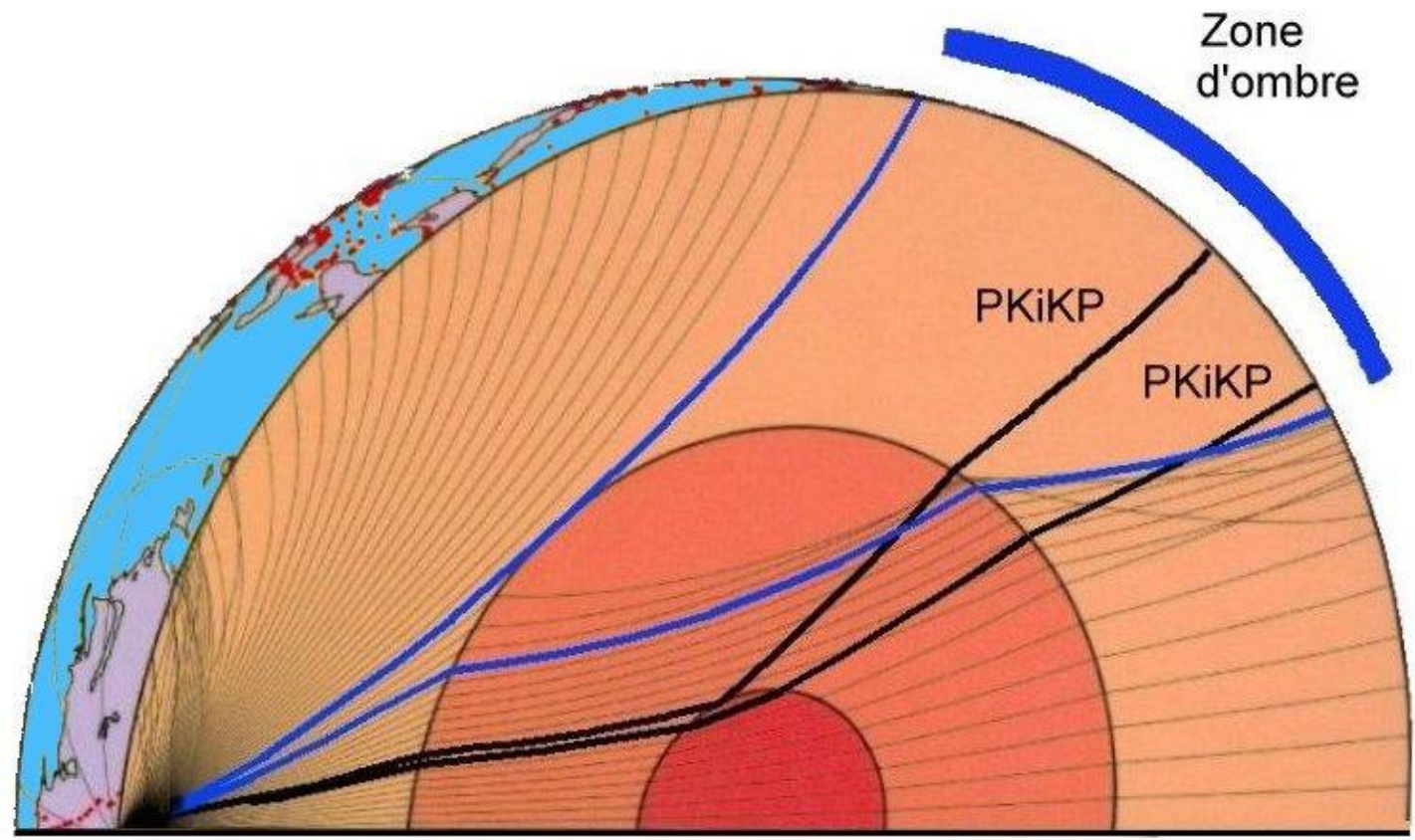
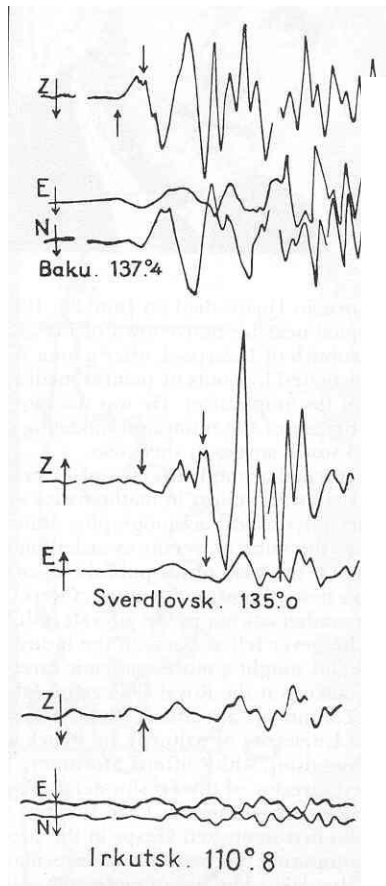
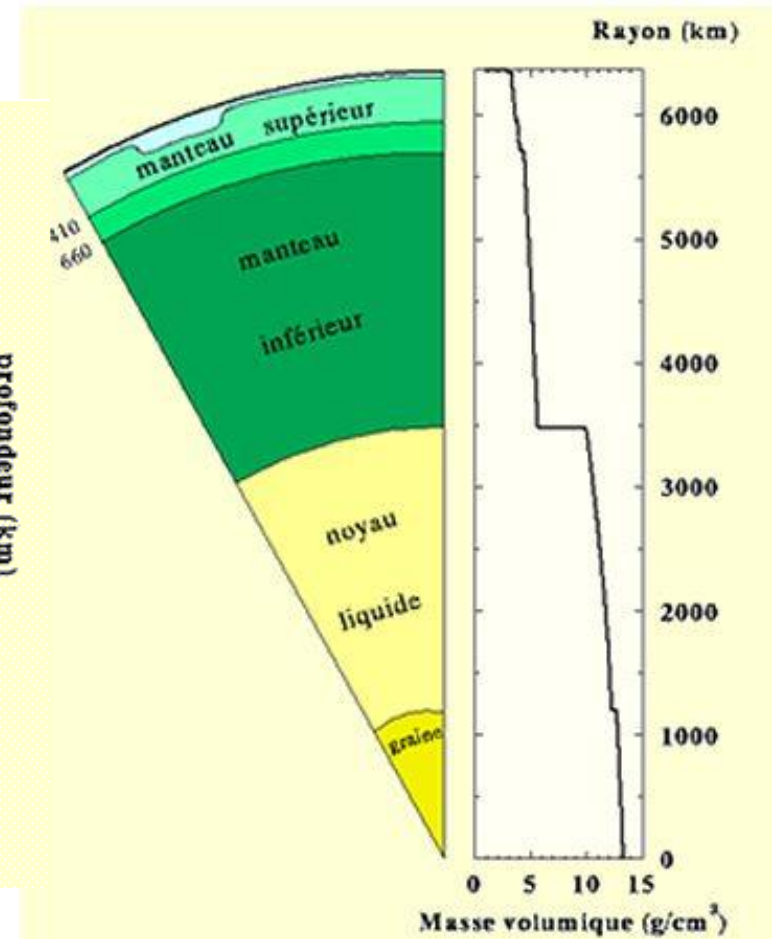
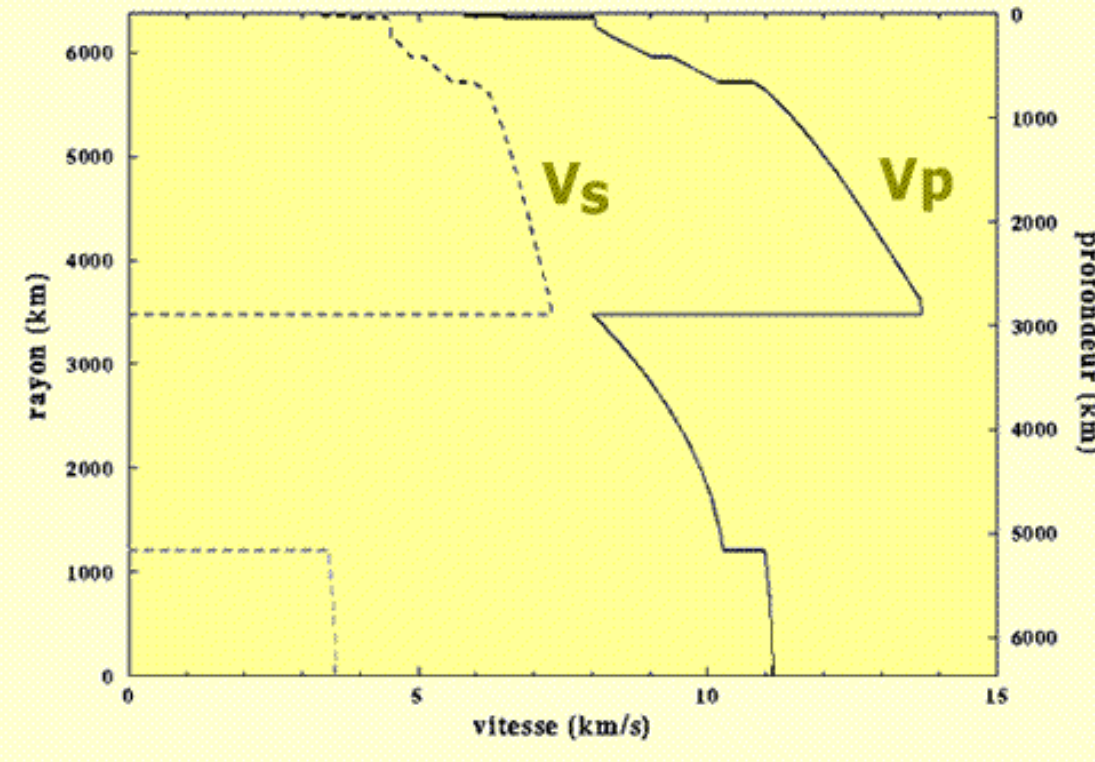


Fig. 7. Travel times for the earth model of Figure 6. The branch labeled  $P_3'$  (now PKIKP) explains the phases in Figure 5 [Lehmann, 1936].

# La découverte de la Graine – Inge Lehmann



# Imagerie sismique



PREM 1981



# La graine est-elle solide?

PKJKP

## GEOPHYSICS

### Shear properties of Earth's inner core constrained by a detected *J* waves in global correlation

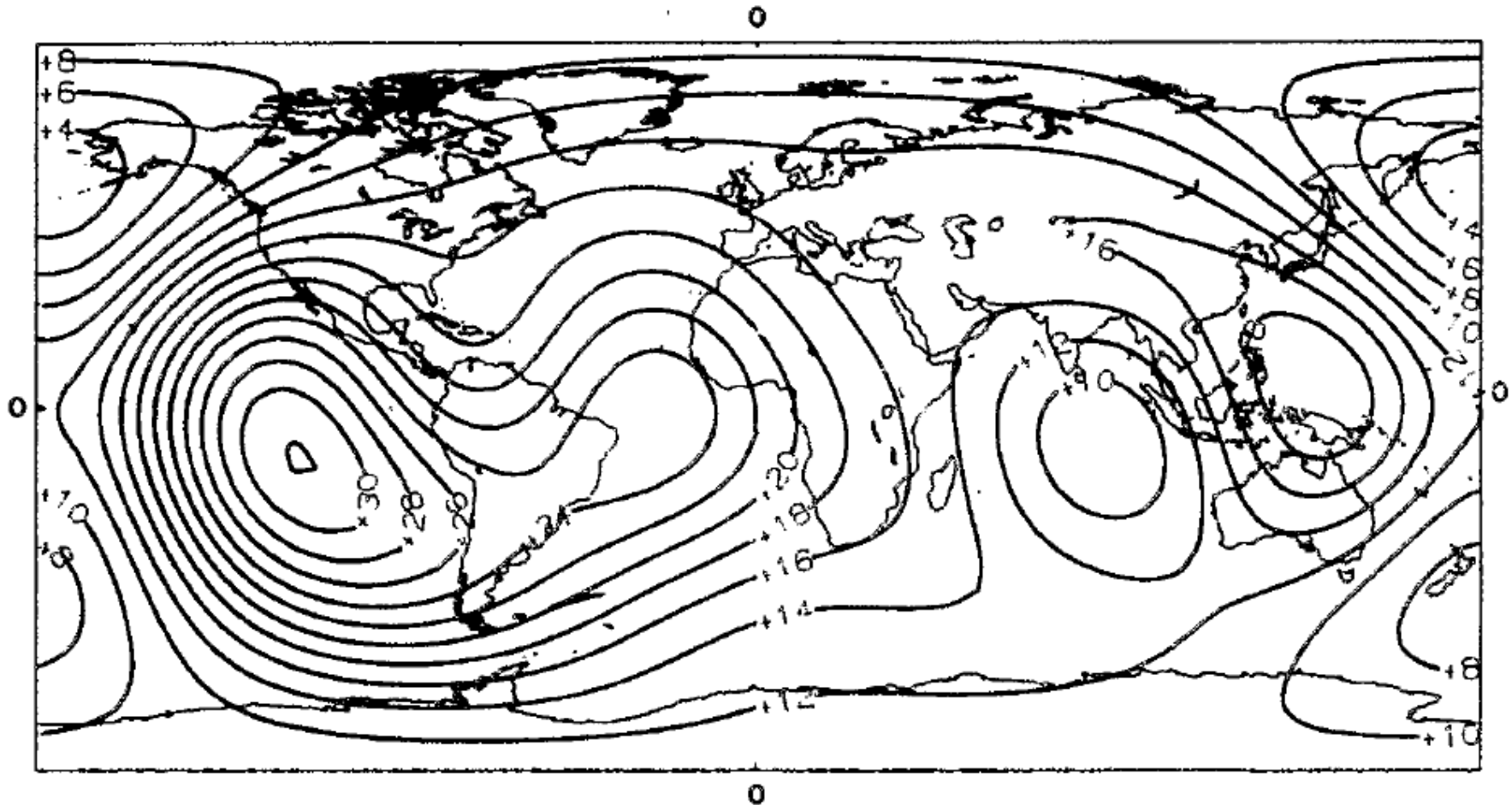
Hrvoje Tkalčić\* and Thanh-Son Phạm

Seismic *J* waves, shear waves that traverse Earth's inner core, provide direct information about the inner core's solidity and shear properties. However, these waves are difficult to detect because of their small amplitudes. We devised a method to detect *J* waves in the earthquake coda correlation wavefield. They are similar to other compressional core-sensitive signals. The inner core is softer, with shear-wave speeds and shear moduli of  $3.42 \pm 0.02$  km/s and  $149.0 \pm 1.6$  gigapascals (GPa) near the inner core boundary and  $3.58$  km/s and  $167.4 \pm 1.6$  GPa in Earth's center. The values are 2.5% lower than the Preliminary Earth Reference Model. This provides new constraints on the interpretation of Earth's inner core.

Science - 2018

The screenshot shows the ABC News website interface. At the top, there's a navigation bar with 'Sites', 'ABC', 'Log In', and 'Search'. Below that is the 'NEWS' logo and a 'SET LOCATION' button. The main navigation menu includes 'Just In', 'Politics', 'World', 'Business', 'Sport', 'Science', 'Health', 'Arts', 'Analysis', 'Fact Check', and 'More'. The 'Science' section is highlighted, with sub-sections for 'Space', 'Nature', 'Humans', 'Technology', and 'Programs'. A blue banner for 'Invictus Games' is visible. The main article headline is 'Revealed by earthquakes, Earth's inner core may be softer than previously thought'. Below the headline are social media sharing options for Facebook and Twitter, and a 'Print' icon. The article is attributed to 'ABC Science' by science reporter 'Belinda Smith', posted yesterday at 21:06. The main image is a cross-section of Earth's inner core, showing a spiral pattern of seismic waves. To the right, there are two 'TOP SCIENCE STORIES' thumbnails: one showing a large fish and another showing a diver underwater.

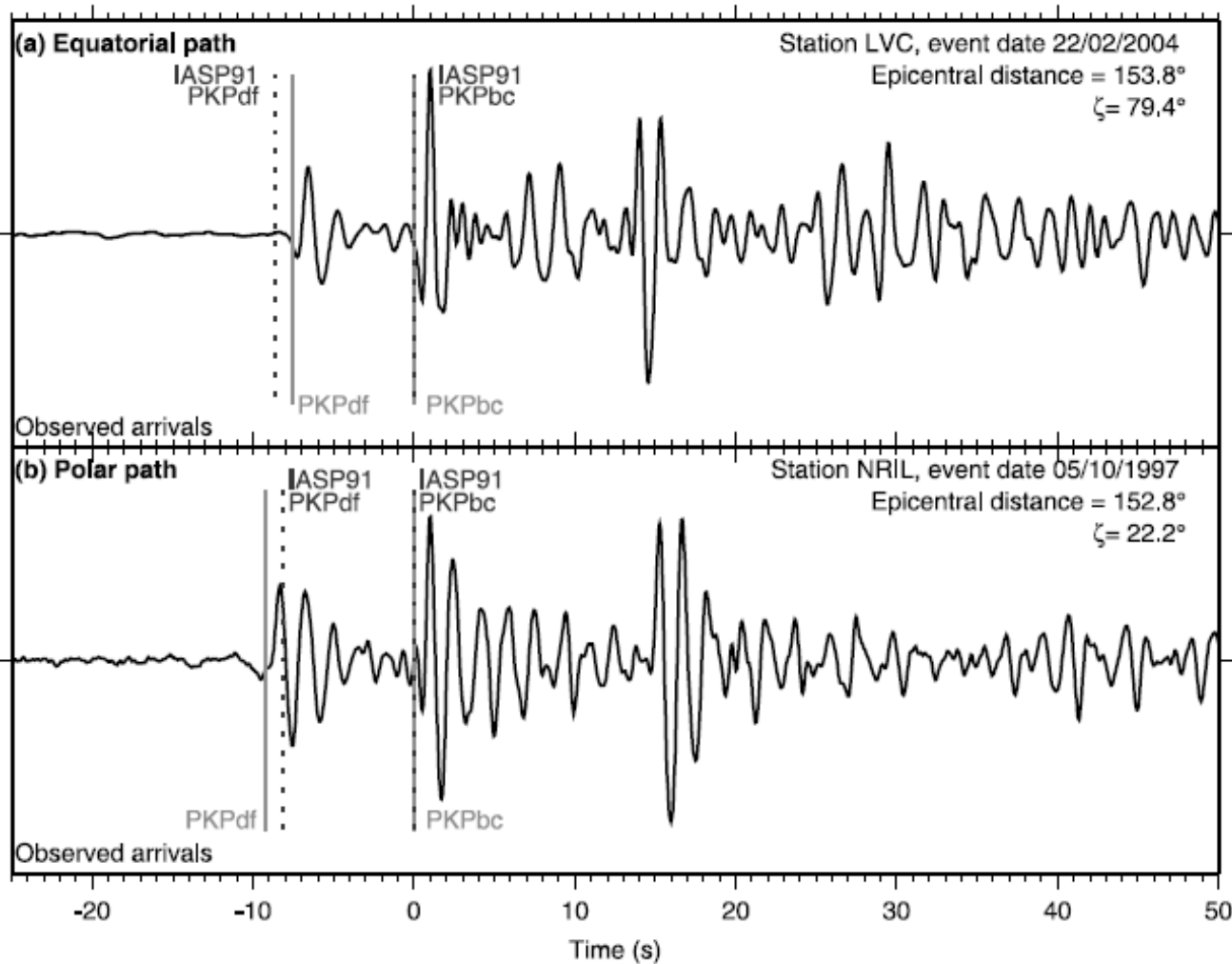
# Anisotropie sismique de la Graine



**Fig. 4** Spherical harmonics expansion up to a degree 4 of the PKIKP-P travel-time residual field. Values are in tenths of a second. A low number means a fast velocity in the core.

Poupinet et al, 1983

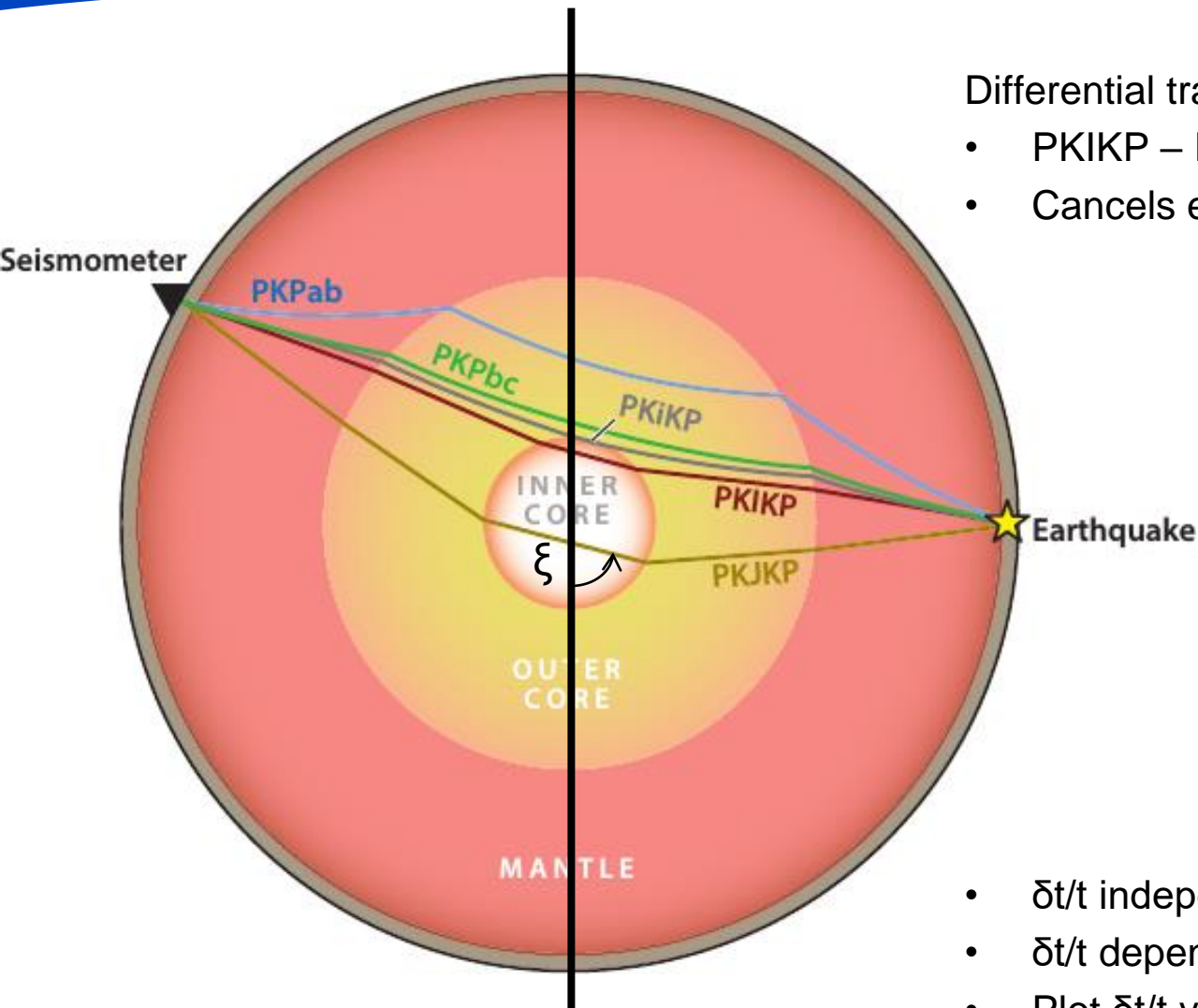
# Difference de temps d'arrivée



Annie Souriau  
Georges Poupinet  
ISTerre, oct 2013

Poupinet et al, nature 1983, Souriau 2008

# Séismologie différentielle



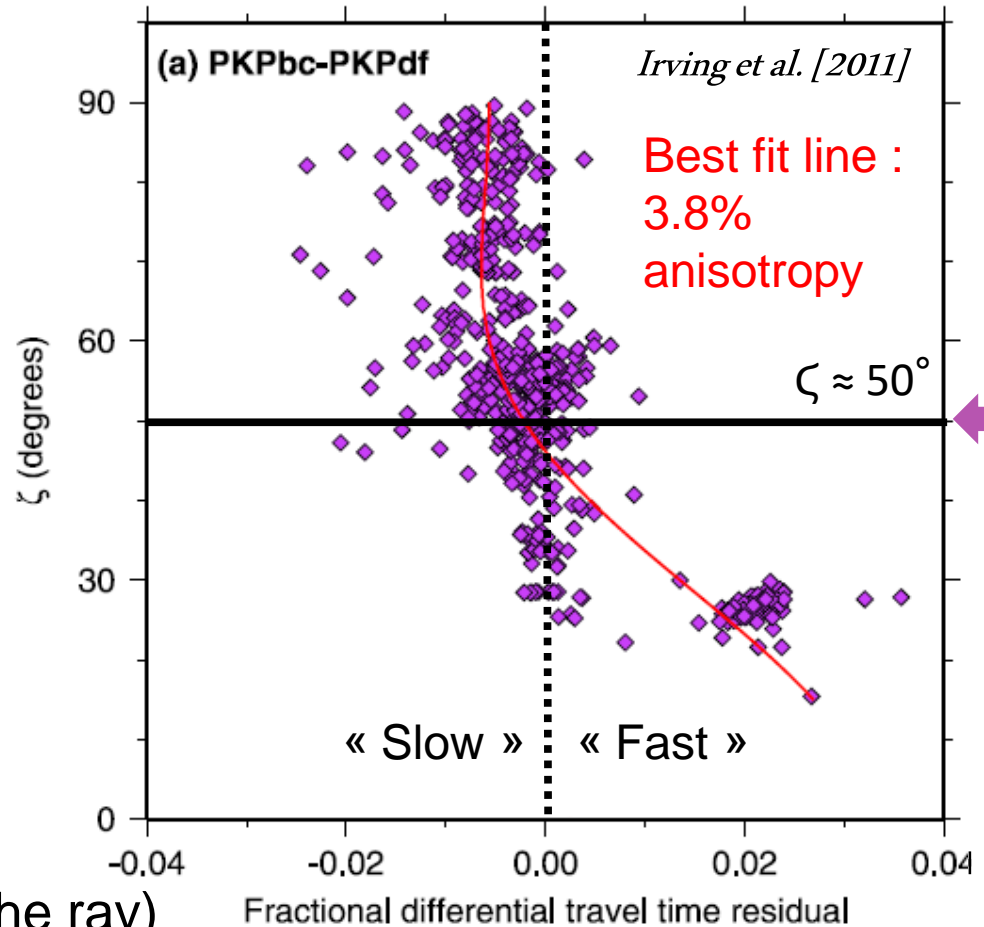
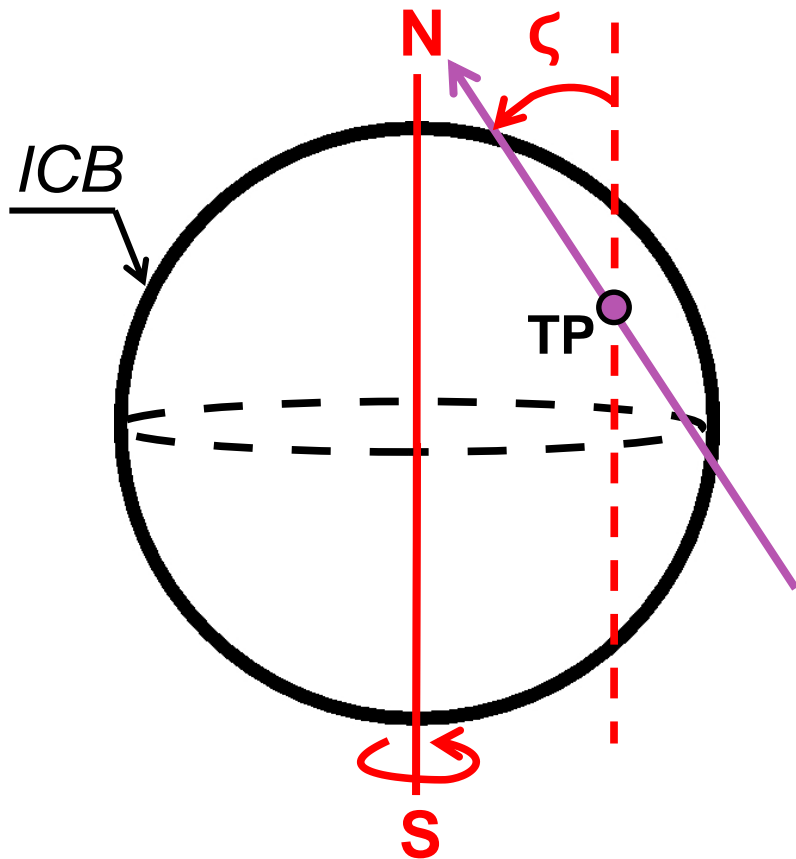
Differential travel time  $\delta t$ :

- PKIKP – PKiKP, or other combinations
- Cancels effects of mantle and crust

- $\delta t/t$  independent of  $\xi$ : no anisotropy
- $\delta t/t$  depends on  $\xi$ : anisotropy
- Plot  $\delta t/t$  vs.  $\xi$ , angle to Earth rotation axis

Illustration : Deuss, *Annu. Rev. Earth Planet. Sci.* 2015

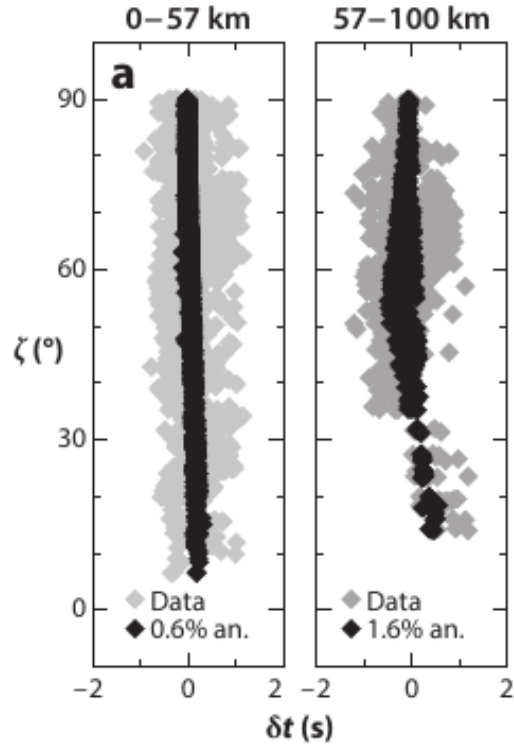
# La graine est anisotrope!



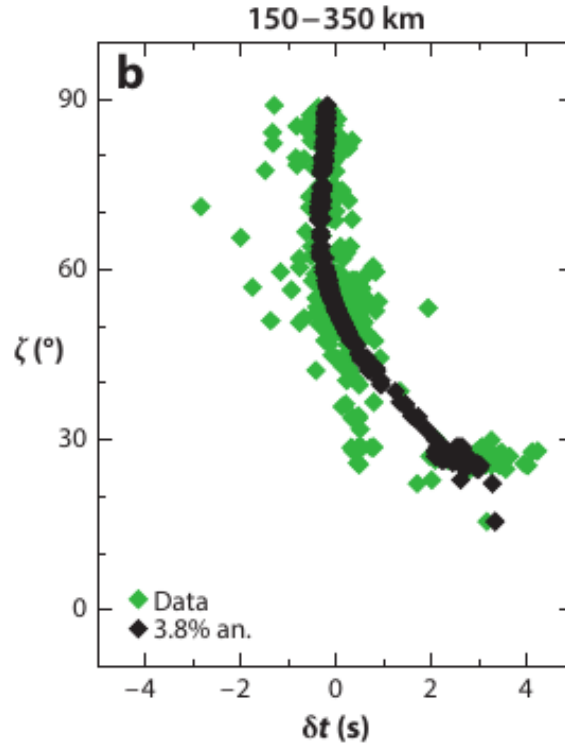
**TP** : turning point (deepest point of the ray)

# L'anisotropie dépend de la profondeur

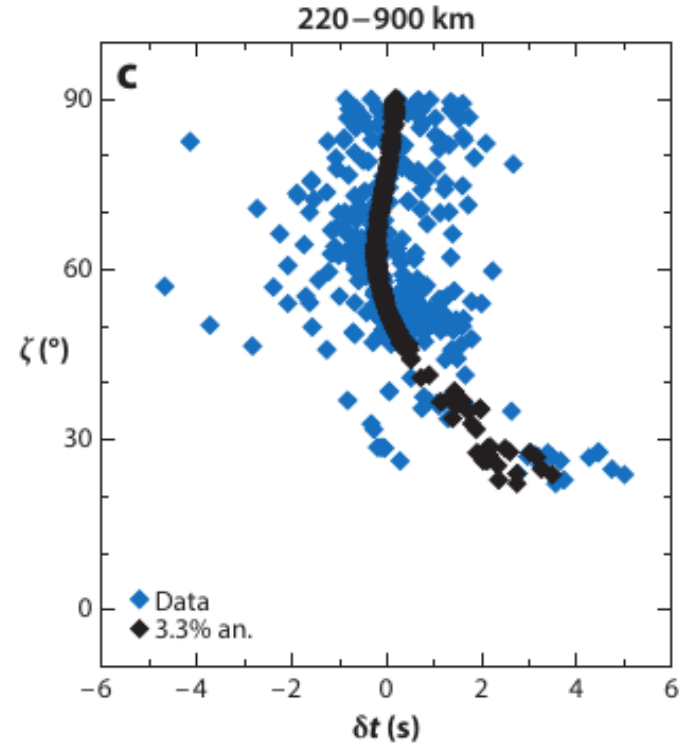
PKiKP-PKIKP



PKPbc-PKIKP



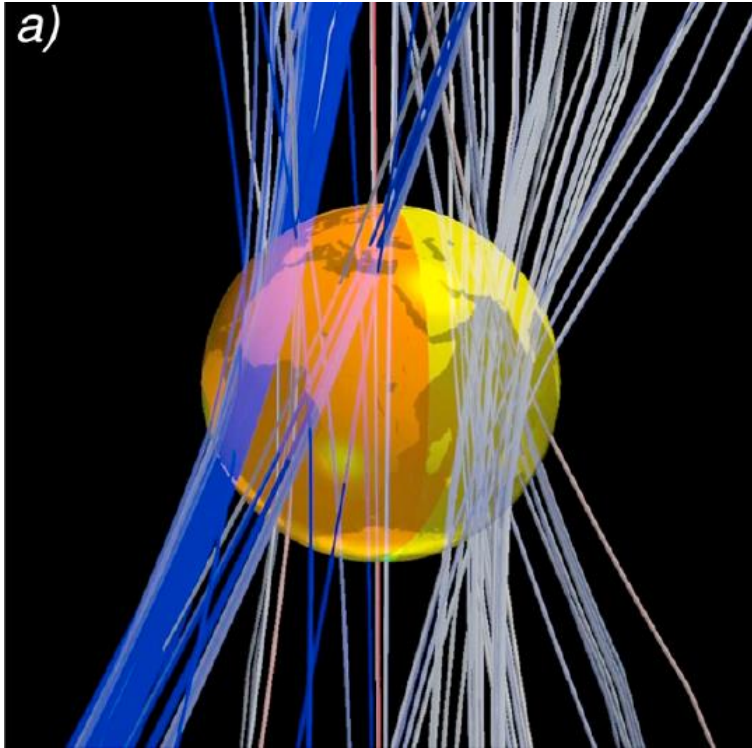
PKPab-PKIKP



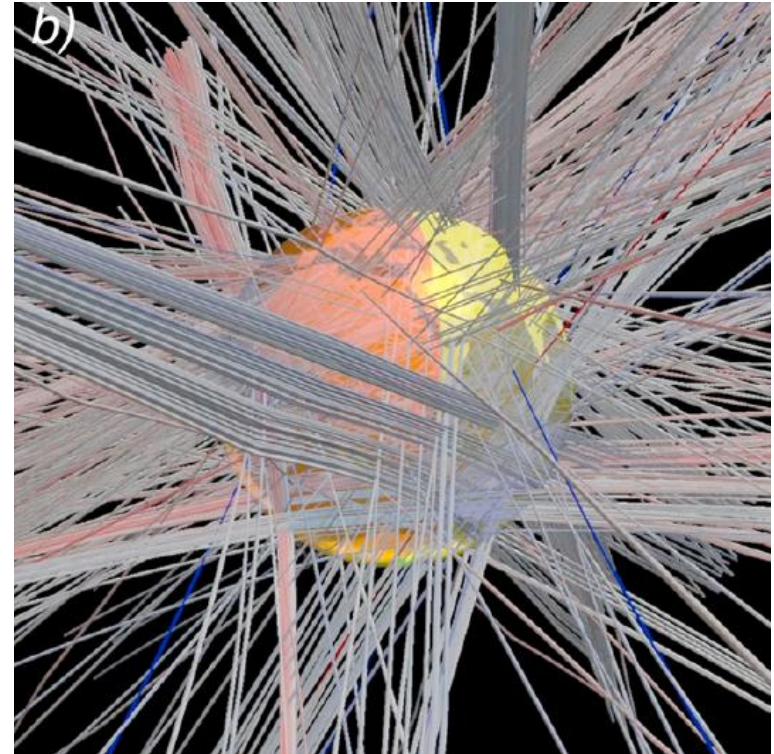
Deuss, *Annu. Rev. Earth Planet. Sci.* 2014  
Data are from Irving & Deuss (2011a) and Waszek & Deuss (2011)

# Très peu de rais sismiques...

Quasi-polar PKIKP raypaths  
 $\xi \leq 35^\circ$



Quasi-equatorial PKIKP raypaths  
 $\xi > 35^\circ$



- 1- Very incomplete coverage (N-S path particularly)
- 2- Waves go through the whole inner core

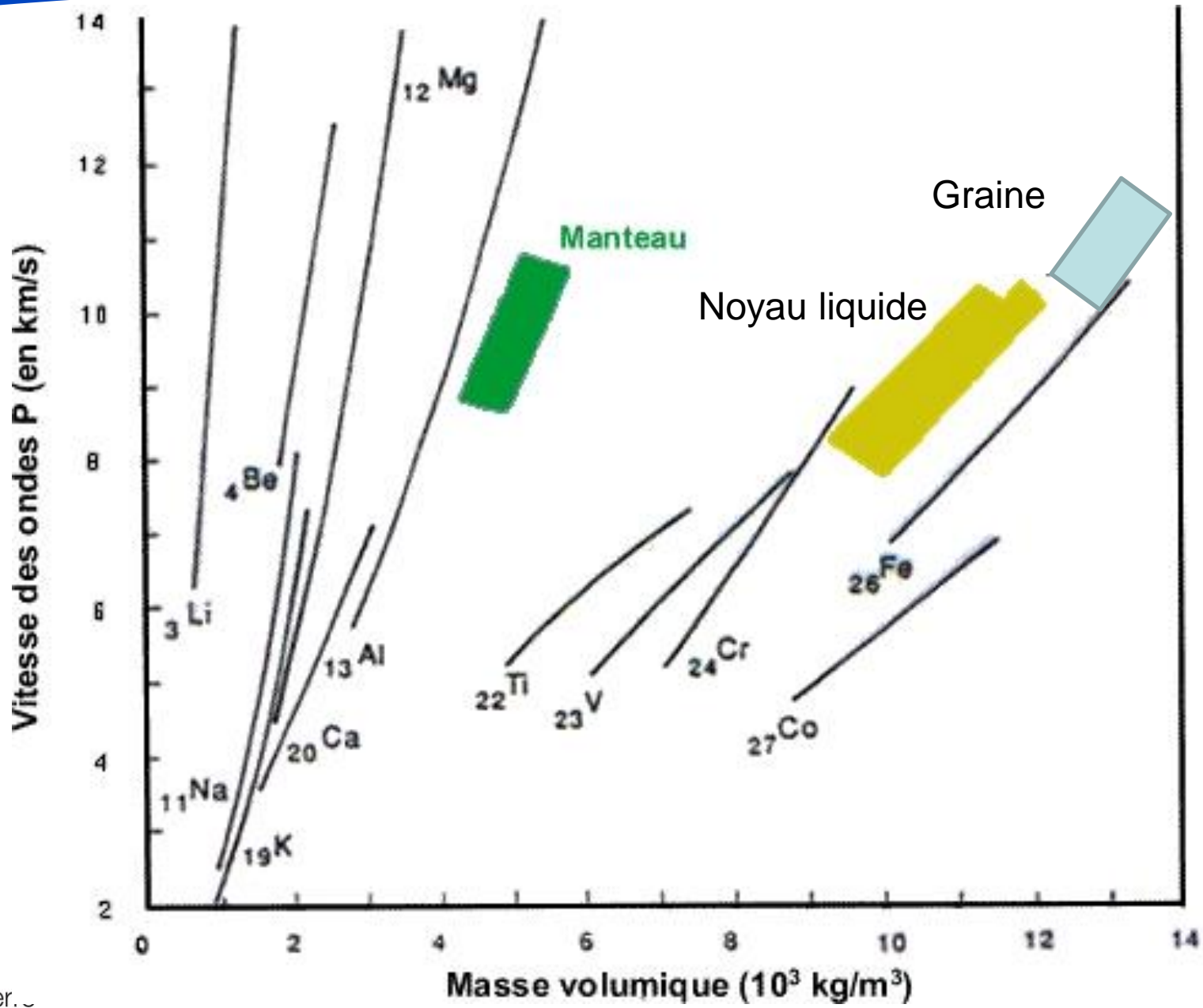
Illustration : Tkalčić, *Rev Geophys.* 2015

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# Loi de Birch



# Géochimie du noyau

Terre =  $\Sigma$  météorites chondritiques

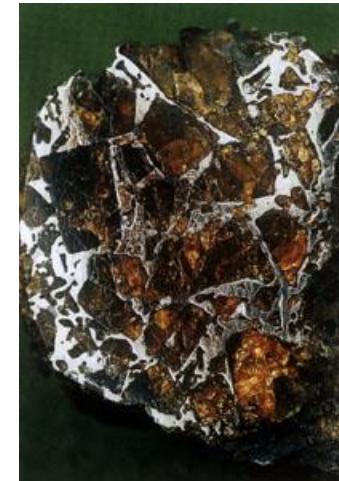
Noyau = Terre - croute - manteau



Chondrite

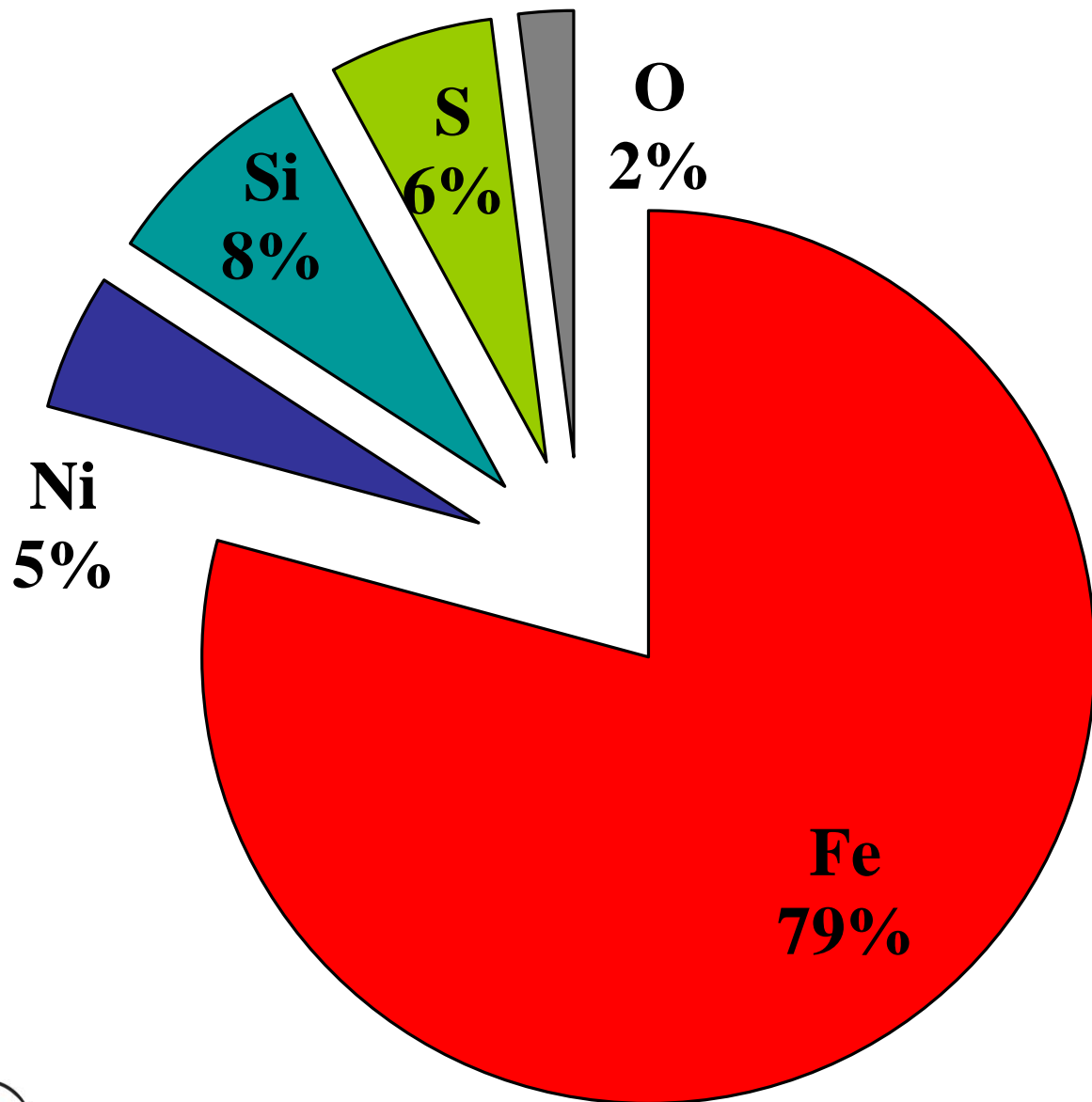


Météorite de Fer



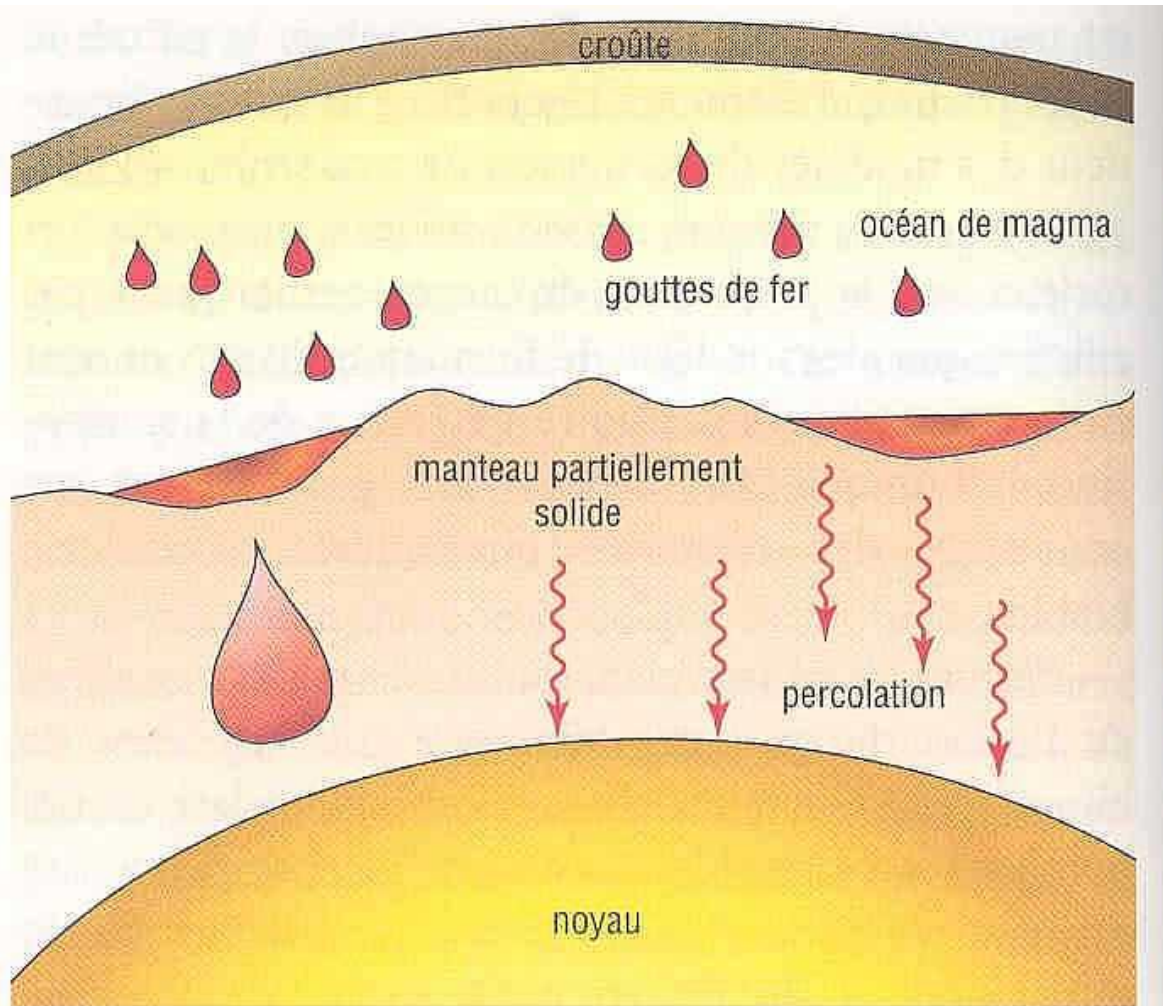
Pallasite

# Composition géochimique du noyau



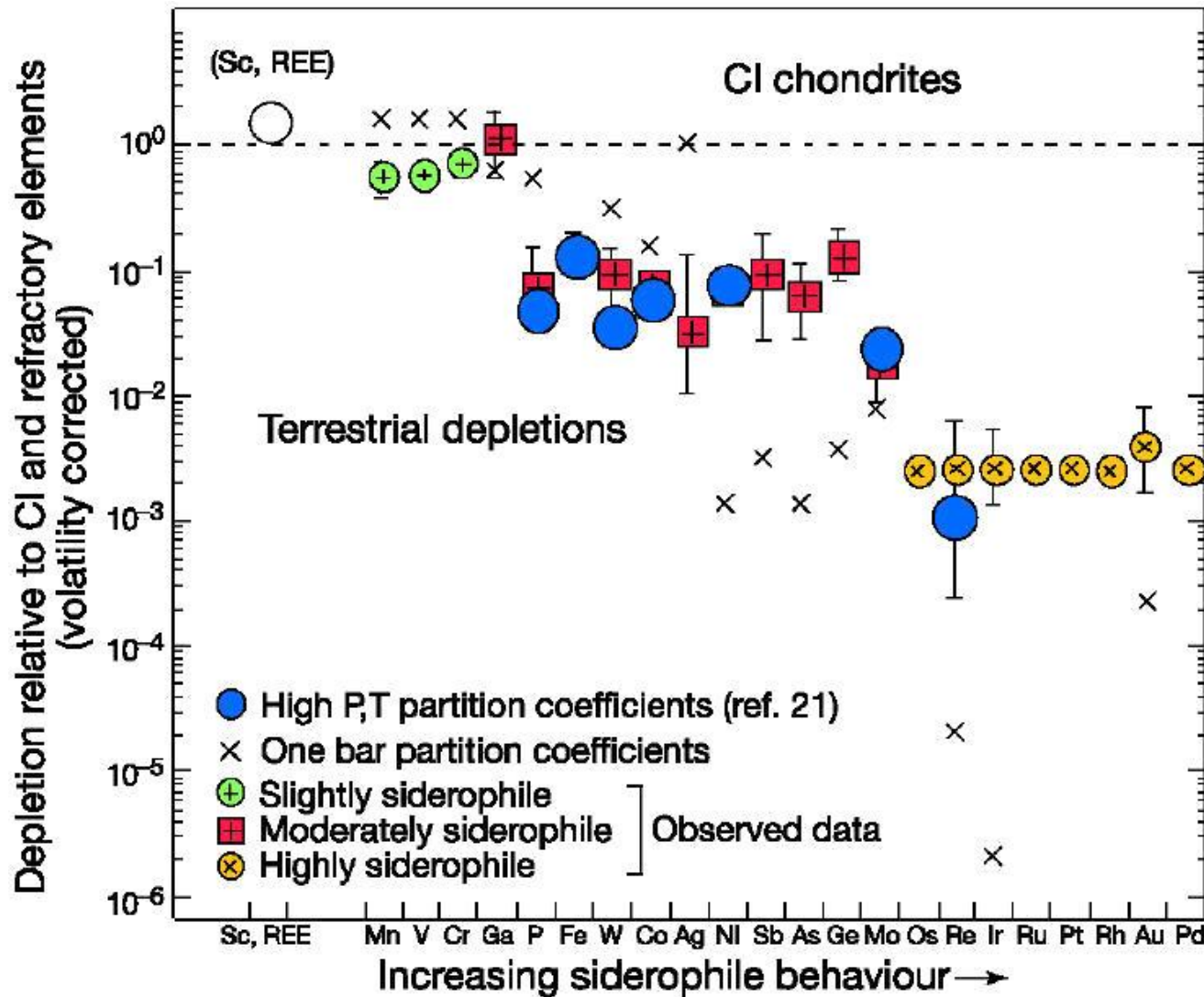
Allegre et al, 1995

# Formation du noyau



Source : D. J. Stevenson, *Science*, 1981.

# Sidérophile/lithophile



Drake et al, 2002

# Mélange turbulent métal/silicates

306

R. Deguen et al. / Earth and Planetary Science Letters 310 (2011) 303–313

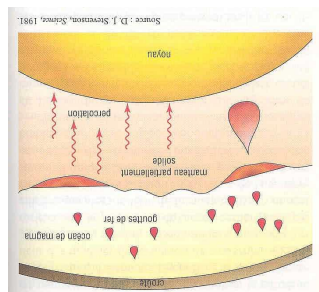
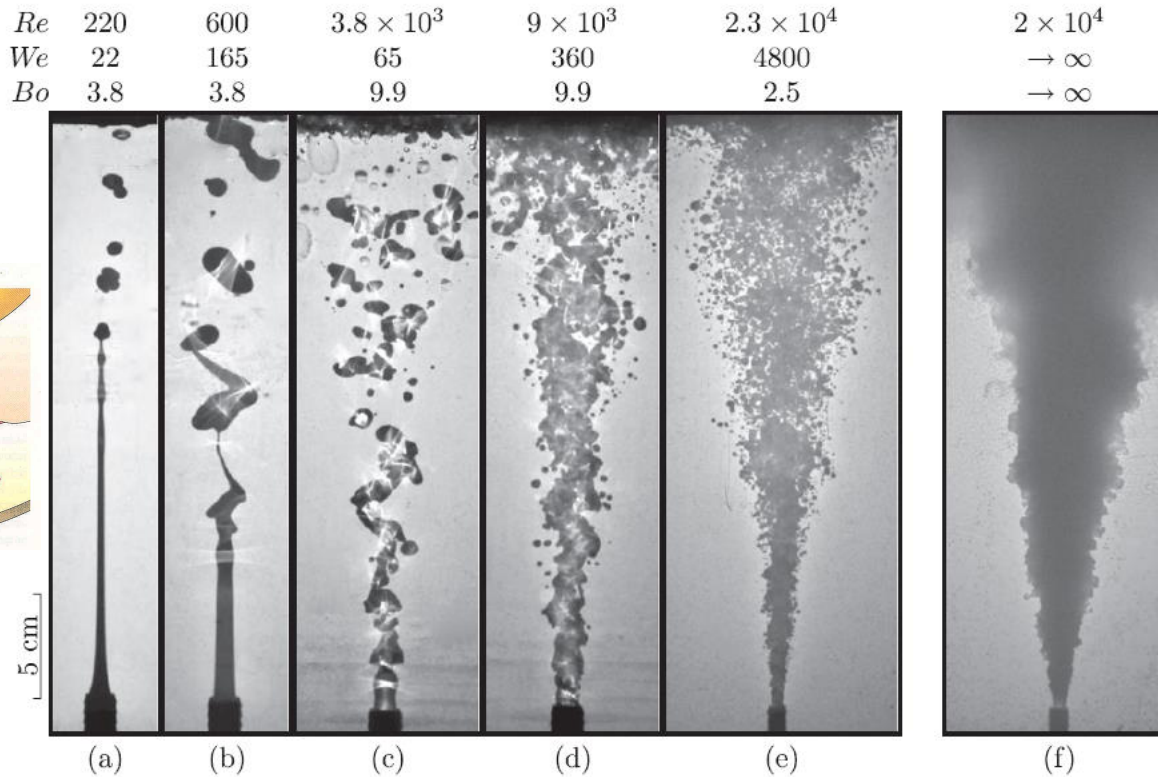
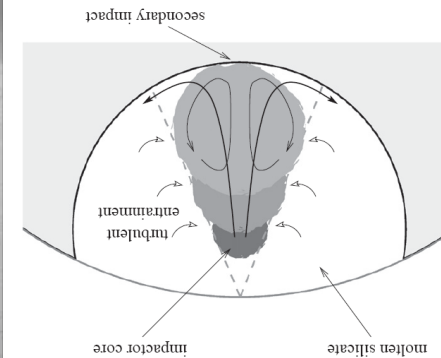


Fig. 2. A schematic view of the evolution of a large impactor core (gray) in a magma pool.

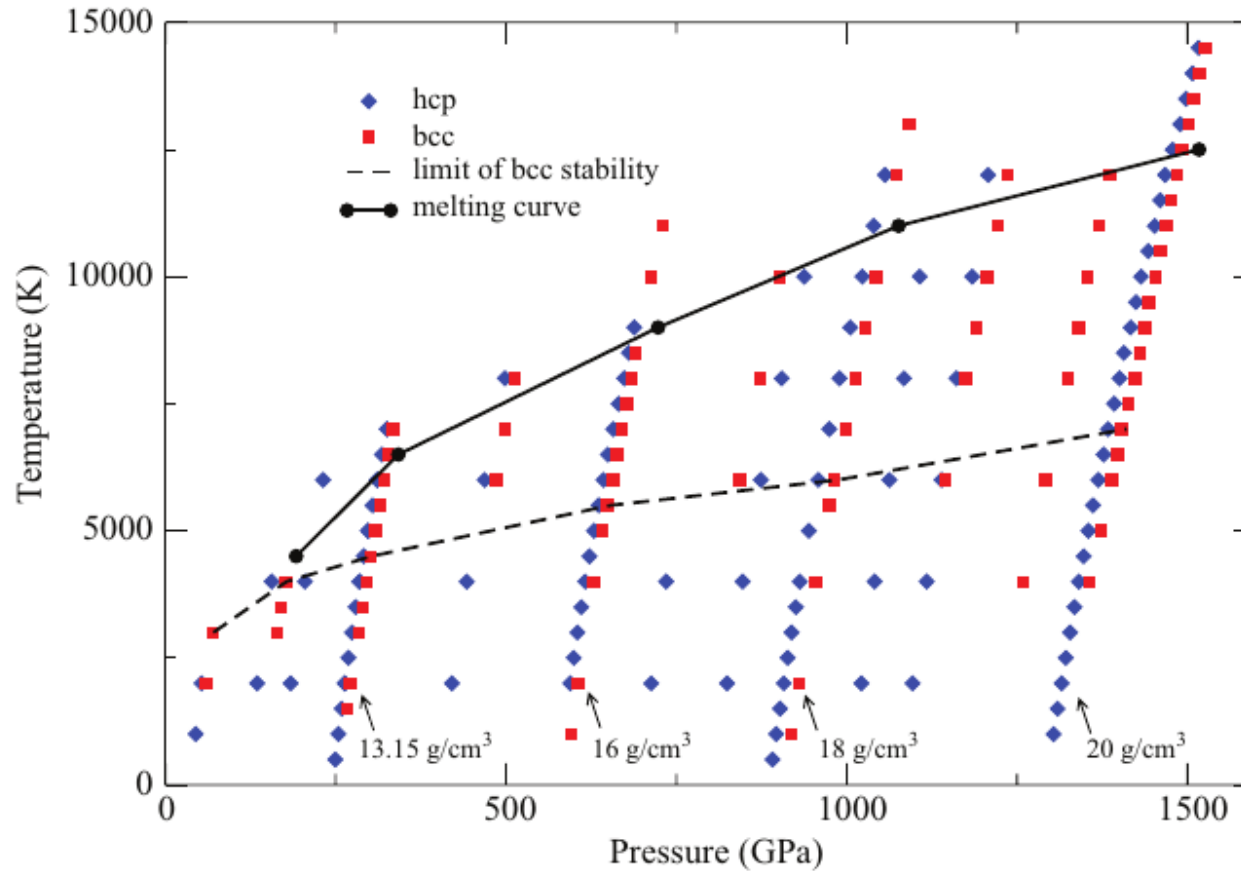


**Fig. 1.** Forced plumes in water. Canola oil is used in the experiments shown in a) and b) ( $\lambda = 0.1$ ,  $\Delta\rho/\rho_w = 0.08$ ), and a low viscosity silicone oil is used in the experiments shown in c) to e) ( $\lambda = 1.2$ ,  $\Delta\rho/\rho_w = 0.18$ ). f): forced plume of a water–alcohol mixture (density  $\rho = 810 \text{ kg}\cdot\text{m}^{-3}$ ) in cold water. In a), disruption is due to the Rayleigh–Plateau capillarity instability; fragmentation is due mainly to shear instabilities in d) and e). See text for dimensional parameters values.

# Diagramme de phase « théorique » du Fe

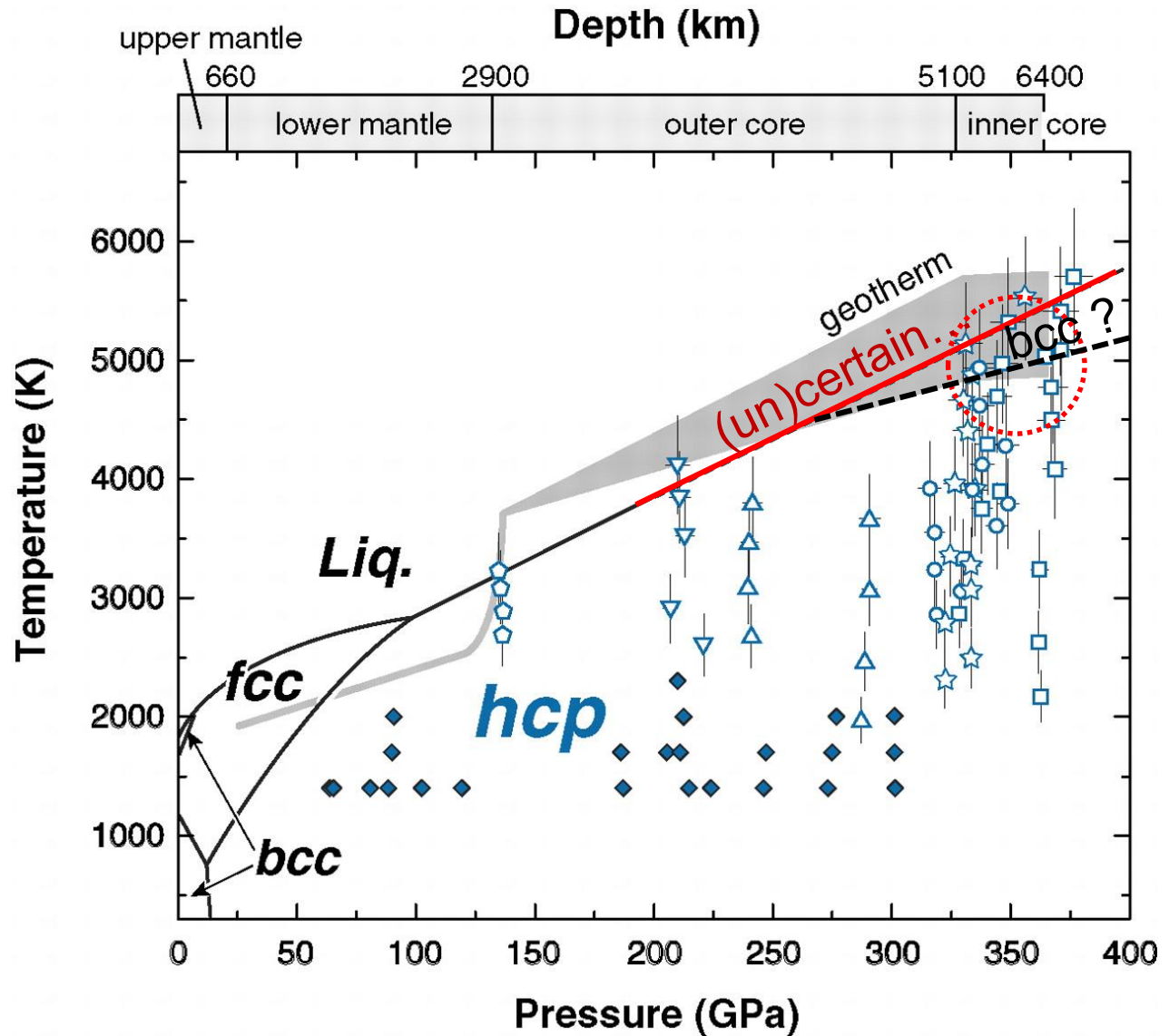
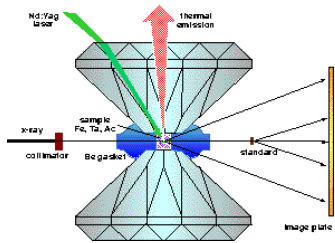
PHYSICAL REVIEW B **87**, 094102 (2013)

## *Ab initio* equation of state of iron up to 1500 GPa



# Diagramme de phase « expé » du Fe

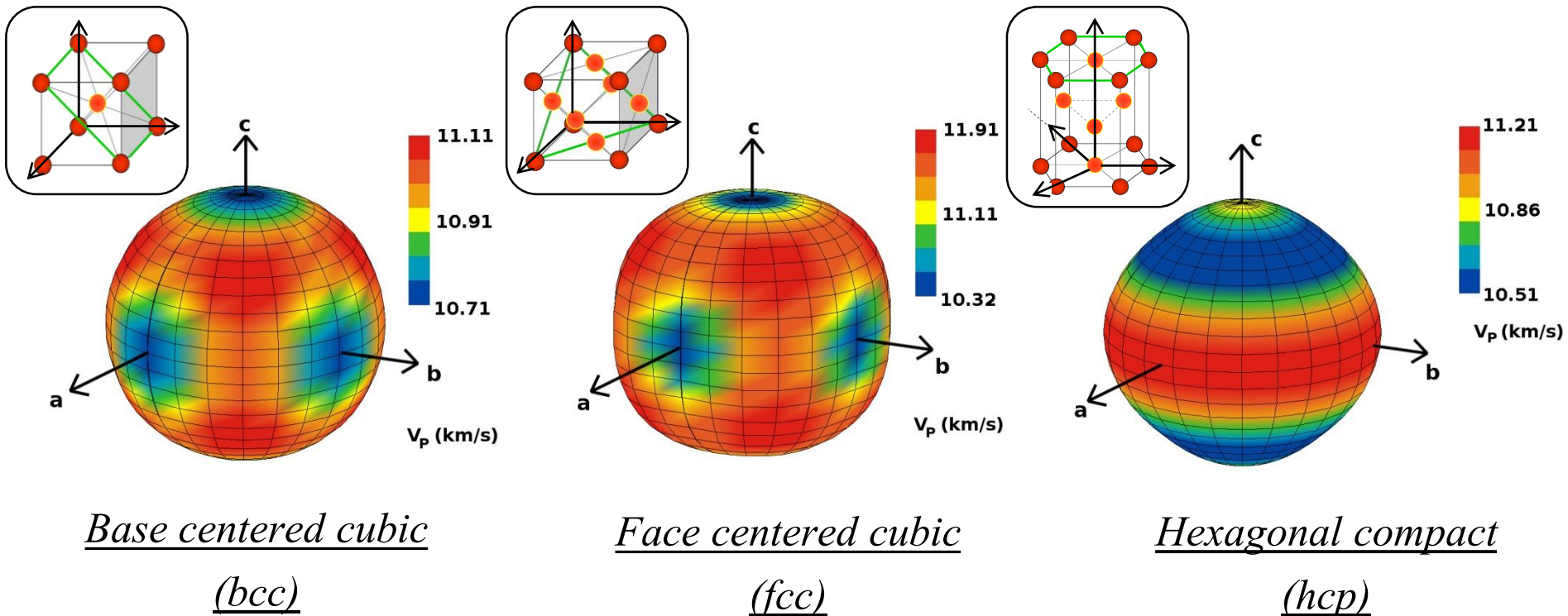
Tateno et al. [2010]





# Anisotropie cristalline

3 possible cristallographic phases for Fe at the inner core conditions



Base centered cubic  
(bcc)

Face centered cubic  
(fcc)

Hexagonal compact  
(hcp)

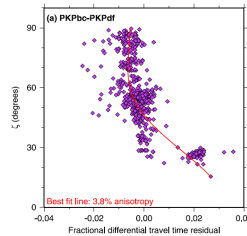
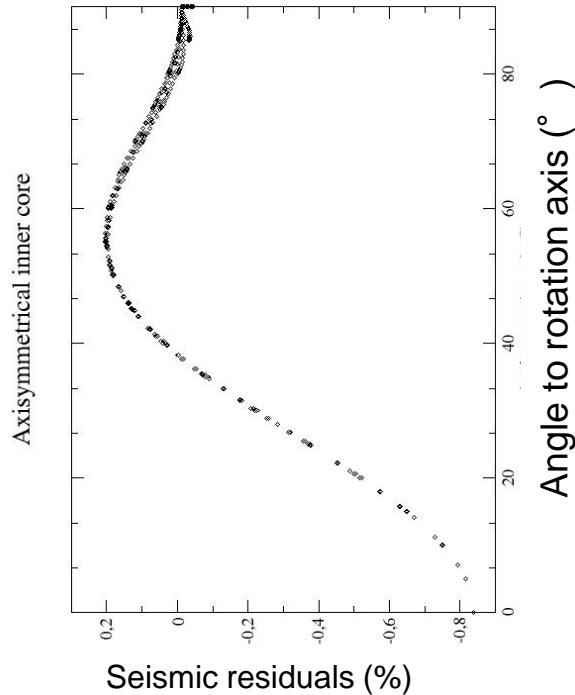
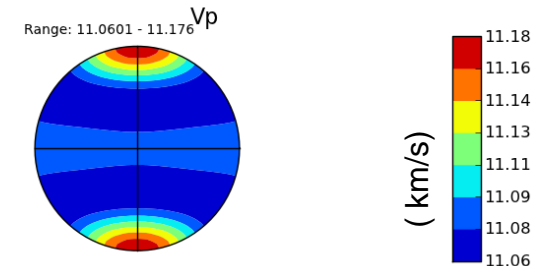
Vocadlo, 2007

Vocadlo, 2008

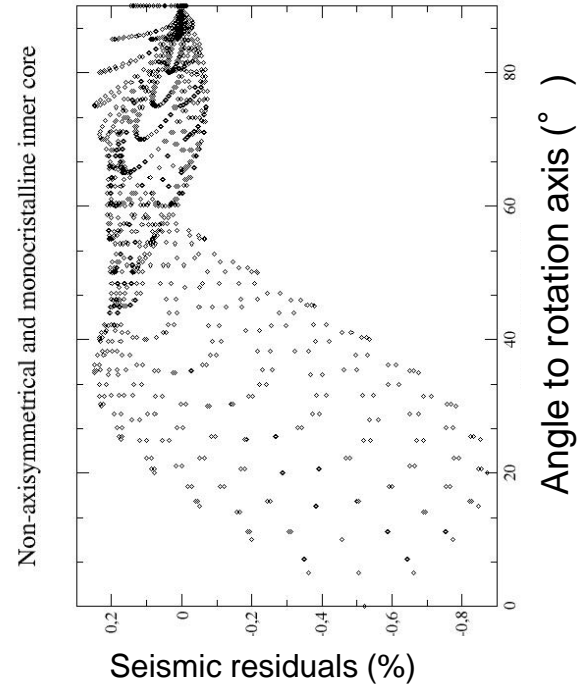
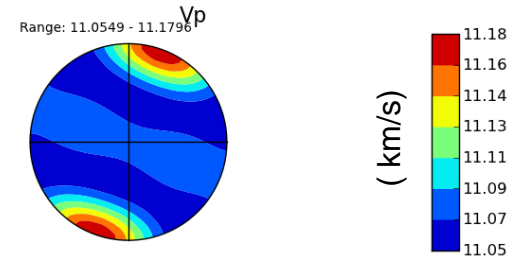
Vocadlo, 2009

# La graine: un monocristal?

## Axisymmetric single cristal inner core



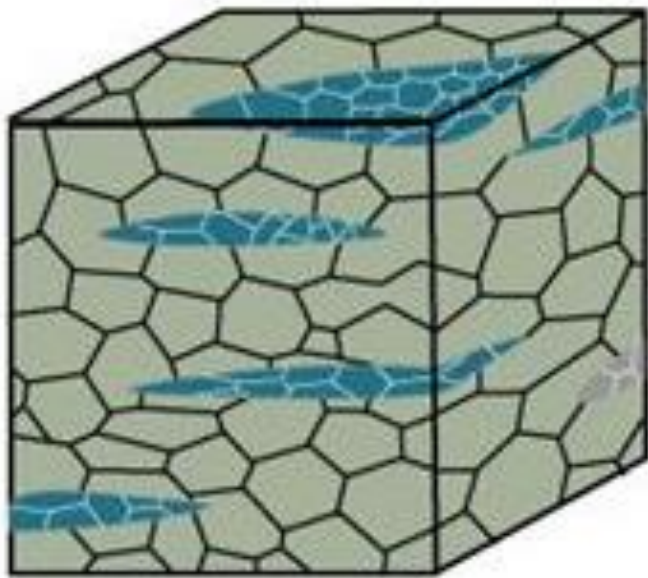
## Non-axisymmetric single cristal inner core



# Source d'anisotropie polycristalline

Shape preferred orientation

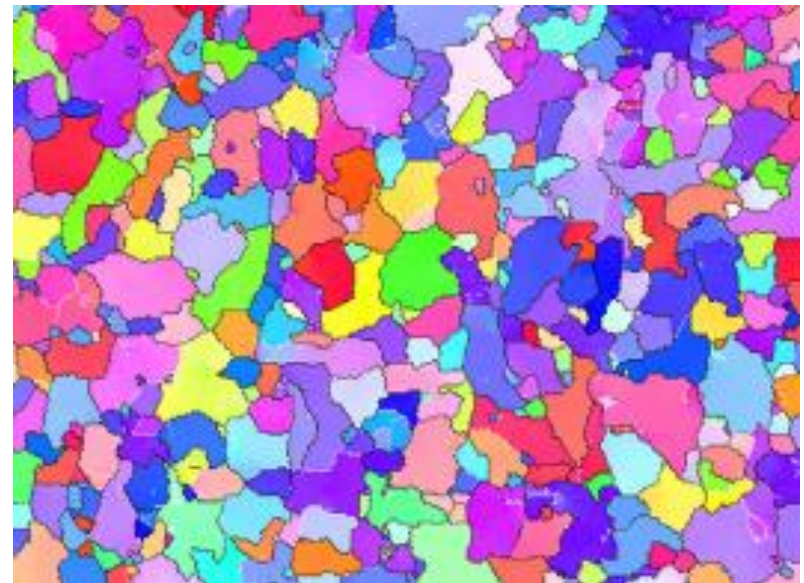
- Aligned grain shapes
- Aligned melt pockets



SPO in the inner core  
"Structural anisotropy"  
How were the SPO generated?

Lattice preferred orientations

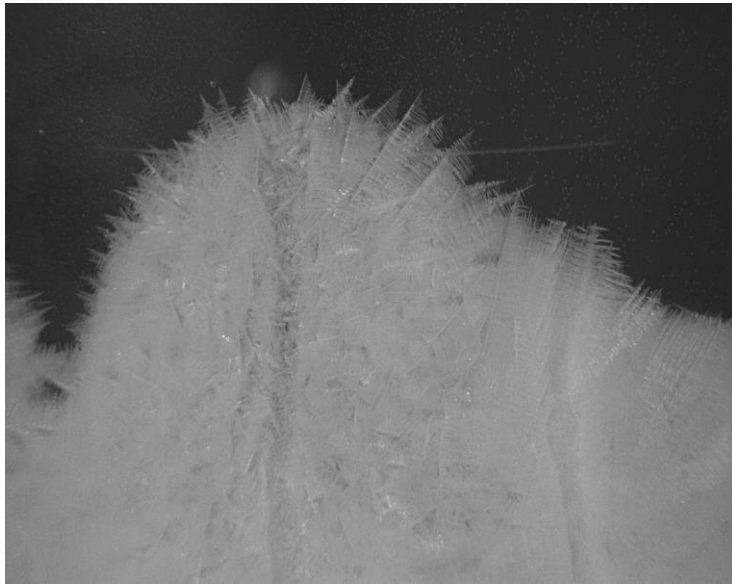
- Crystallization
- Plastic deformation



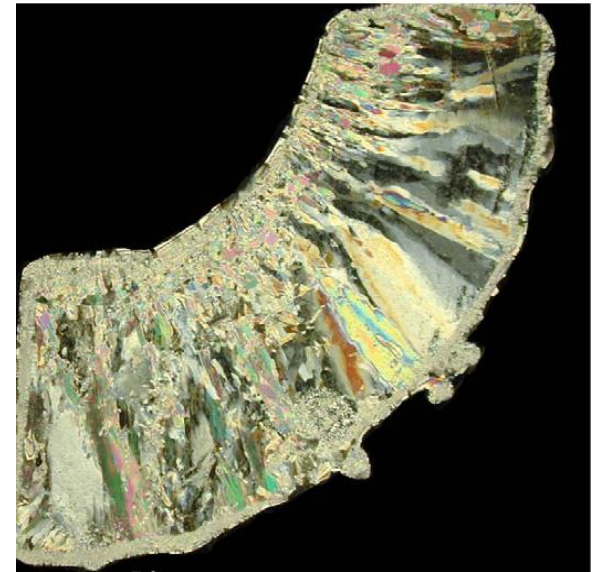
LPO in the inner core  
"Deformation anisotropy"  
Coupling of IC dynamics and  
anisotropy

# Solidification de cristaux

Cristallographic Preferred Orientation CPO

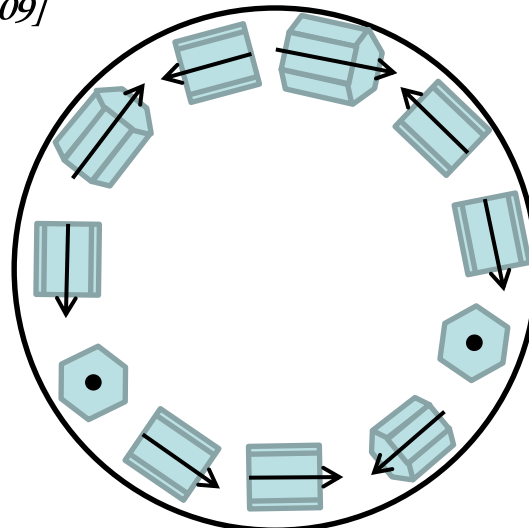


*Deguen [2009]*



*Bergman [2005]*

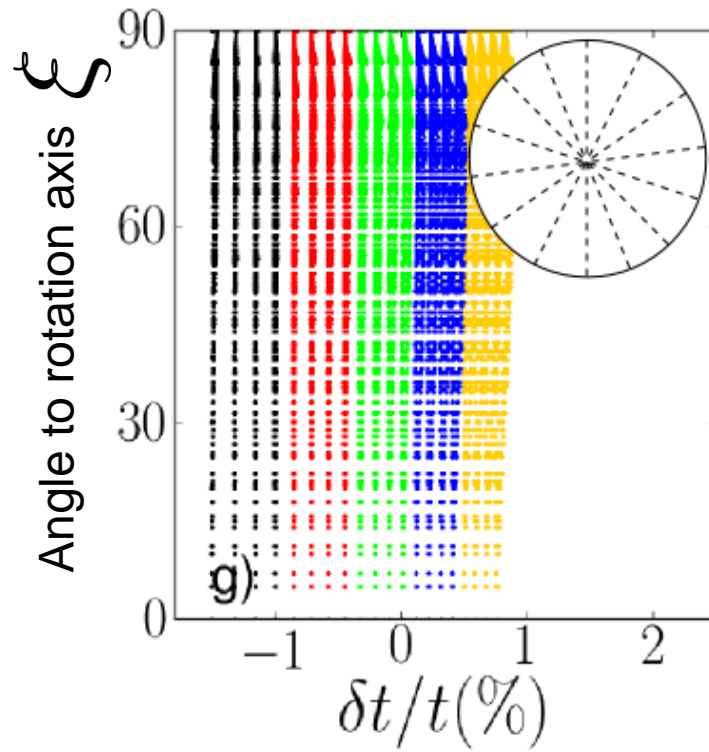
Spherical cristallisation



La graine terrestre

# Graine cristallisée sphérique

300 000 synthetic rays probing the inner core



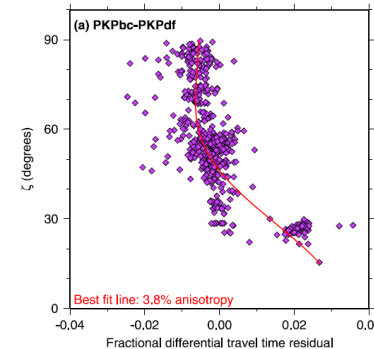
Preferred alignment direction:  
For *c*-axes ———  
For *a*-axes - - -

- 0-244 km
- 244-488 km
- 488-733 km
- 733-977 km
- 977-1221 km

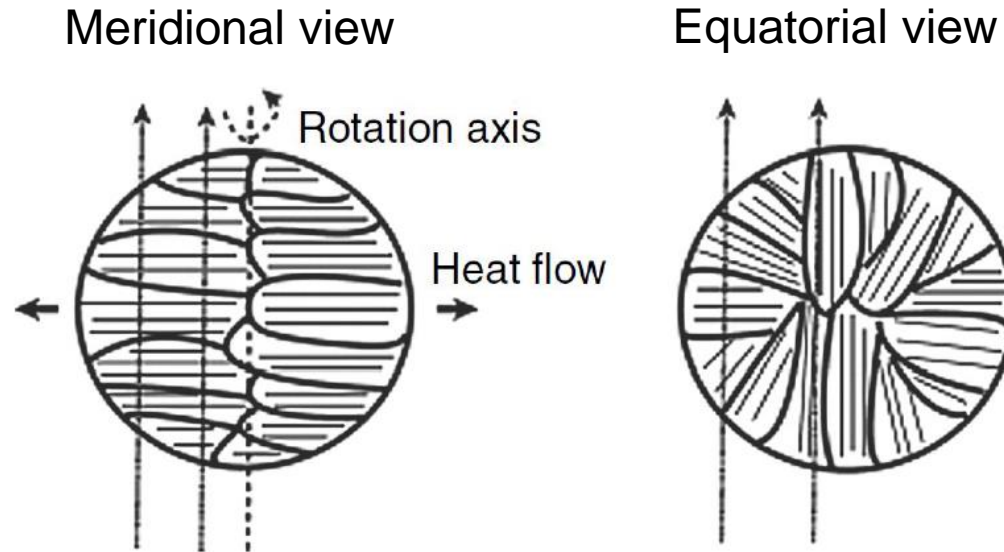
## Seismic residuals

$$\frac{\delta t}{t} = \frac{s_{ray} - s_0}{s_0}$$

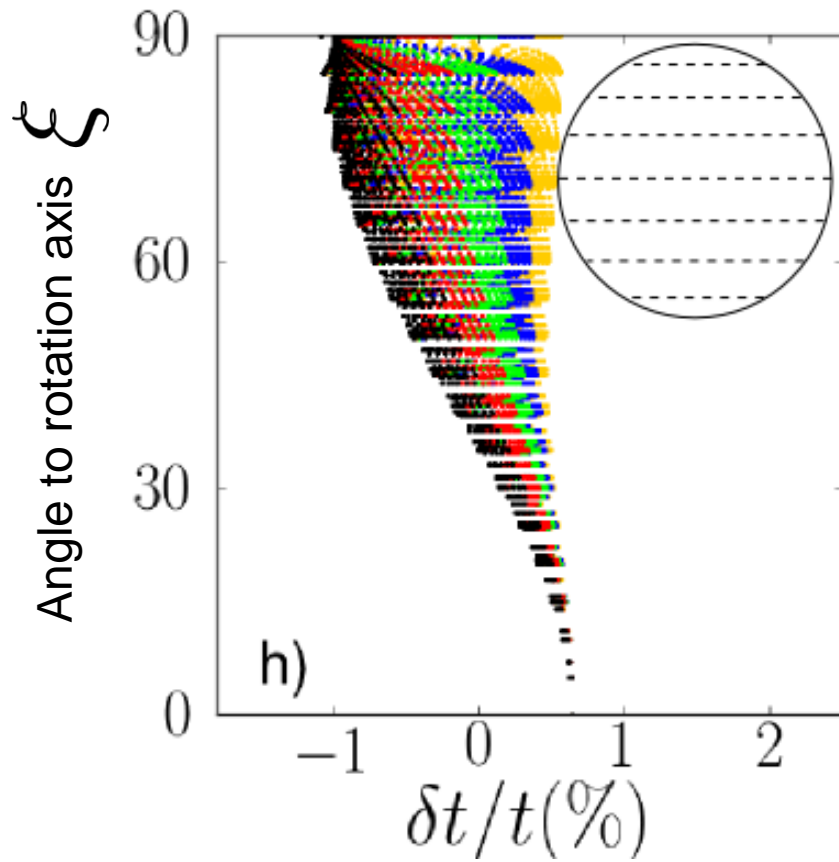
Where  $s_0$  = average slowness in IC



# Graine cristallisée cylindrique

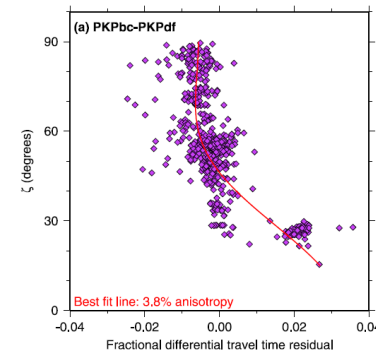


*Bergman [1997], Sumita [2007]*



Preferred alignment direction:  
 For *c*-axes     |  
 For *a*-axes     |

- 0-244 km
- 244-488 km
- 488-733 km
- 733-977 km
- 977-1221 km



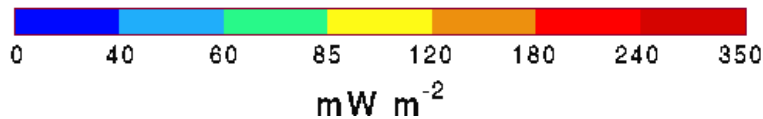
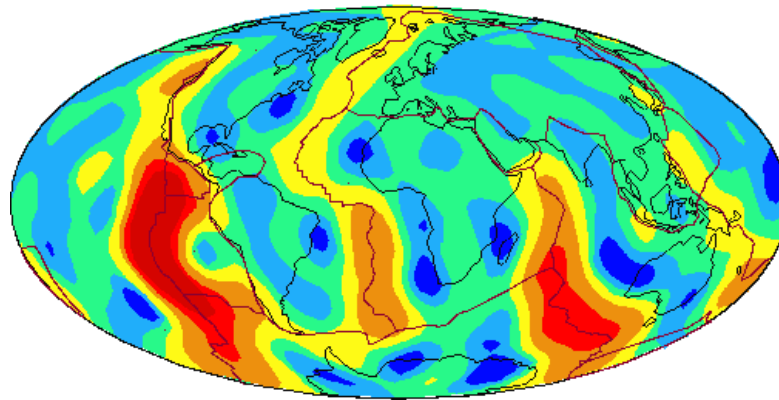
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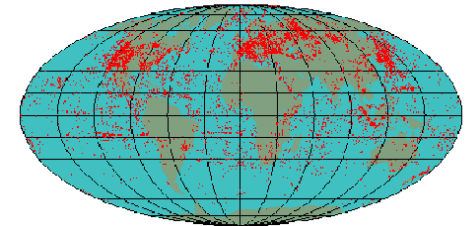


# Et la Terre se refroidit...

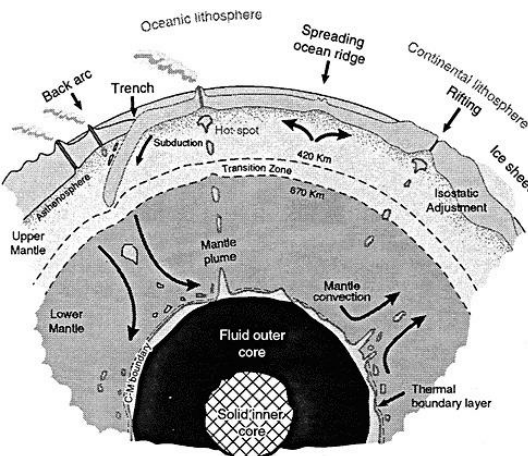
Flux de chaleur



Heat Flow Sites



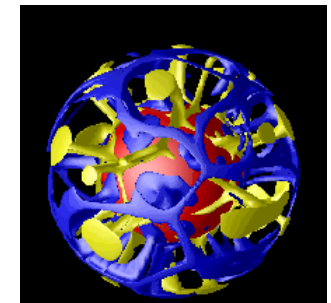
$$40 \text{ TW } (\pm 5) = 5 \text{ TW } (\pm 5) + 25 \text{ TW } (\pm 5) + 10 \text{ TW } (?)$$



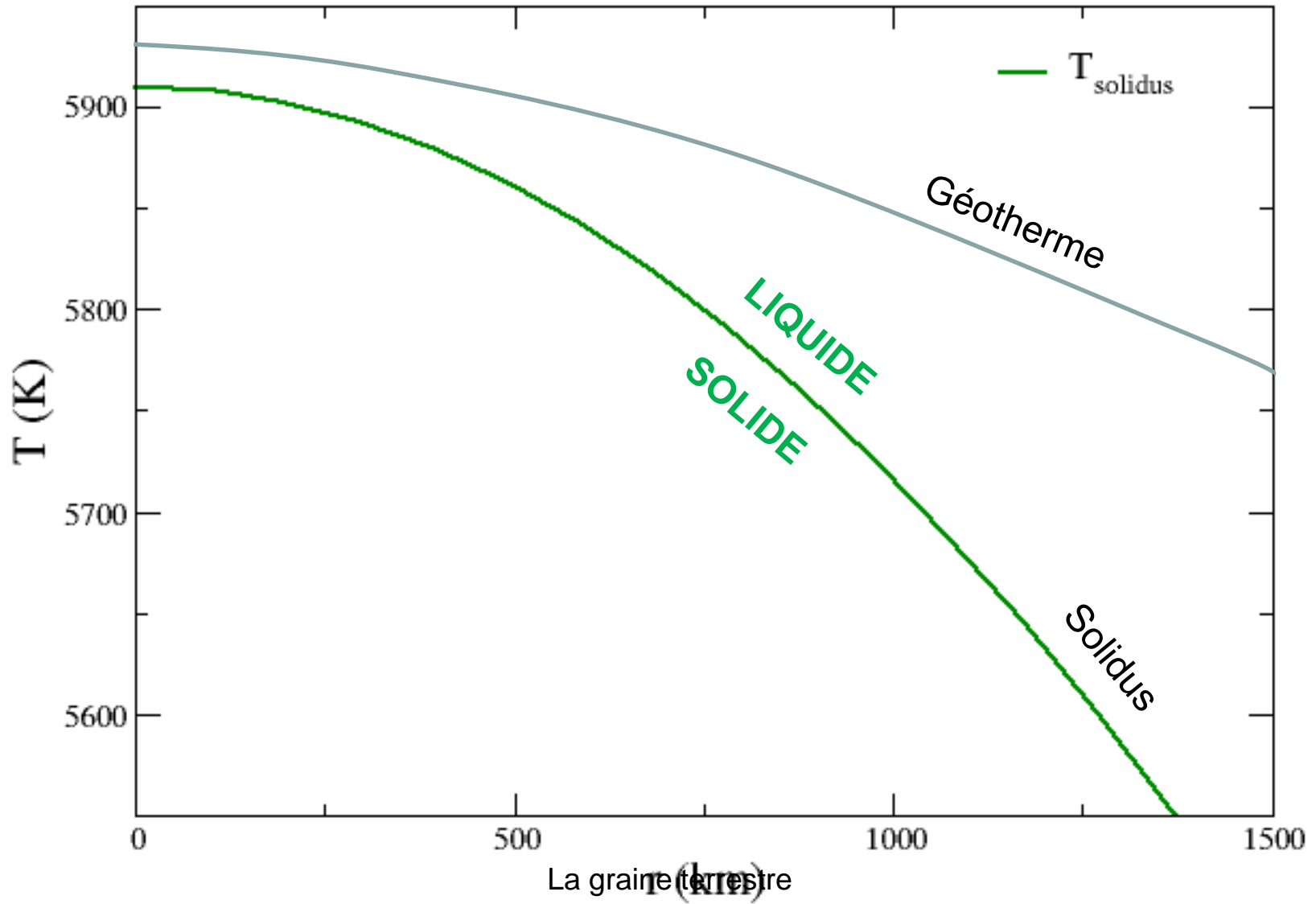
Noyau

Radioactivité

Refroidissement..

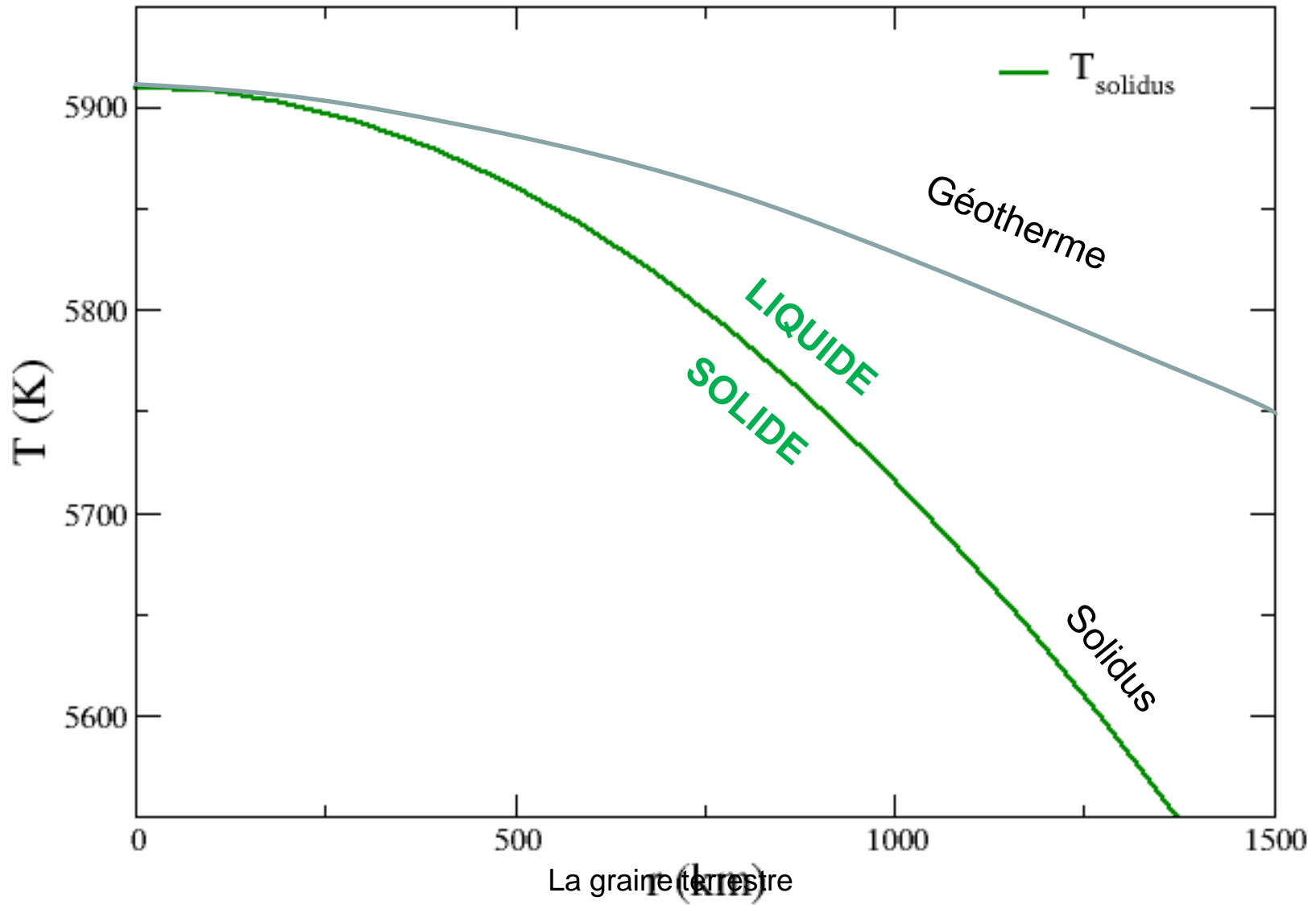


# Evolution thermique de la graine

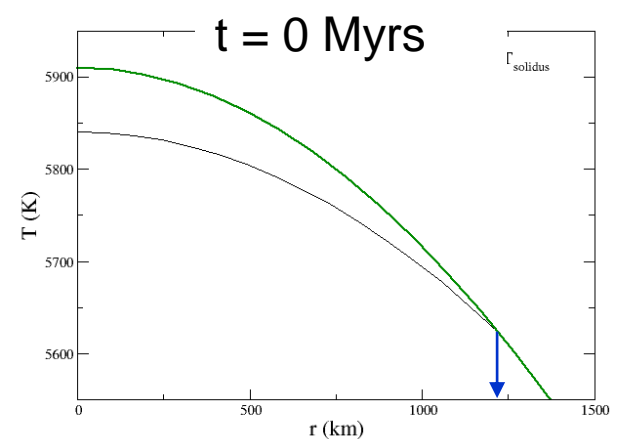
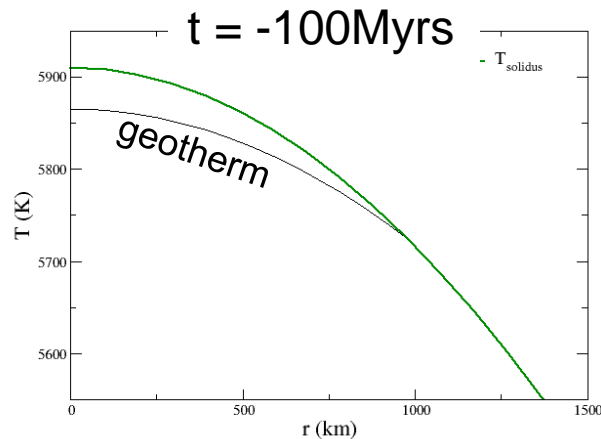
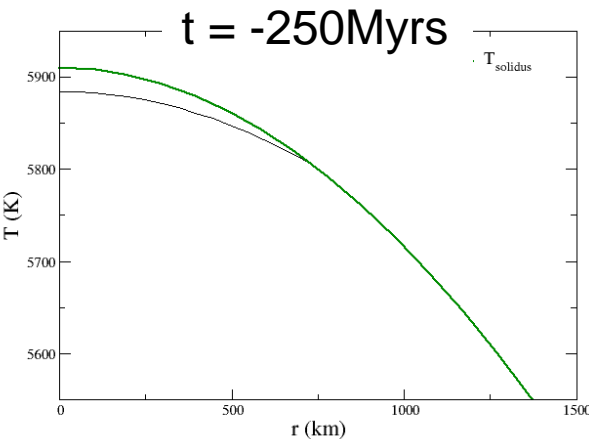
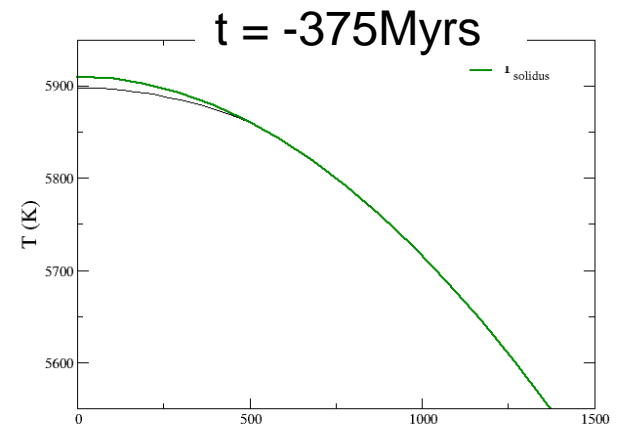
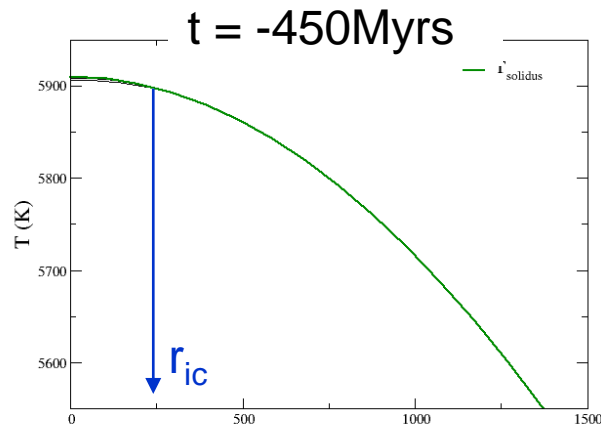
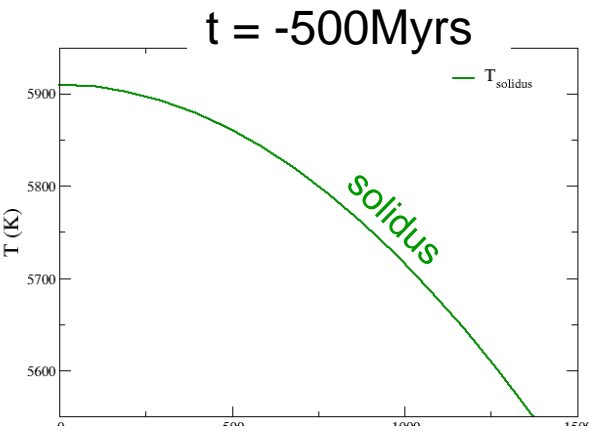


# Evolution thermique de la graine

$$\tau_{ic} = 0.5 \text{ Gy}$$

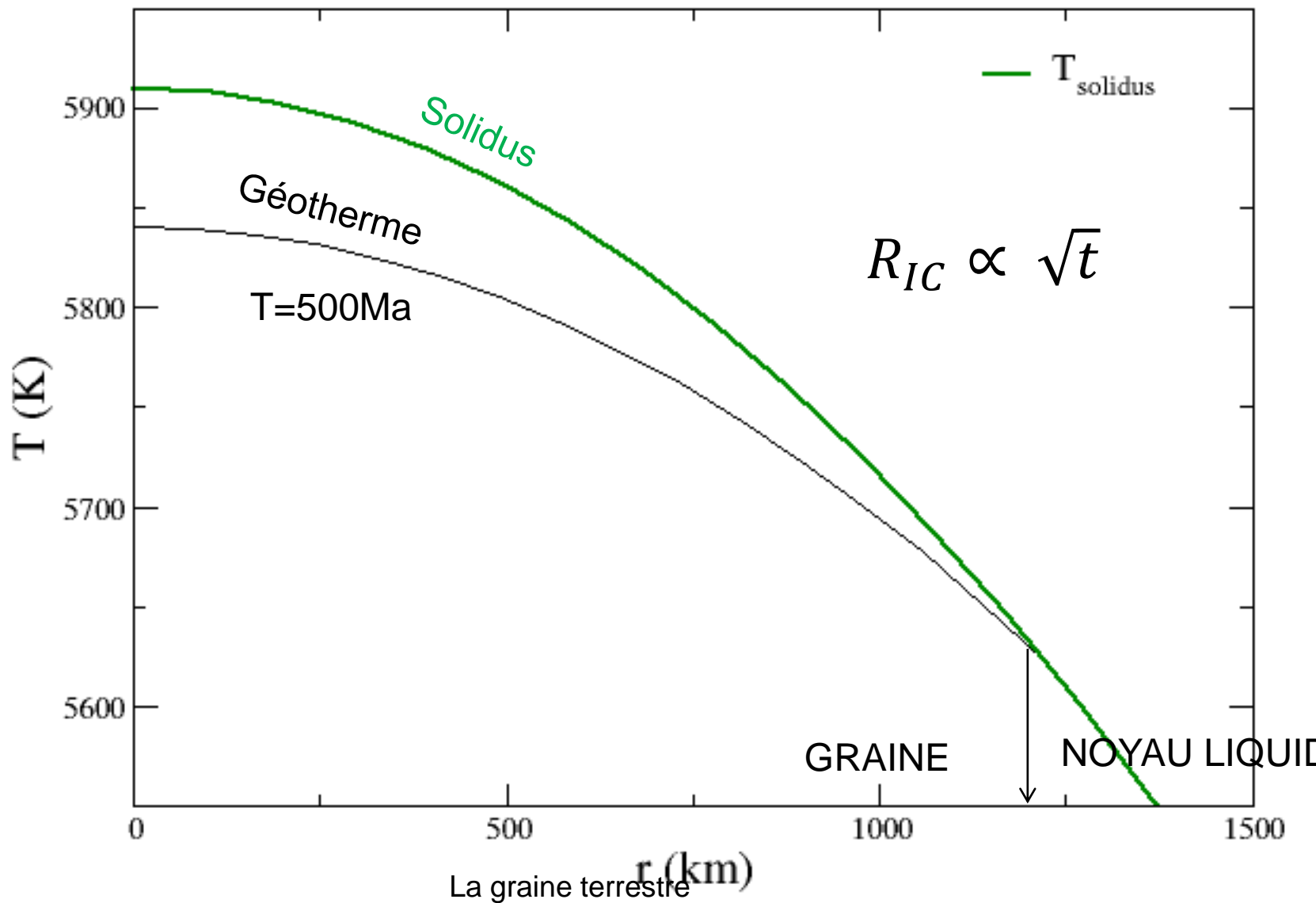


# Et la graine crut...

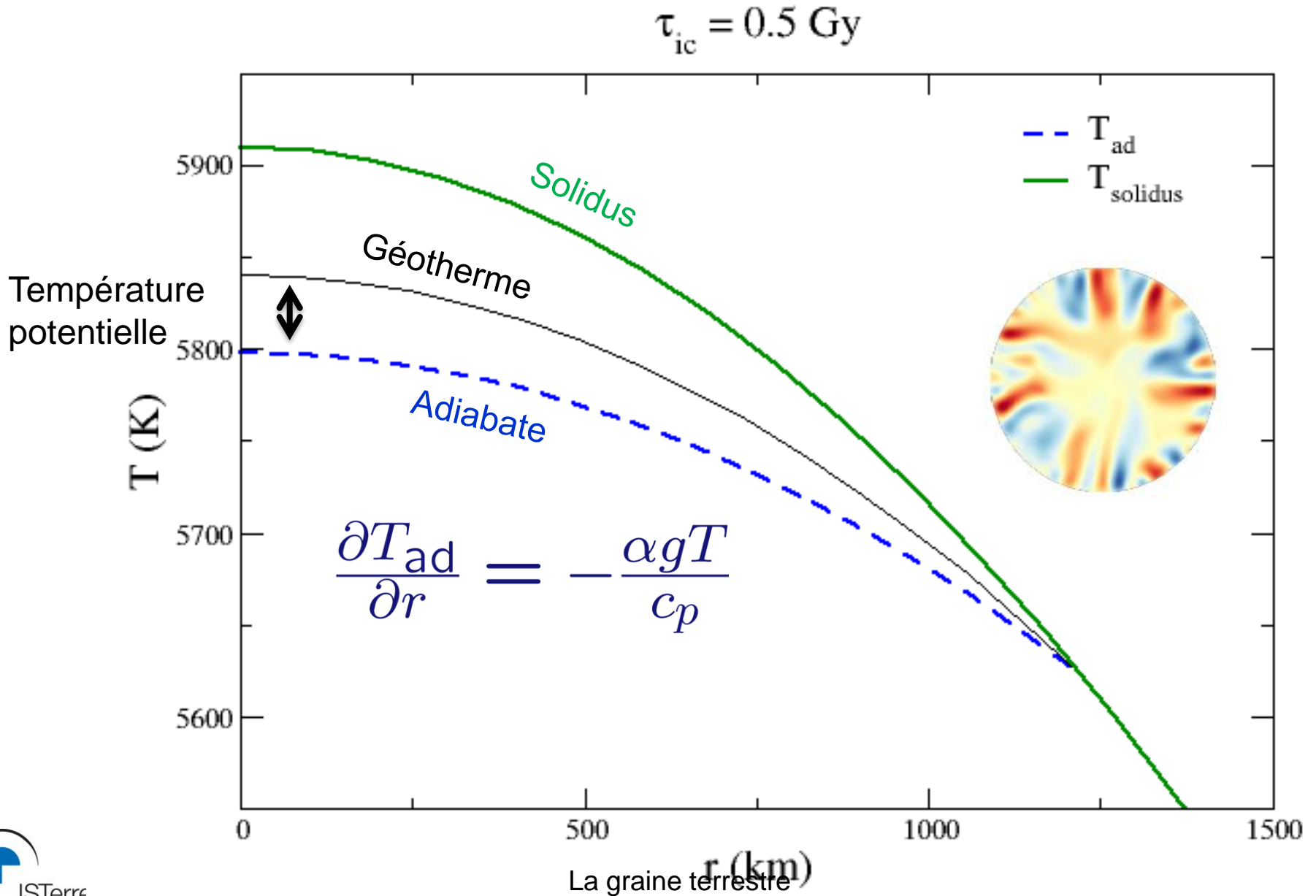


**r<sub>ic</sub> = 1220 km**

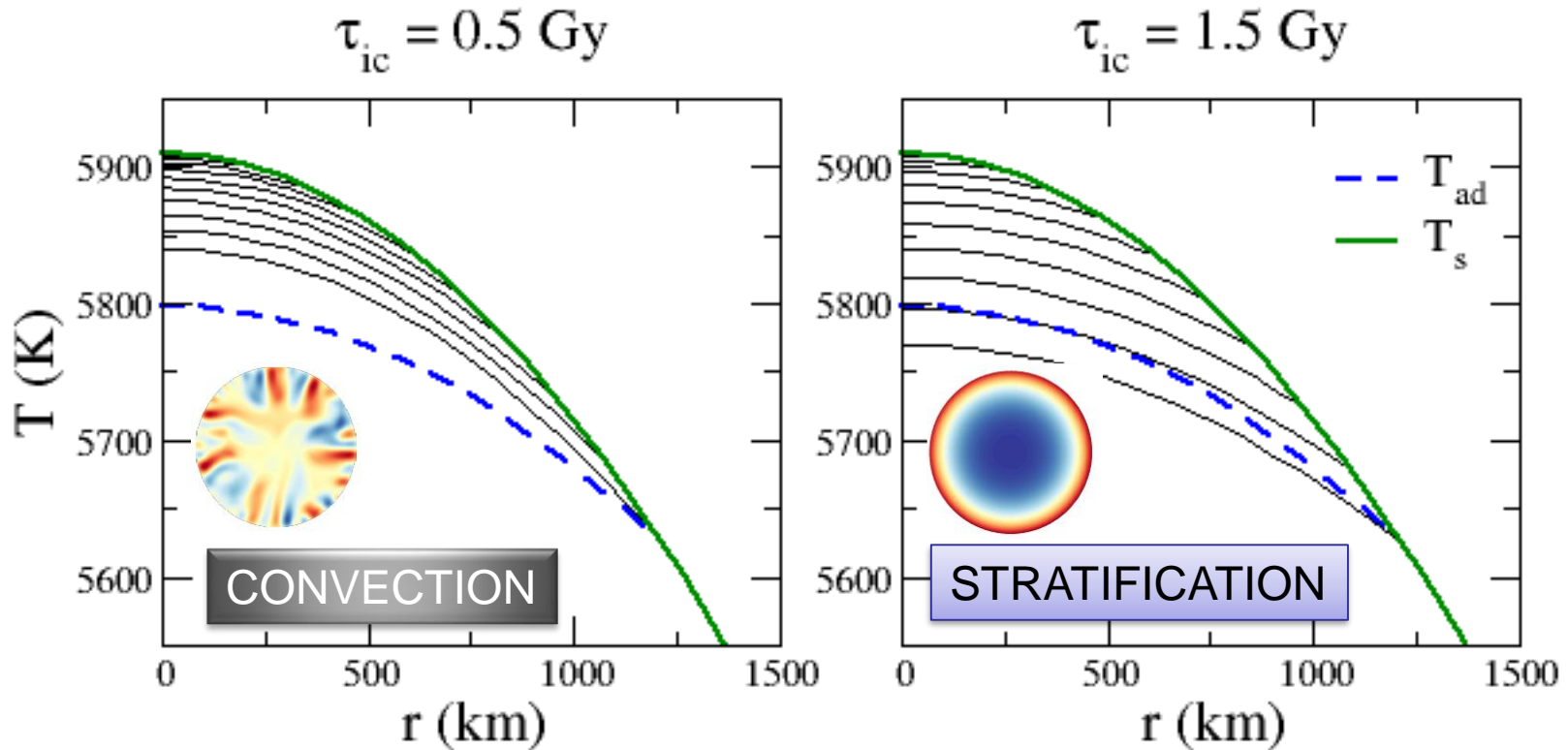
$$\tau_{ic} = 0.5 \text{ Gy}$$



# Equilibre thermodynamique



# L'âge de la graine



Le refroidissement de la graine contrôle son état dynamique

Flux de chaleur à la CMB

Conductivité thermique du Fer

# Conductivité thermique du Fer

Fer liquide			
Référence	Éléments légers	CMB	ICB
Stacey & Anderson (2001)	Si	46	63
Stacey & Loper (2007)	∅	28.3	29.3
de Koker <i>et al.</i> (2012) (Fig. 3)	∅	~130	~210
	Si ou O	90-130	140-190
Pozzo <i>et al.</i> (2013)	∅	159	246
	Fe <sub>82</sub> Si <sub>10</sub> O <sub>8</sub>	107	160
	Fe <sub>79</sub> Si <sub>8</sub> O <sub>13</sub>	99	148
Gomi <i>et al.</i> (2013)	Fe <sub>77.5</sub> Si <sub>22.5</sub>	90.1	148
	Fe <sub>70</sub> C <sub>30</sub>	84.2	136
	Fe <sub>76.8</sub> O <sub>23.2</sub>	125	212
	Fe <sub>80.6</sub> S <sub>19.4</sub>	130	220
Seagle <i>et al.</i> (2013)	∅	67-145	
	Si (9% en masse)	41-60	
Gomi & Hirose (2015)	Fe <sub>67.5</sub> Ni <sub>10</sub> Si <sub>22.5</sub>	83.3-93.0	
Gomi <i>et al.</i> (2016)	Fe <sub>65</sub> Ni <sub>10</sub> Si <sub>25</sub>	87.1	
Konôpková <i>et al.</i> (2016)	∅	33±7	46±9
	Présents	25±7	35±10
Ohta <i>et al.</i> (2016)	Fe <sub>67.5</sub> Ni <sub>10</sub> Si <sub>22.5</sub>	88 <sup>+29</sup> <sub>-13</sub>	
Xu <i>et al.</i> (2018)	Présents	77±10	
Zhang <i>et al.</i> (2020)	~8% en masse et ~5% Ni	70±10	
Fer solide			
Référence	Éléments légers	graine	
Stacey & Anderson (2001)	Si	79	
Gomi & Hirose (2015)	Fe <sub>79</sub> Ni <sub>10</sub> Si <sub>11</sub>	166.9-183.4	
Konôpková <i>et al.</i> (2016)	∅	46±9	
	Présents	35±10	
Xu <i>et al.</i> (2018)	∅	147	

TABLE 3.2 – Estimations de la conductivité du fer en  $\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  dans les conditions du noyau, les études expérimentales sont grisées, elles donnent une estimation de la conductivité thermique par extrapolation des résultats expérimentaux.

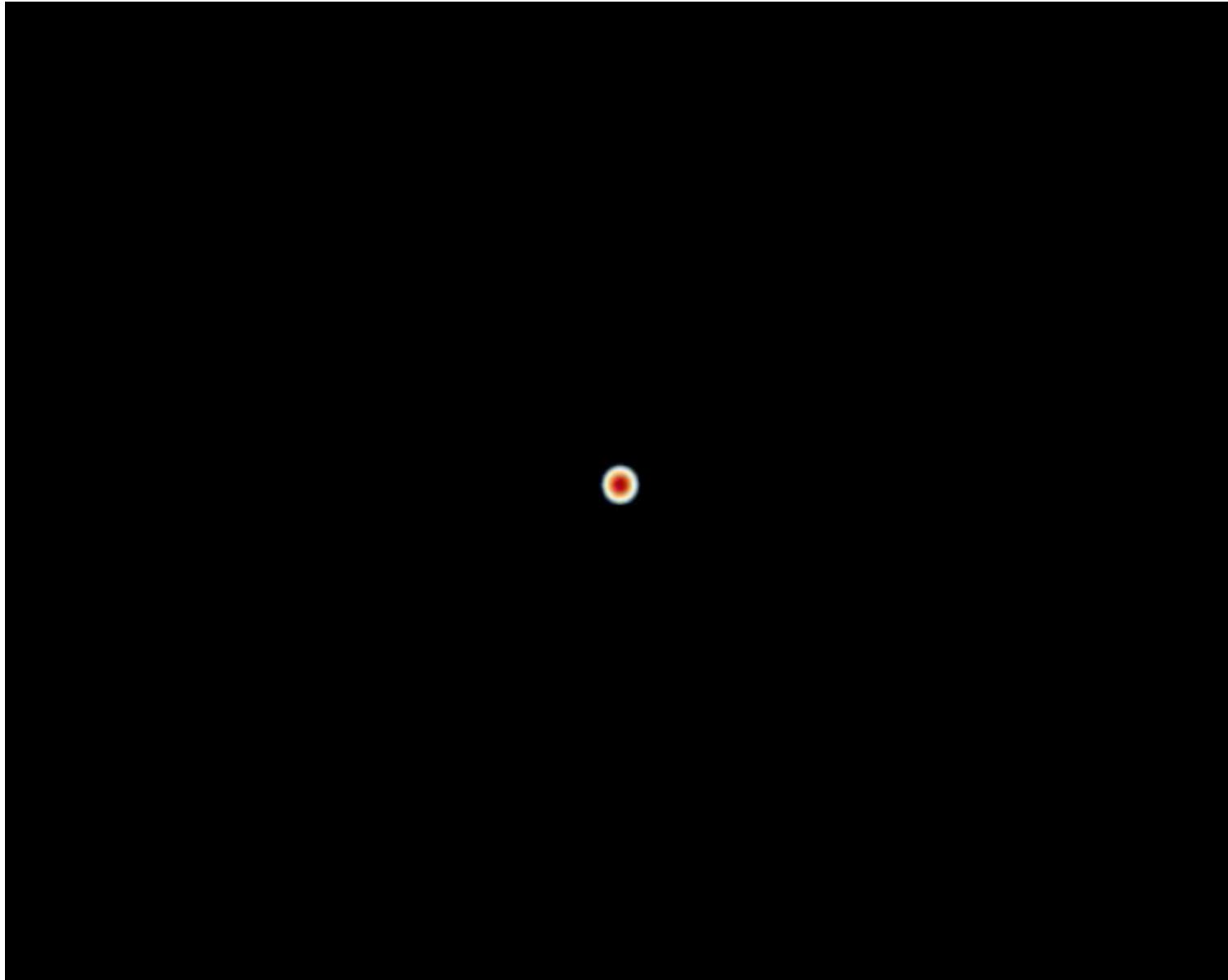
Métayer, 2022)



# Plan

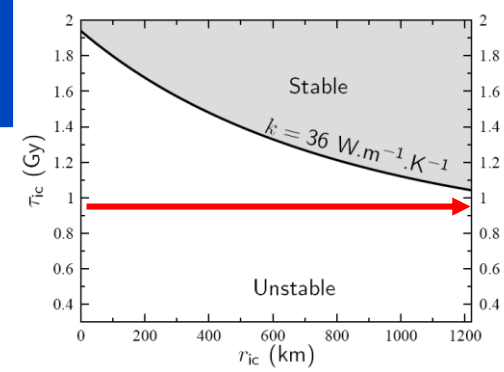
1. Sismologie de la graine
2. Une graine en Fer ?
3. Formation de la graine
4. **Dynamique de la graine**
5. L'anisotropie de la graine

# Convection thermique dans la graine



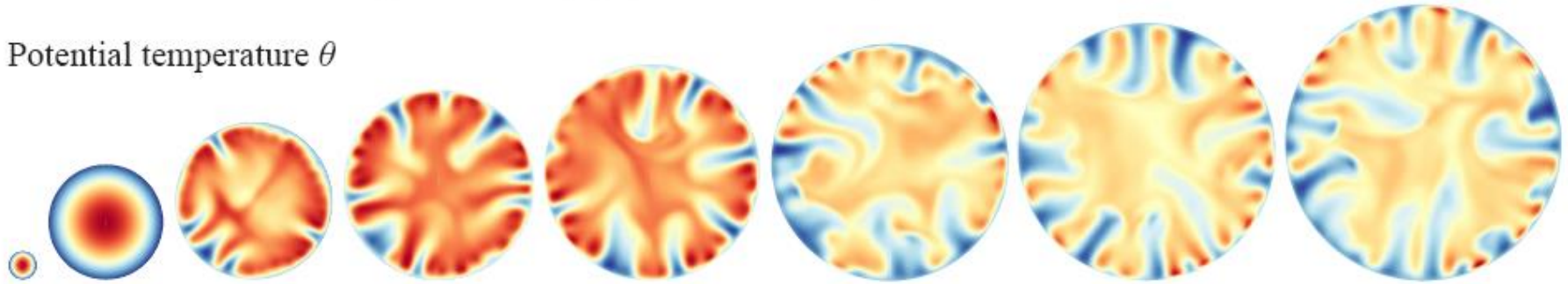
La graine terrestre

# Convection thermique

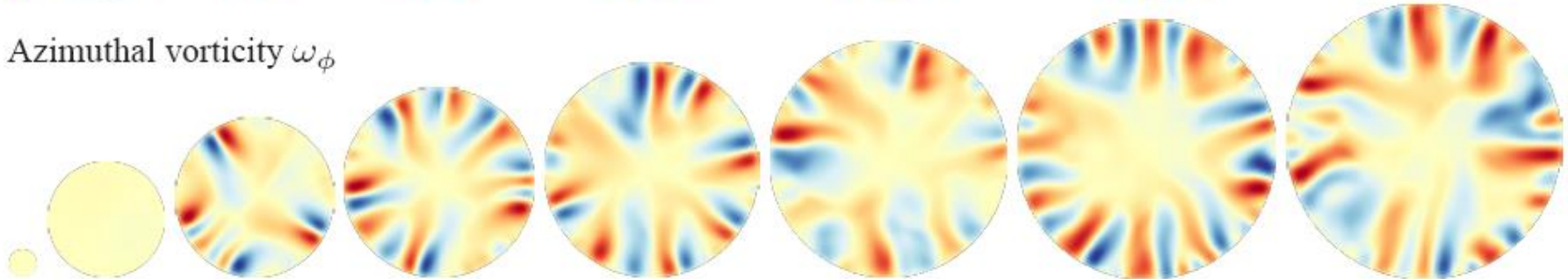


a.  $\tau_{ic} = 0.9 \text{ Gy}$ ,  $\eta = 10^{18} \text{ Pa.s}$ ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$ .

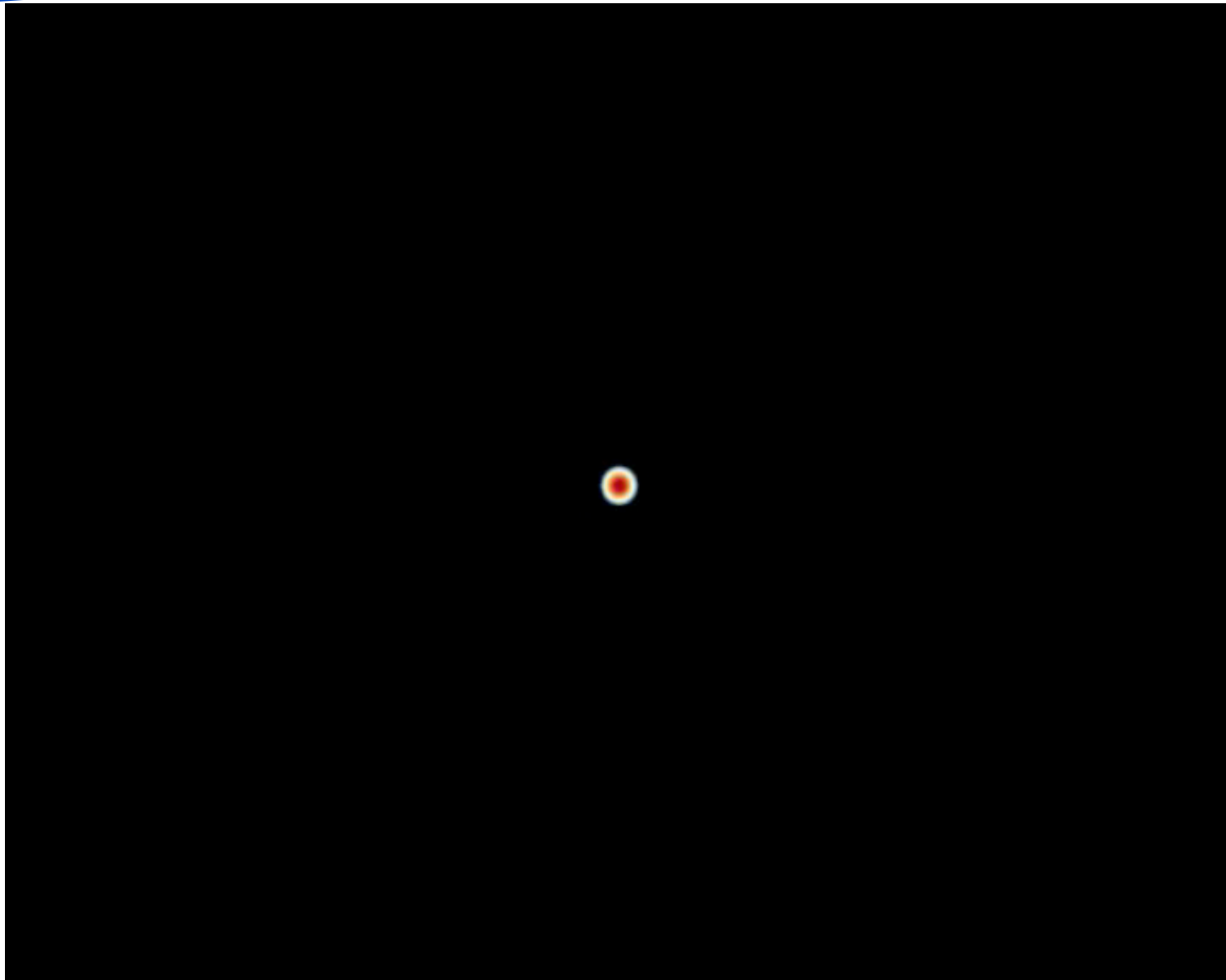
Potential temperature  $\theta$



Azimuthal vorticity  $\omega_\phi$

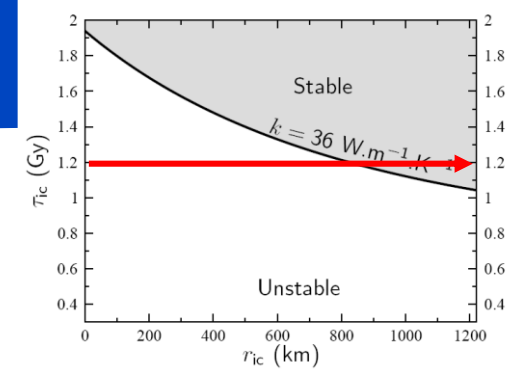


# Convection thermique dans la graine



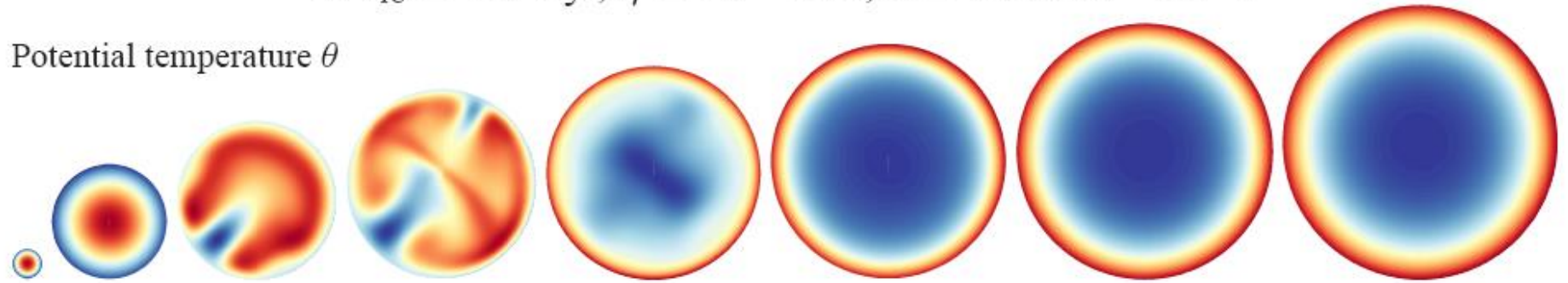
La graine terrestre

# Une fenêtre convective

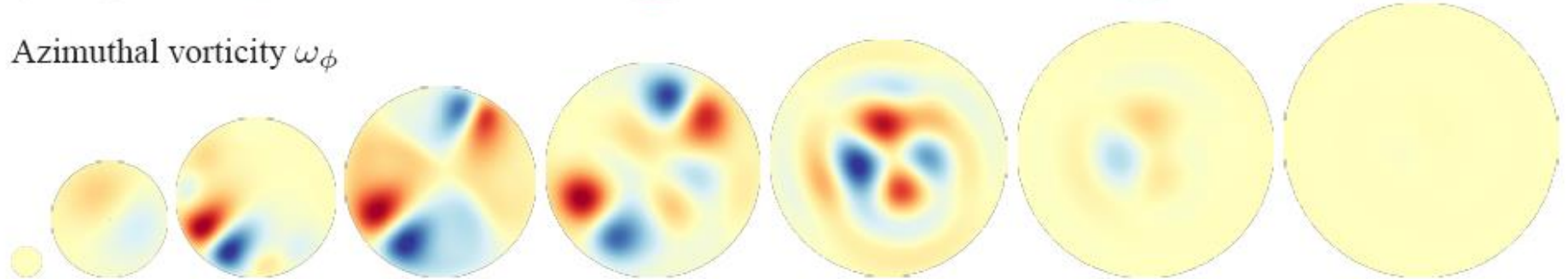


**b.**  $\tau_{ic} = 1.2 \text{ Gy}$ ,  $\eta = 10^{18} \text{ Pa.s}$ ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$ .

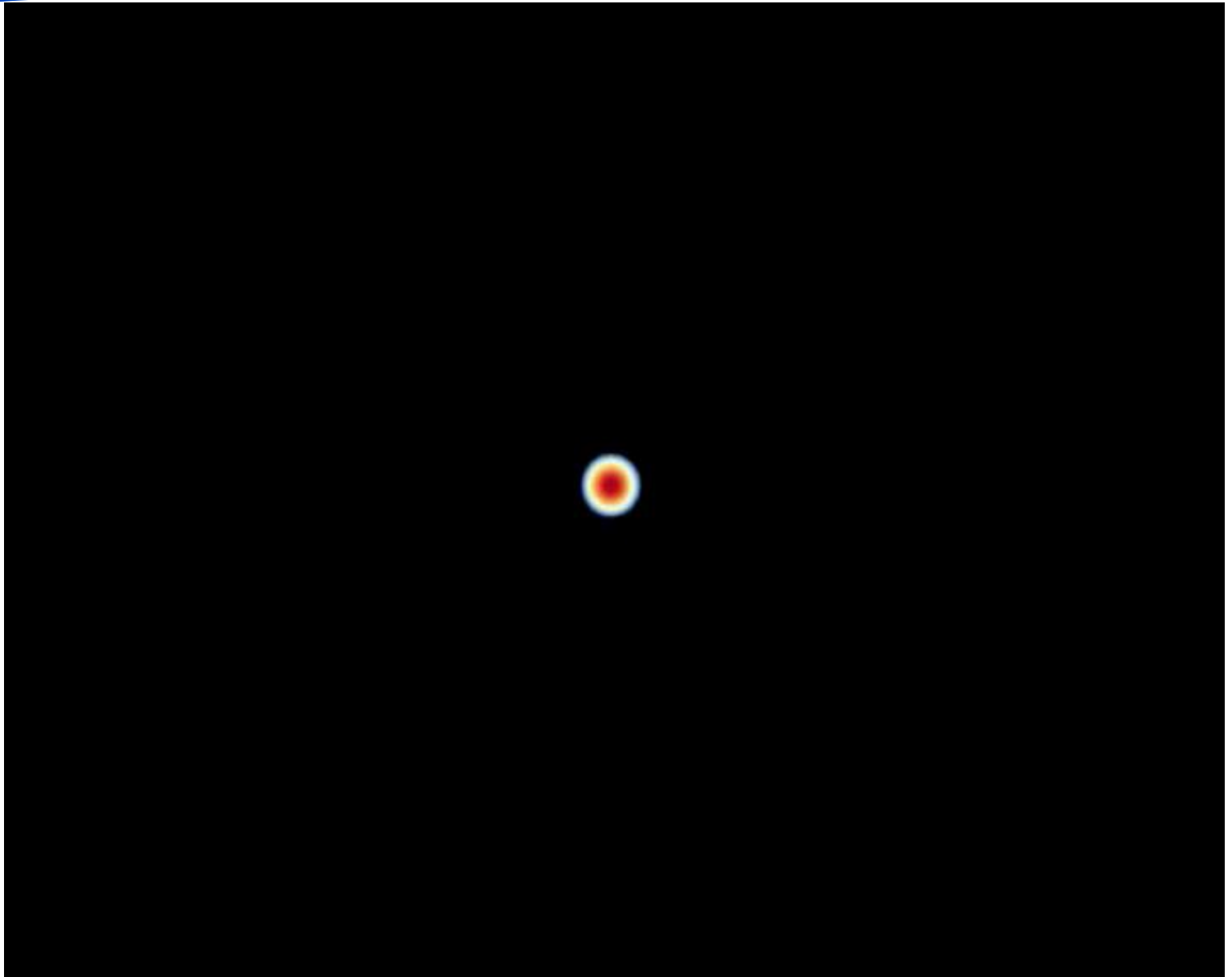
Potential temperature  $\theta$



Azimuthal vorticity  $\omega_\phi$

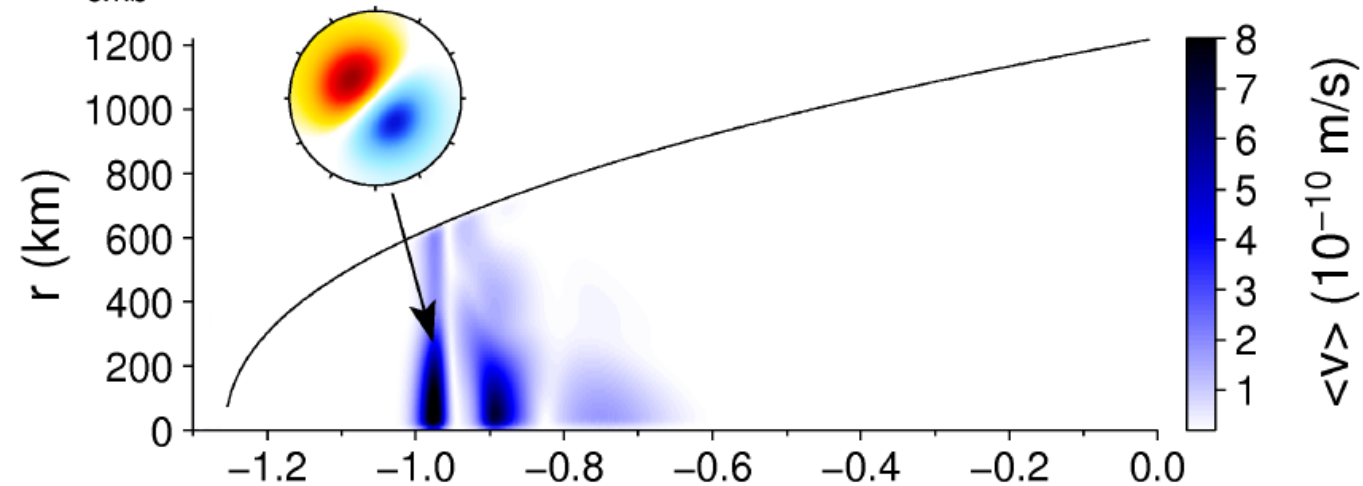


# Épisode convectif dans la graine

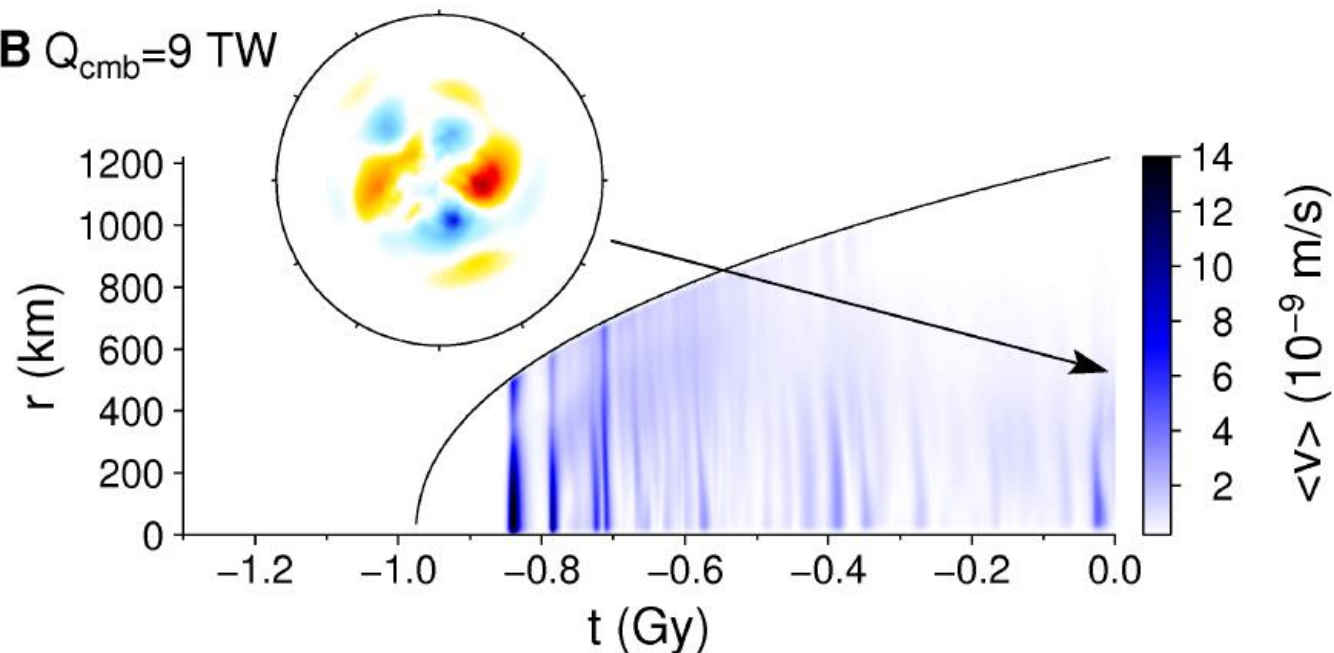


# Un pépin dans la graine!

**A**  $Q_{\text{cmb}}=7$  TW

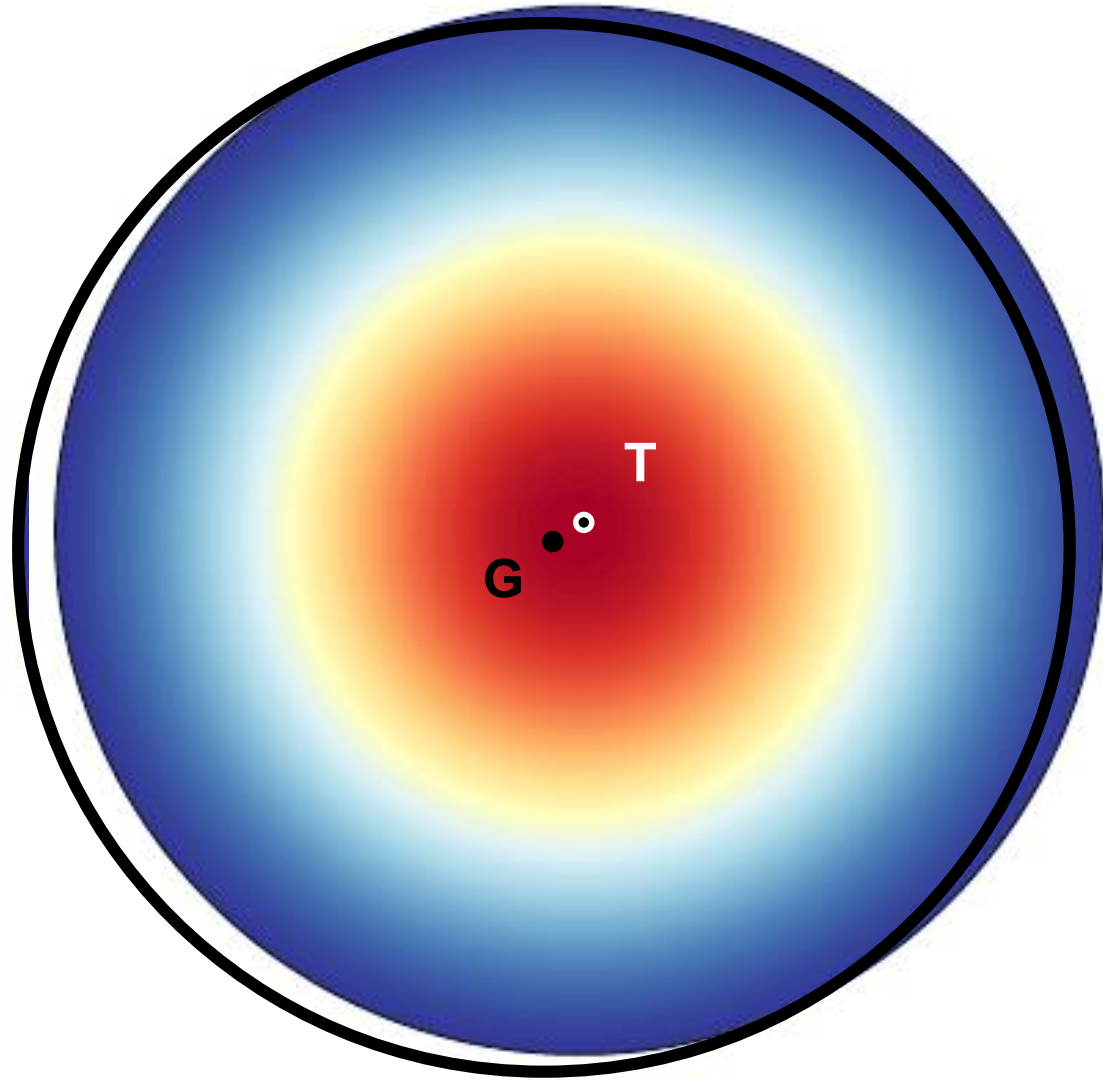


**B**  $Q_{\text{cmb}}=9$  TW



# Un mode convectif particulier

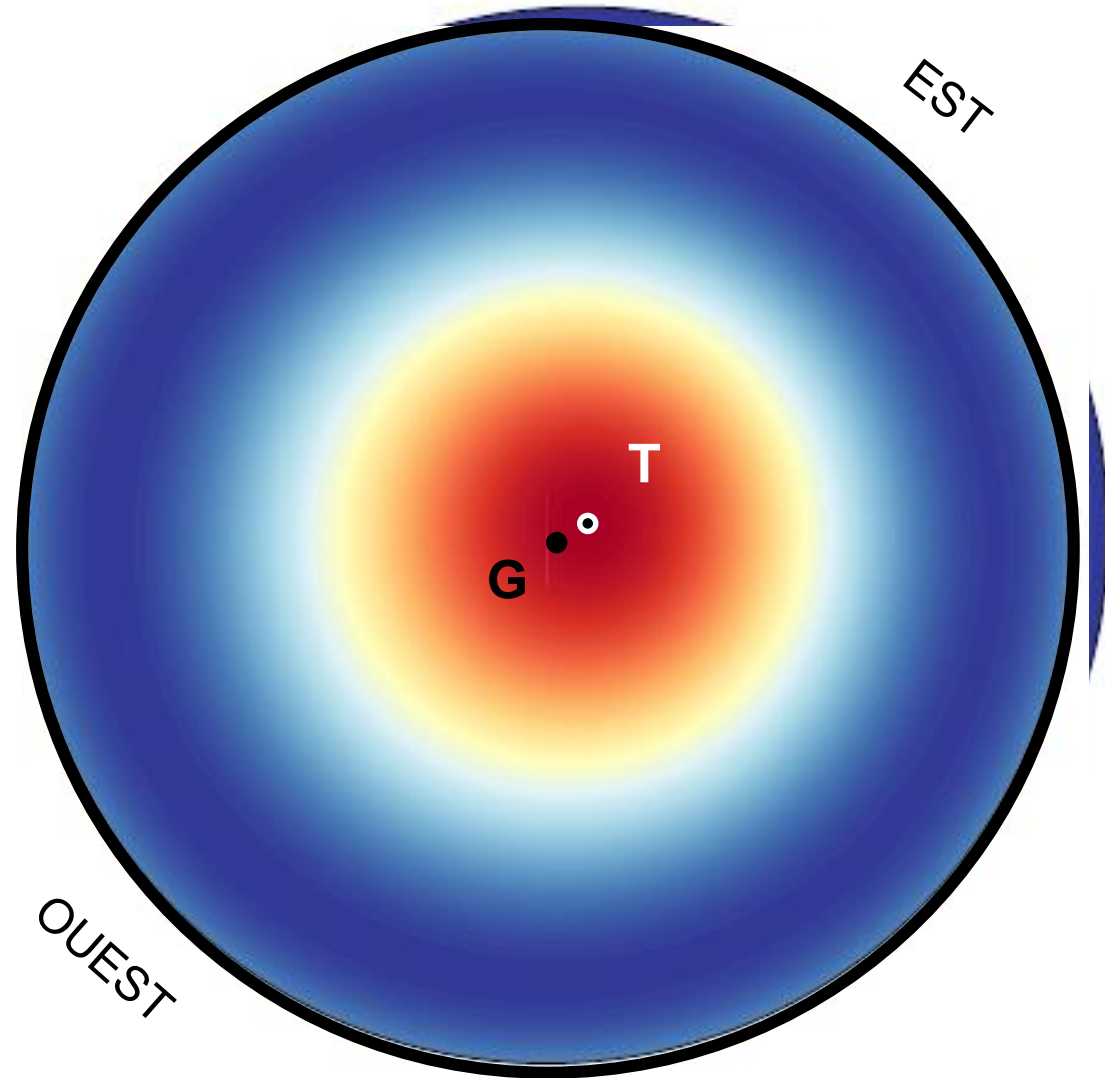
1. Soit une graine rigide ou très visqueuse thermiquement neutre ou sous critique
2. Frontière = solidus (P)
3. Translatez là alors  $G \leftrightarrow T$





# Un mode convectif particulier

1. Soit une graine rigide ou très visqueuse thermiquement neutre ou sous critique
2. Frontière = solidus (P)
3. Translatez là alors  $G \leftrightarrow T$
4. Fondez et cristallisez selon le solidus - rapide
5. Force d'Archimède entretient la translation
6. Variabilité hémisphérique de l'anisotropie



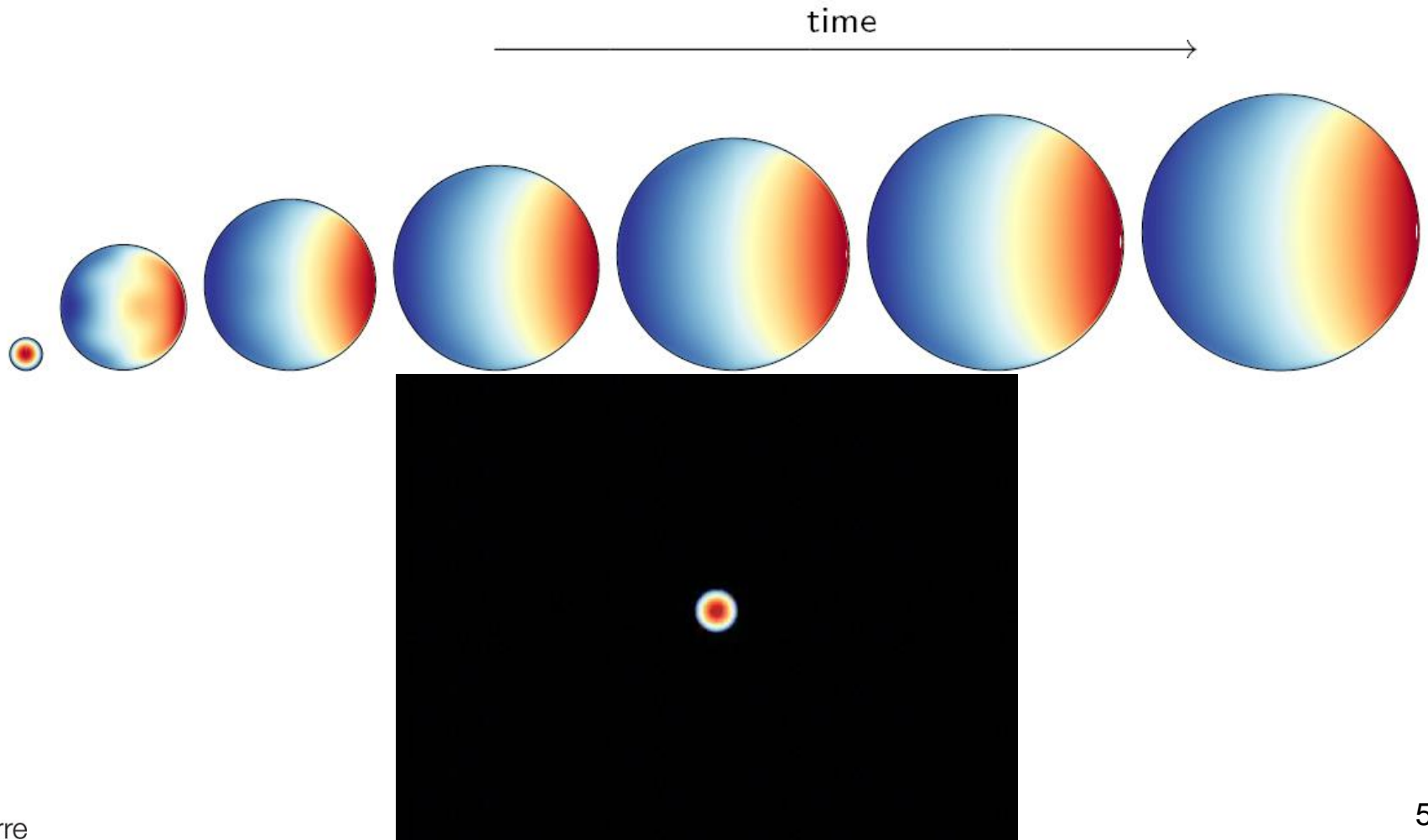
Alboussière et al, Nature, 2010

Monnereau et al, Science, 2010

# translation

$\tau_{ic} = 0.9 \text{ Gy}$  ,  $k = 36 \text{ W.m}^{-1}.\text{K}^{-1}$  , potential temperature :

►  $\eta = 10^{19} \text{ Pa.s}$  , translation regime :



# Convection et translation

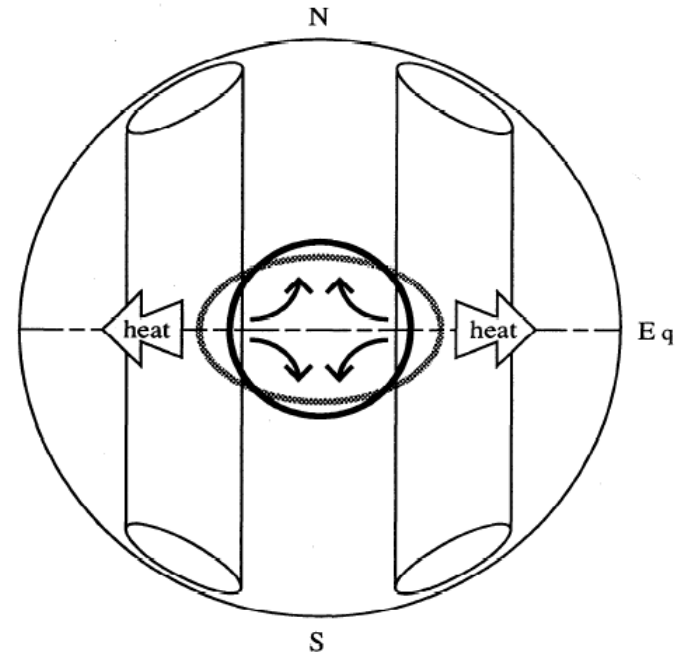
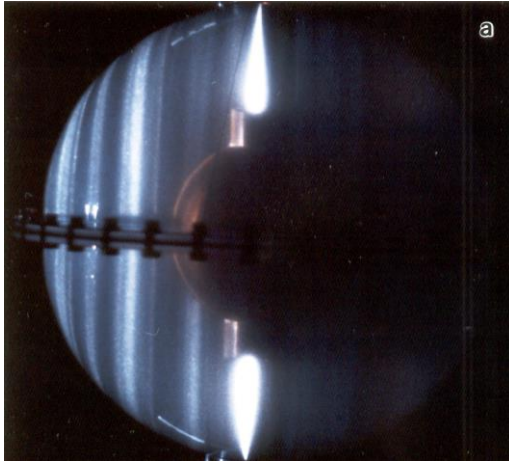
Pour des viscosités modérées



# Plan

1. Sismologie de la graine
2. Une graine en Fer ?
3. Formation de la graine
4. Dynamique de la graine
5. **L'anisotropie de la graine**

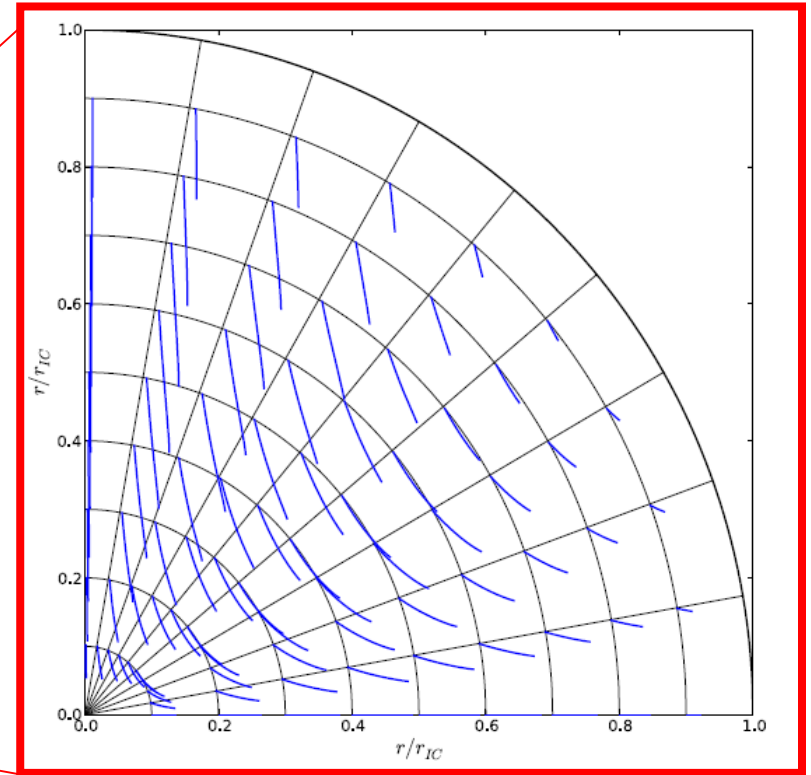
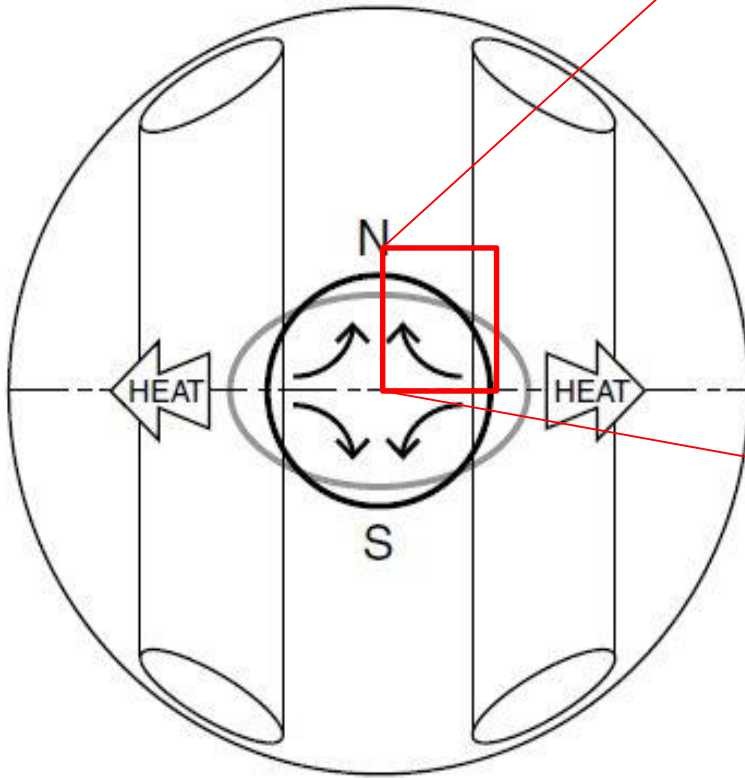
# Croissance équatoriale préférentielle



Yoshida et al, 1996

La graine croîtrait deux fois plus vite dans sa zone équatoriale que dans sa zone polaire  
Relaxation visqueuse quadripolaire

# Equatorial preferential growth



Trajectories of solid particles  
(1/4 of a meridional plan)

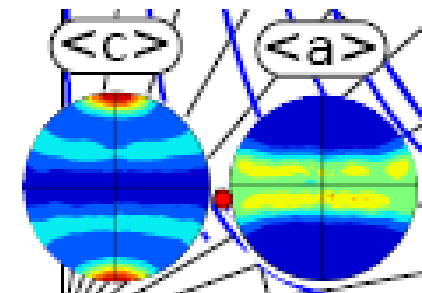
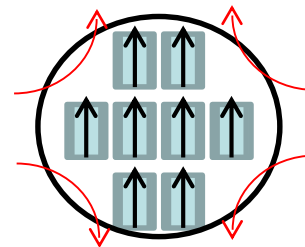
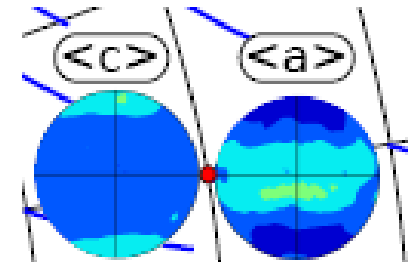
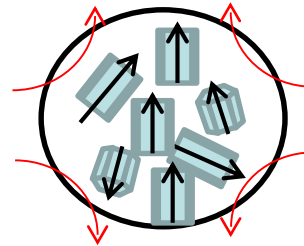
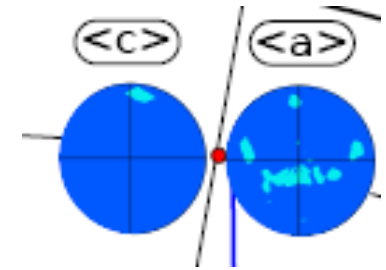
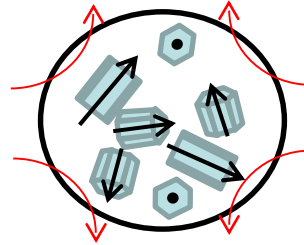
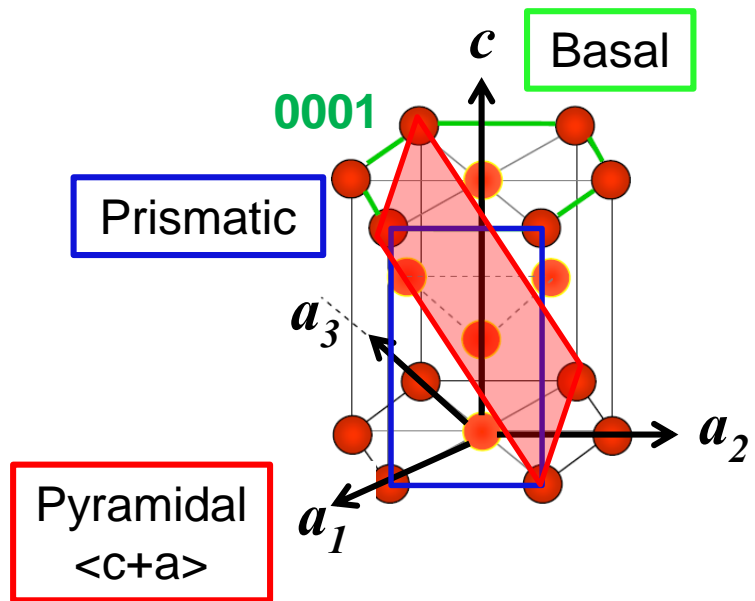
*Yoshida et al. [1996]*

# Anisotropie de texture

Déformation plastique  
ou recristallisation



# Visco Plastic Self Consistent model





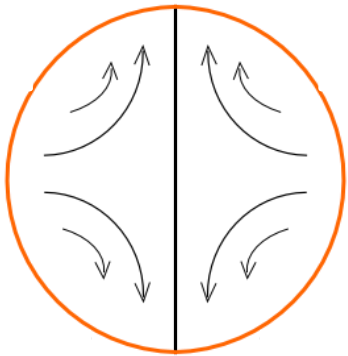
# Direct model of an elastic inner core

Geodynamical model  
+  
Crystalline model (basal)

Textured IC  
VPSC

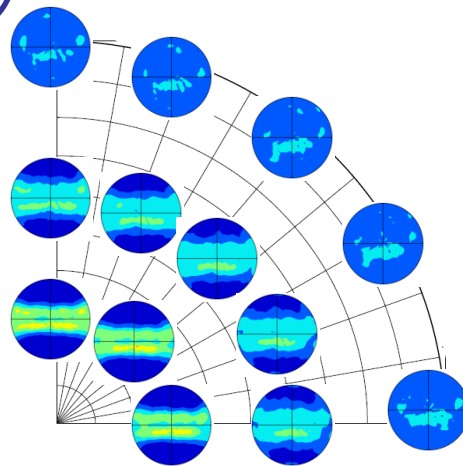
Elastic IC

Seismic response?



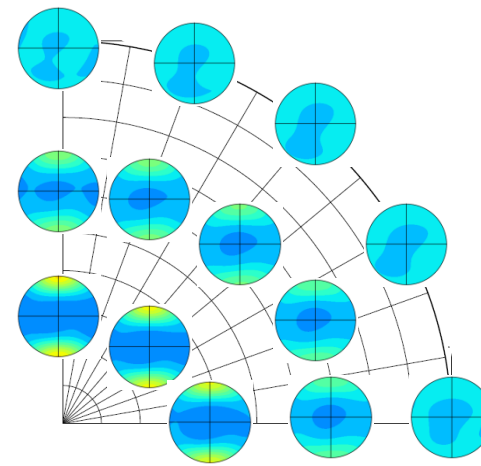
*Yoshida et al [1996]*

*Merkel et al [2006]*



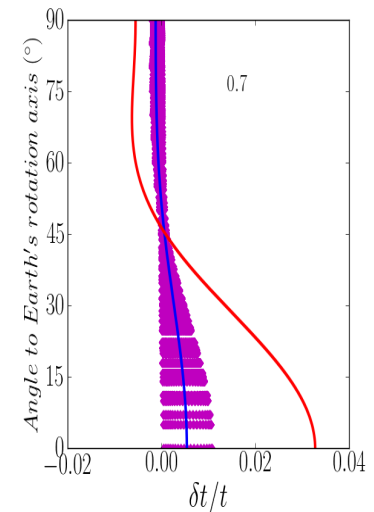
0 4  
Texture c-axis

*Lebenshon et al [1993]*



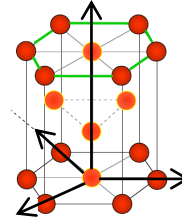
10.6 11.1  
 $V_p$  (km.s<sup>-1</sup>)

*Vocadlo et al [2009]*



*Lincot et al [2014]*

# Global anisotropy for hcp Fe



## Seismic residuals

$$\frac{\delta t}{t} = \frac{s_{ray} - s_0}{s_0}$$

Where  $s_0$  = average slowness in IC

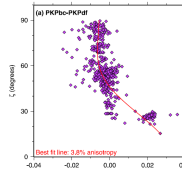
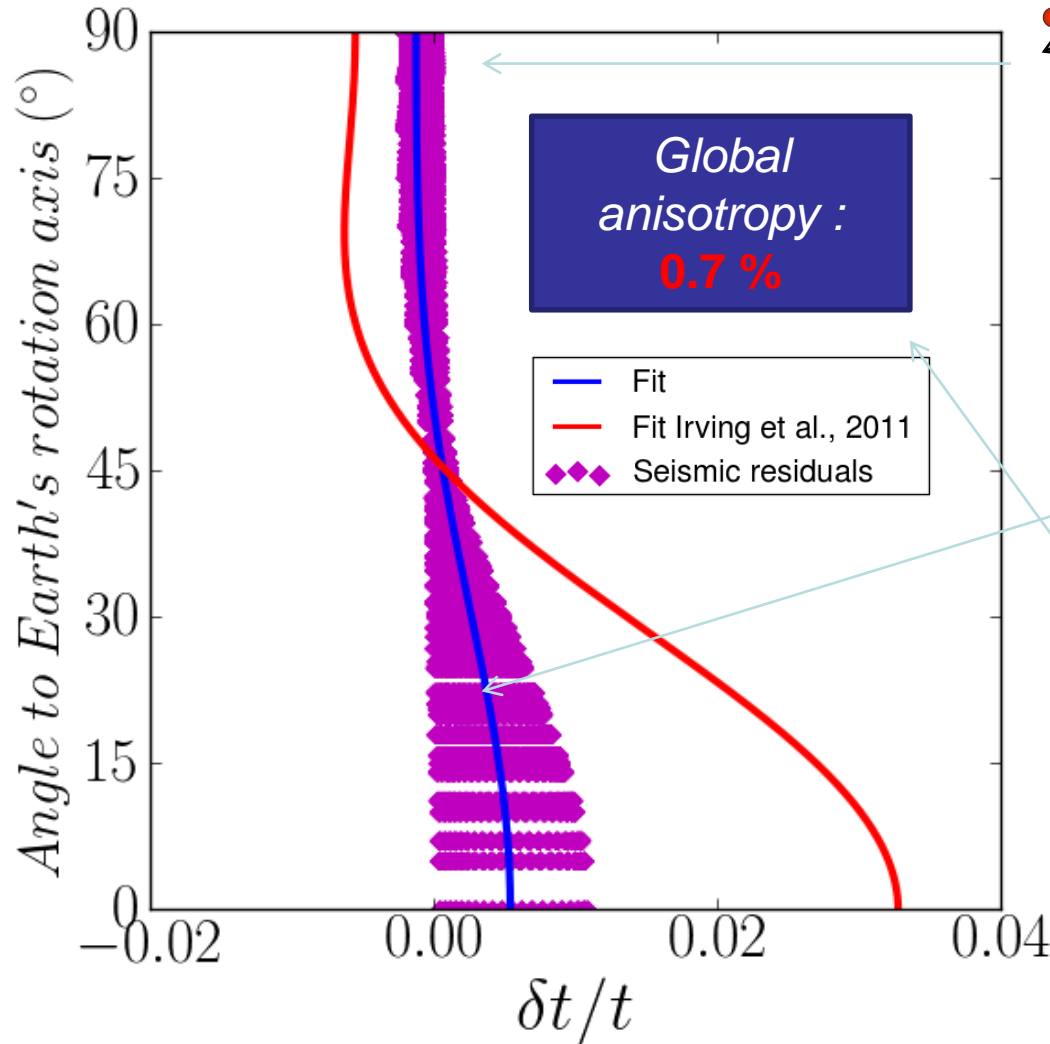
## Fitting residuals (hyp : homogeneous IC)

$$\frac{\delta t}{t} = a + b \cos^2 \zeta + c \cos^4 \zeta$$

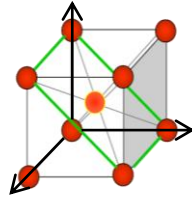
Estimate of  
N-S anisotropy  
( $b + c$ )

→ **global anisotropy**

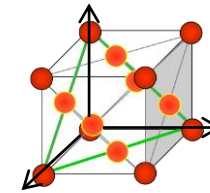
Vocadlo et al. [2009]



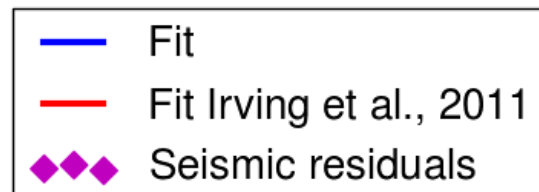
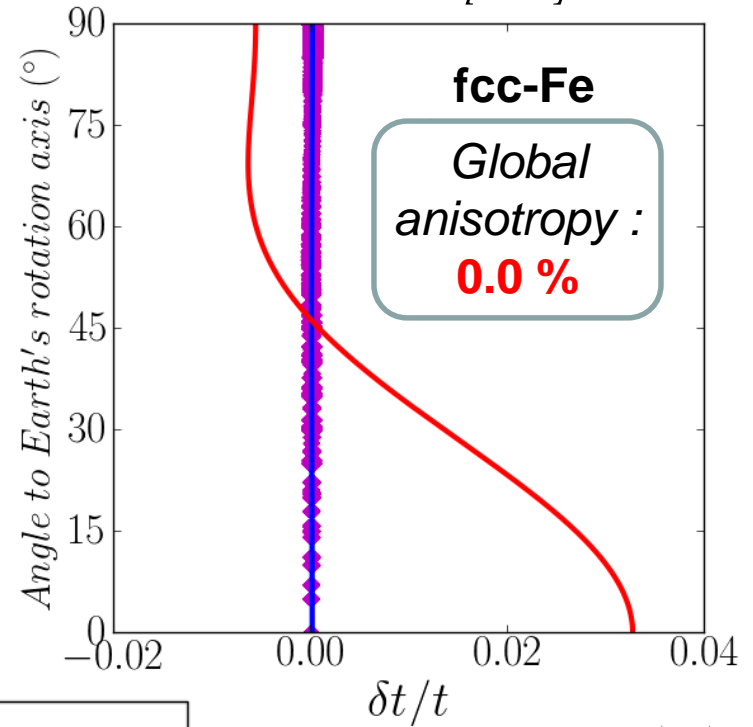
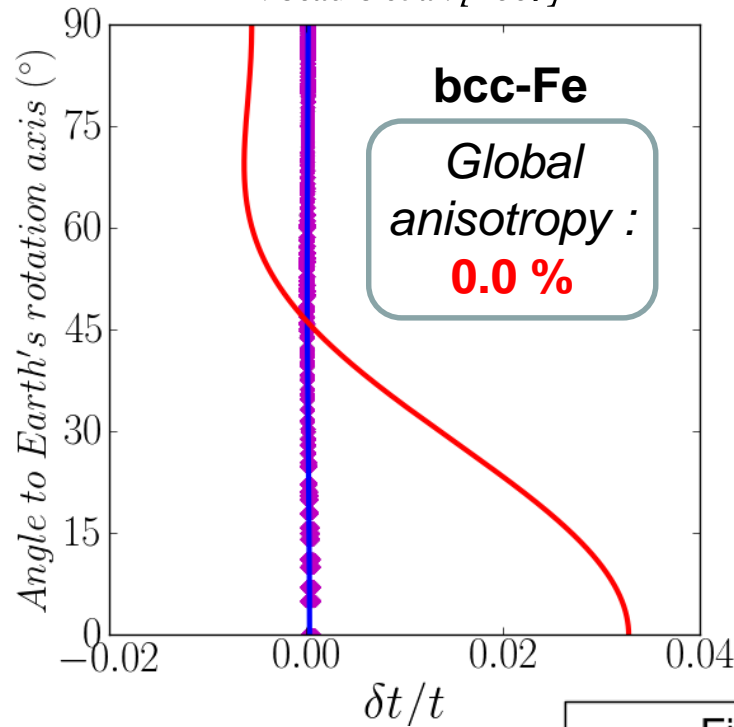
# Seismic response to an IC made of cubic Fe



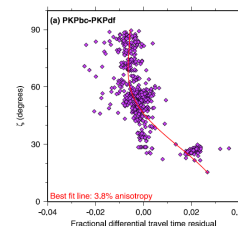
Vocadlo et al. [2007]



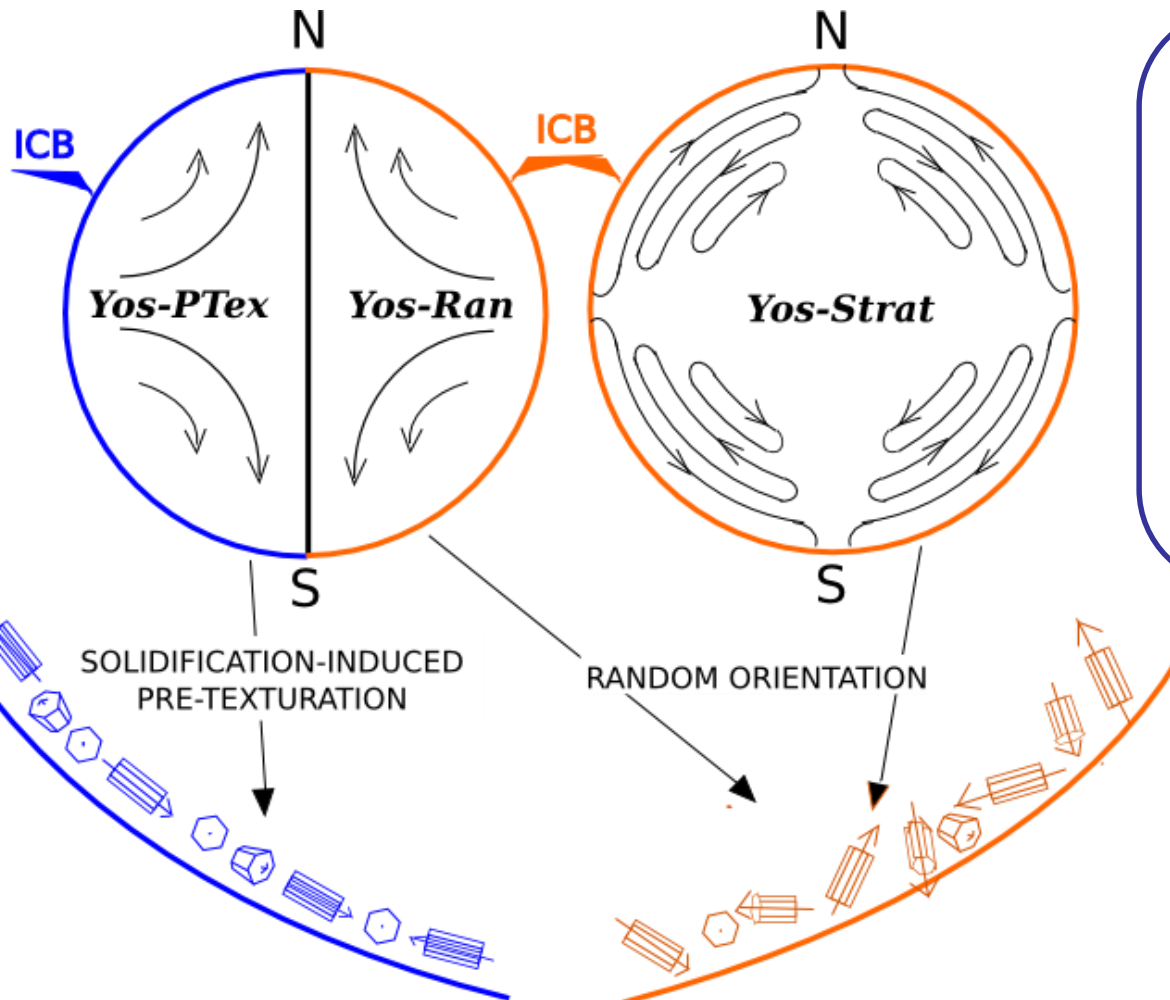
Vocadlo et al. [2008]



La graine terrestre



# How to increase the texturing ?



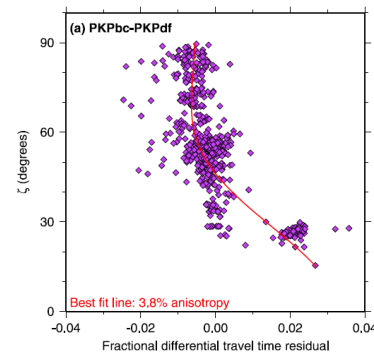
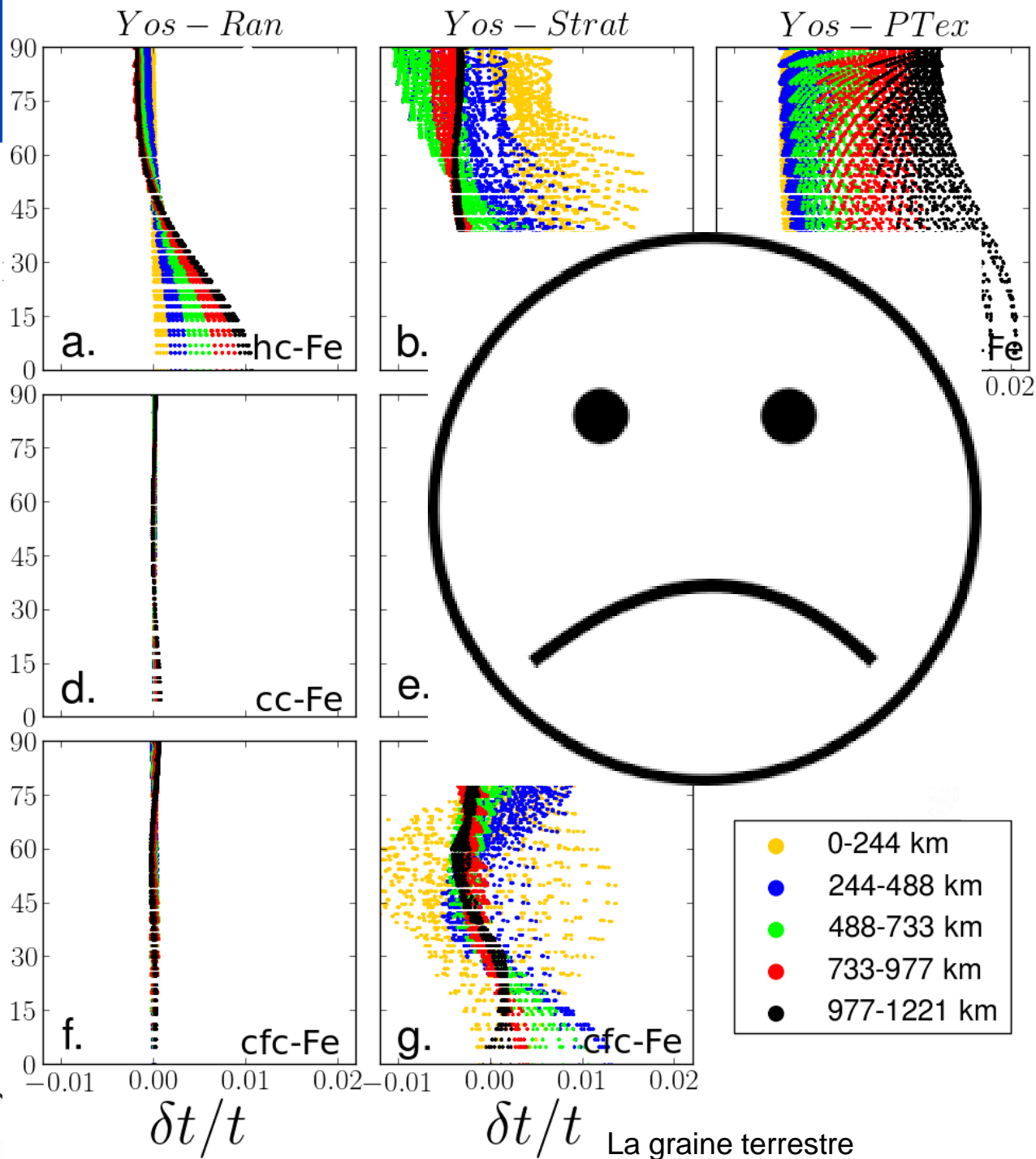
Other geodynamical processes tested :

- Solidification texture CPO for Fe (developping extra texturing at ICB)
- Stratification (up to 300% deformation)

*Deguen et al. [2009]*

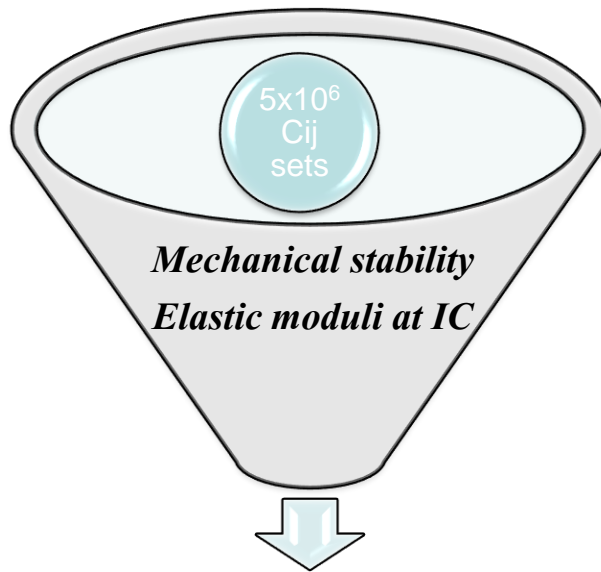
Orientation of *hcp* crystals from crystallisation

Anqle to Earth's rotation axis ( $^{\circ}$ )



# Random draw of $C_{ij}$ values (Monte Carlo)

- No «a priori» on elasticity



3000 synthetic models

*Note : global anisotropy depends on shape of single crystal anisotropy, not on individual  $C_{ij}$  values.*

## *Mechanical stability*

**hcp**

$$C_{11} - C_{12} > 0$$
$$C_{11} + C_{12} + C_{33} > 0$$
$$(C_{11} + C_{12})C_{33} - 2C_{13}^2 > 0$$
$$C_{44} > 0$$

**bcc**

$$C_{11} - C_{12} > 0$$
$$C_{11} + 2C_{12} > 0$$
$$C_{44} > 0$$

## *Elastic moduli at IC conditions*

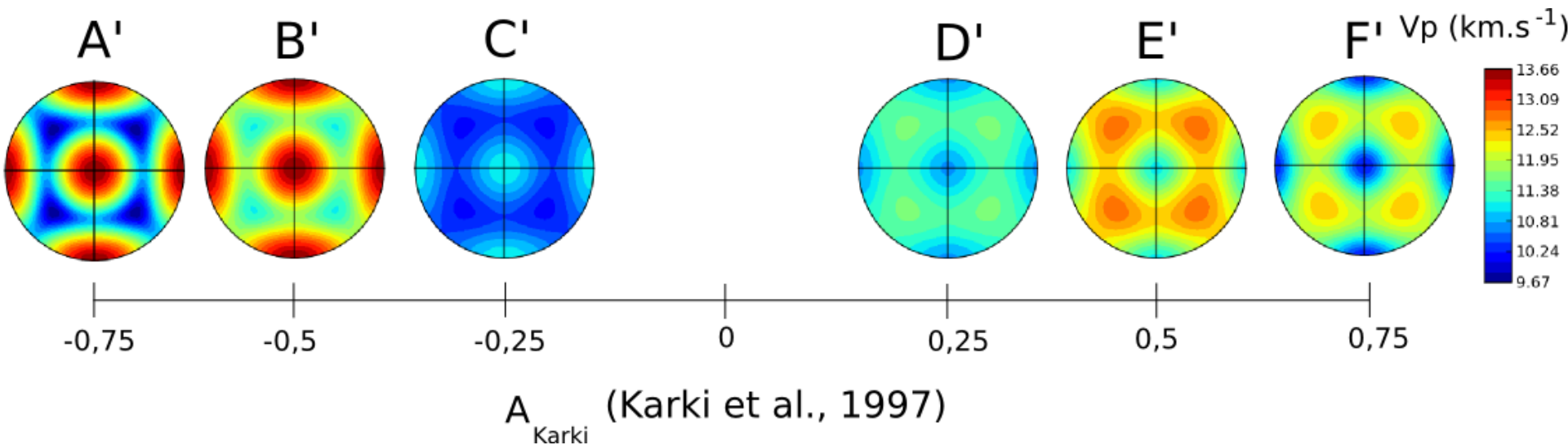
$$K = 1384.4 \text{ GPa} \pm 15\%$$

$$G = 166.4 \text{ GPa} \pm 15\%$$

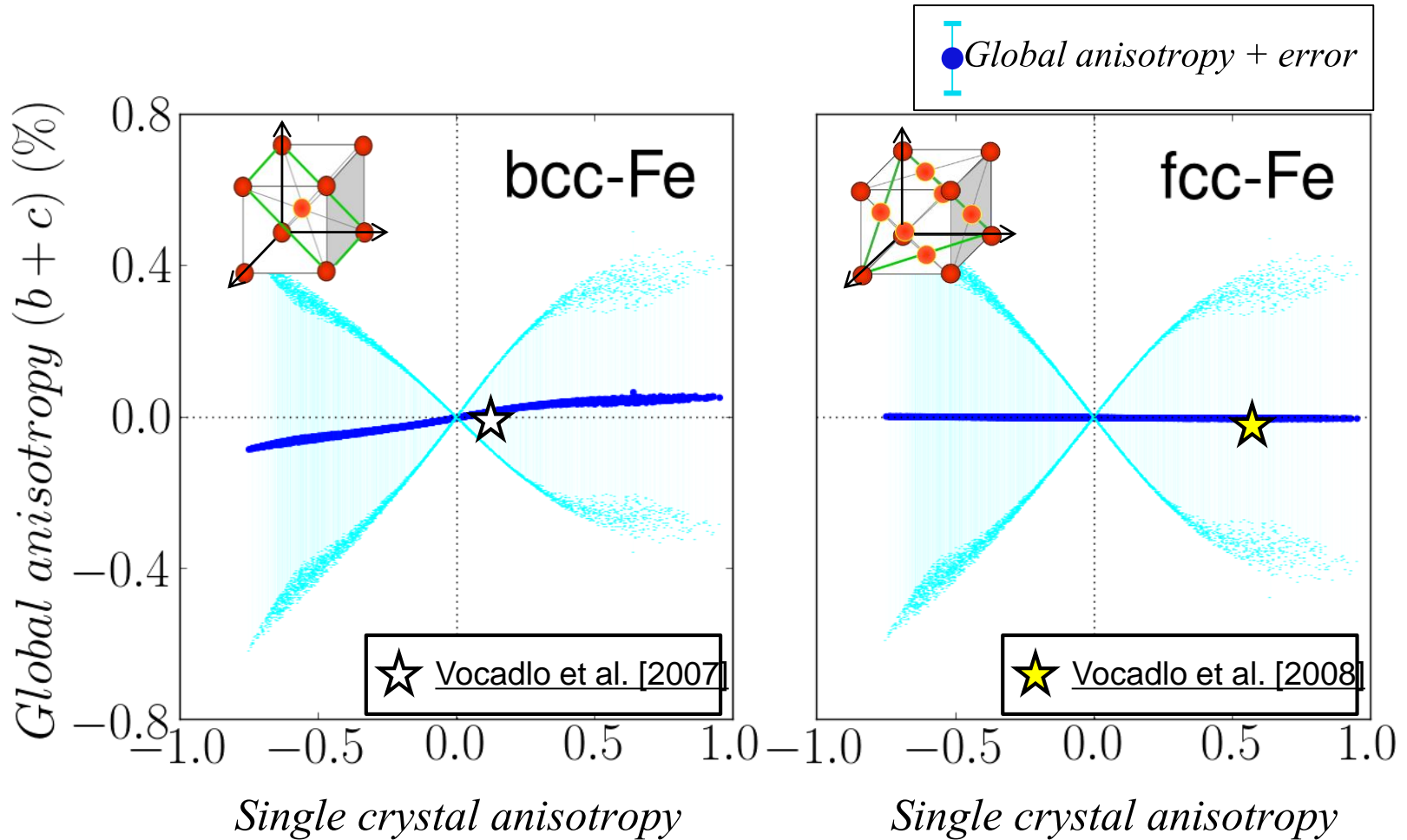
# K dimensionless parameter of crystallographic anisotropy

The Karki parameter

$$K = \frac{2C_{44} + C_{12}}{C_{11}} - 1$$



# Global anisotropy for a cubic-Fe inner core



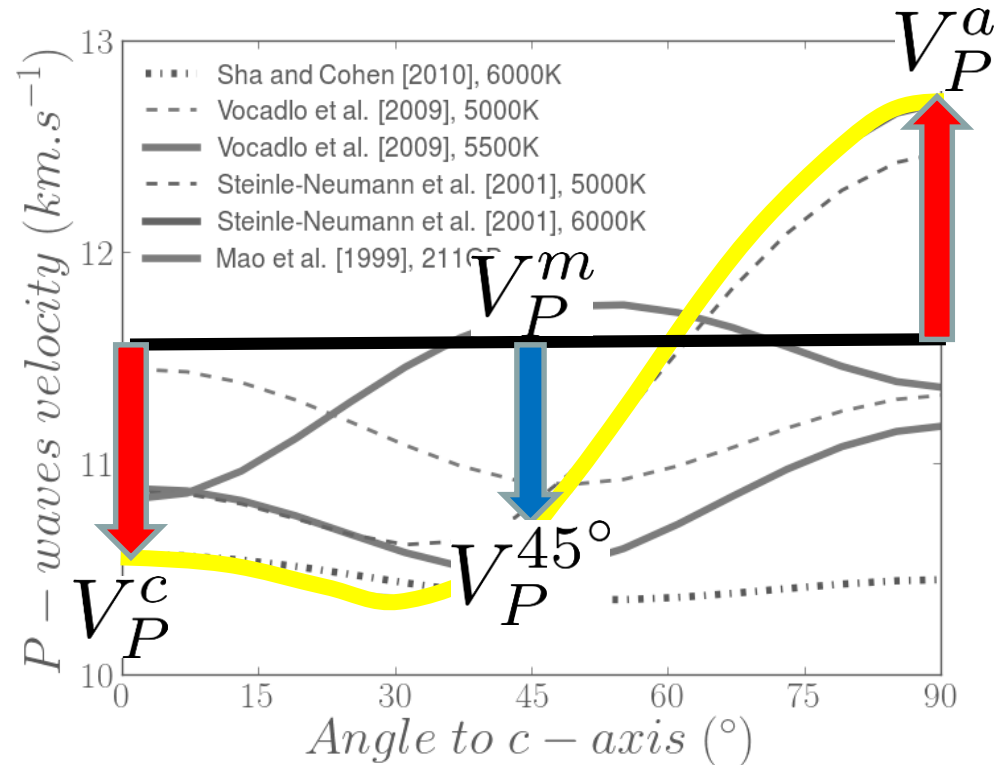
Global anisotropy is below 0.1%



# Dimensionless numbers of anisotropy

## Contrast $V_p$ $c$ - $a$

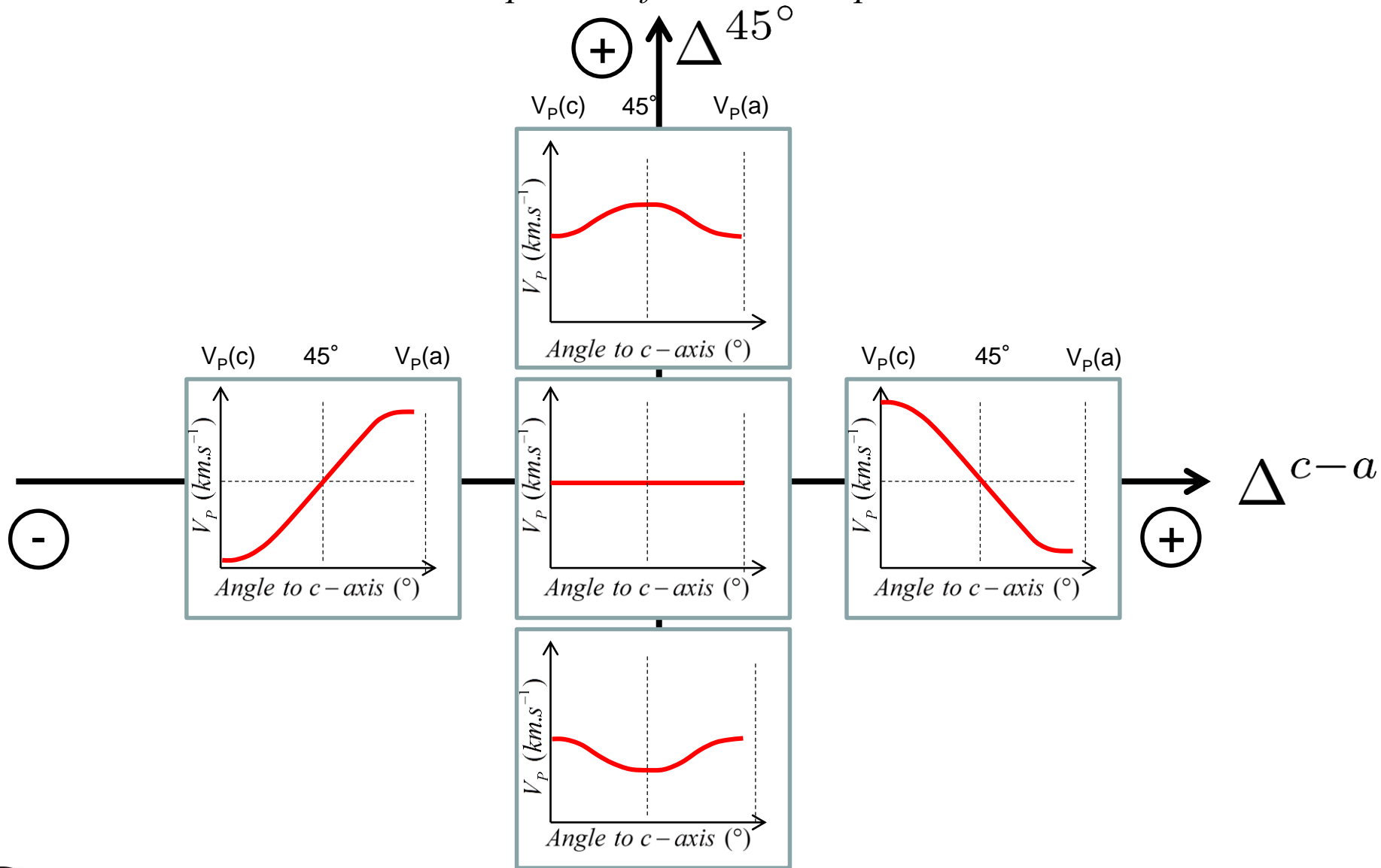
$$\Delta^{c-a} = \frac{V_P^c - V_P^a}{V_P^m}$$



$$\Delta^{45^\circ} = \frac{V_P^{45^\circ} - (V_P^c + V_P^a) / 2}{V_P^m}$$

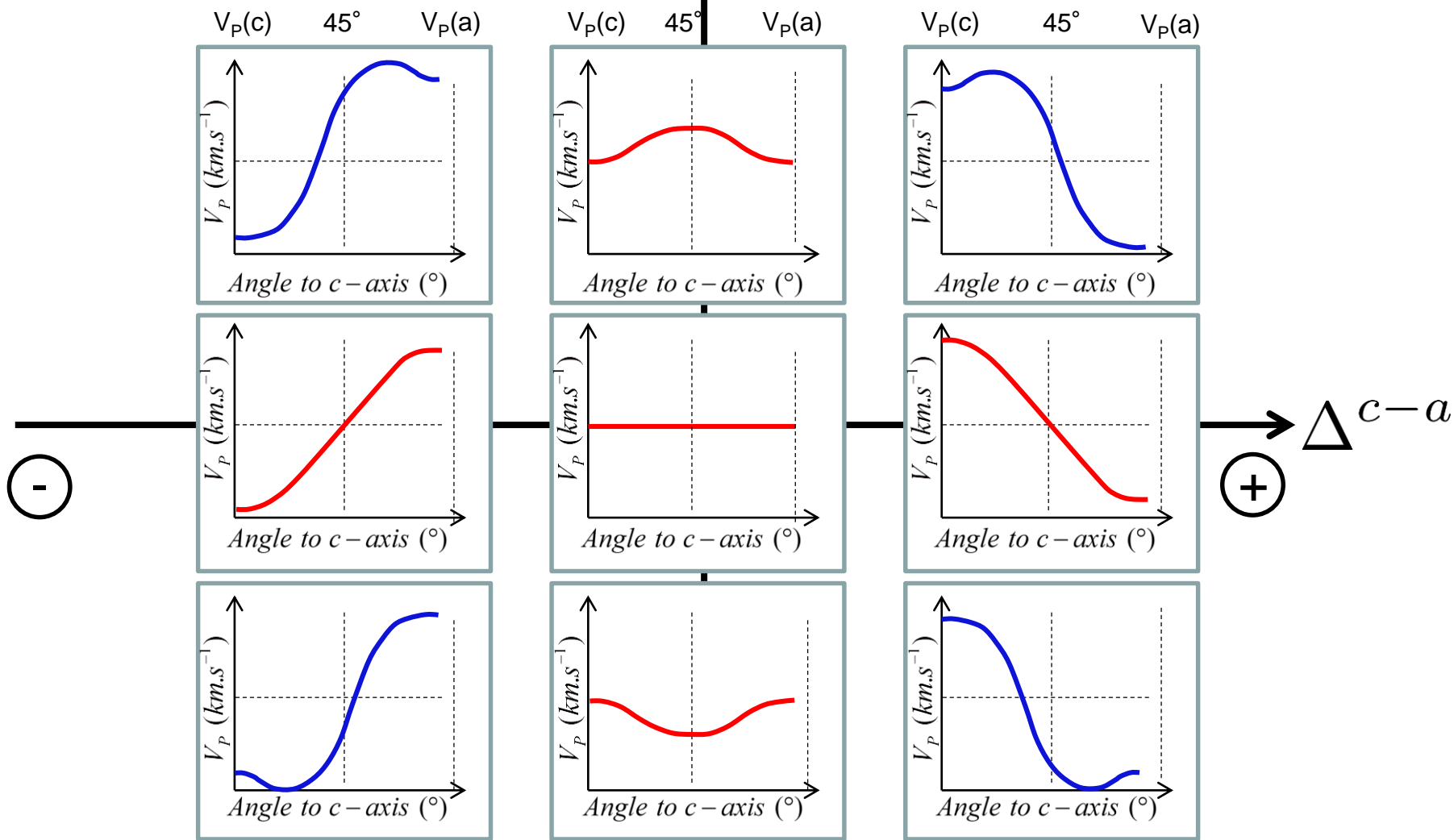
## Amplitude of bell-like shape

*Amplitude of bell-like shape*



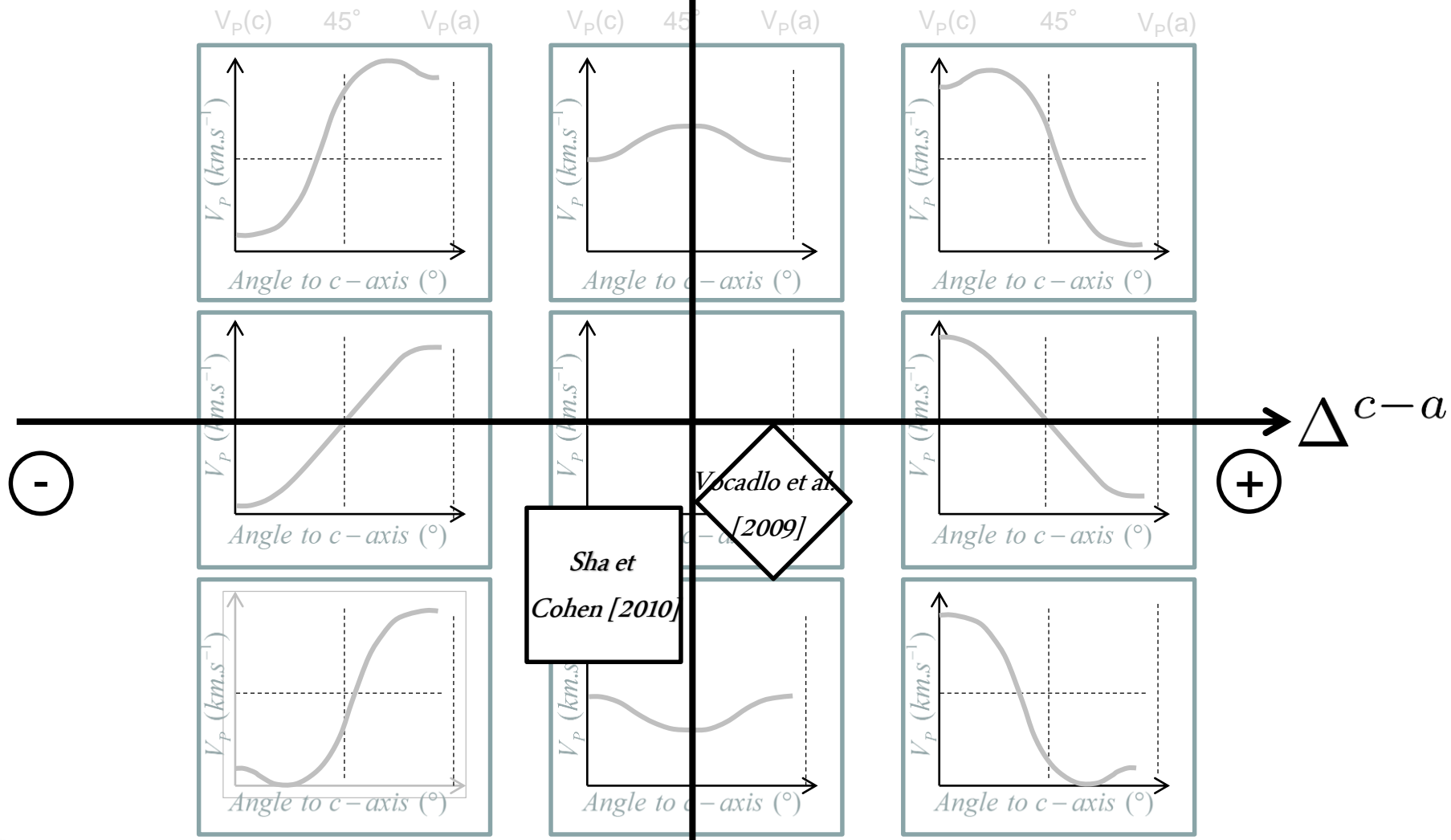
# Amplitude of bell-like shape

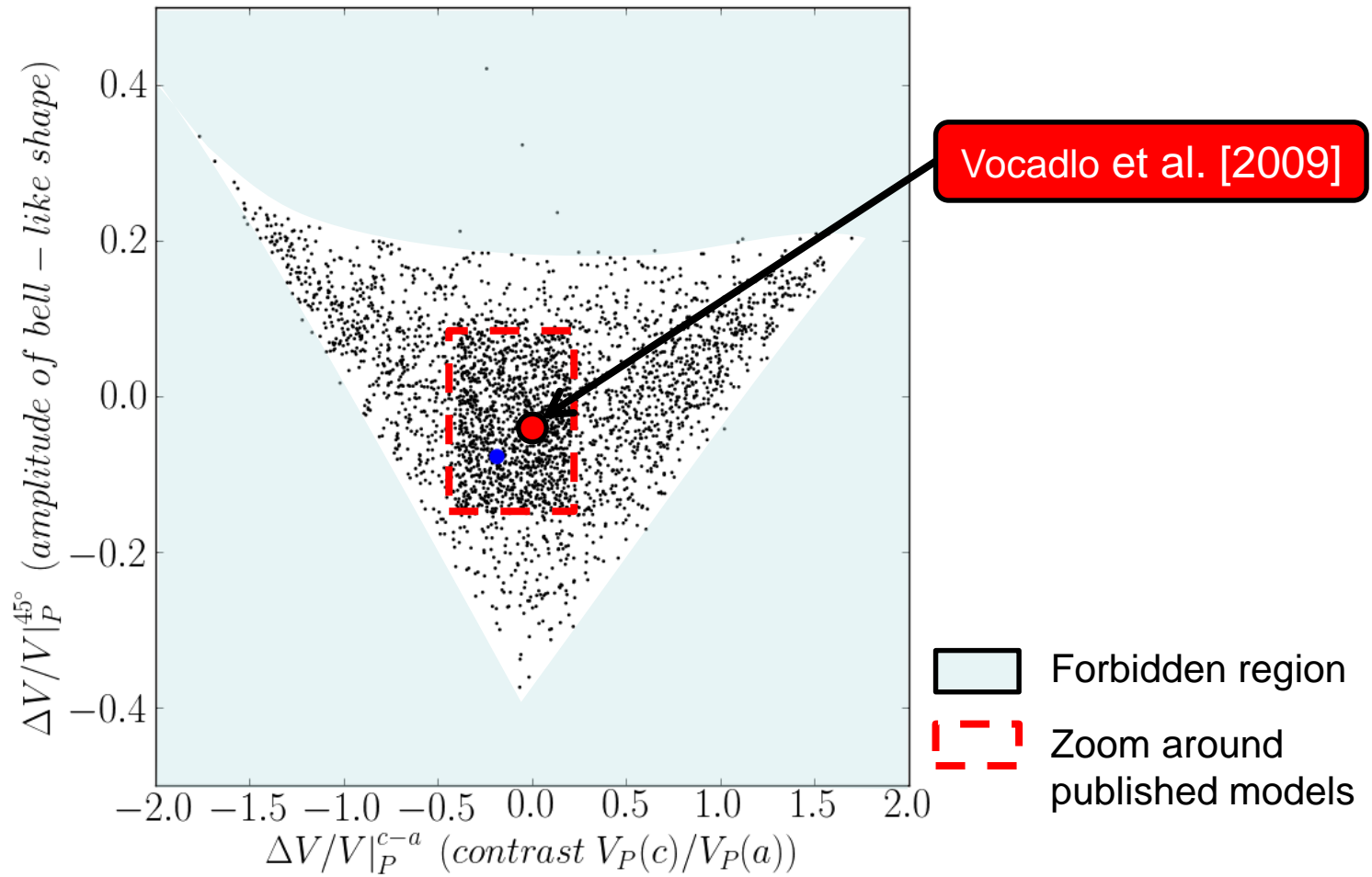
$\oplus$   $\uparrow$   $\Delta 45^\circ$



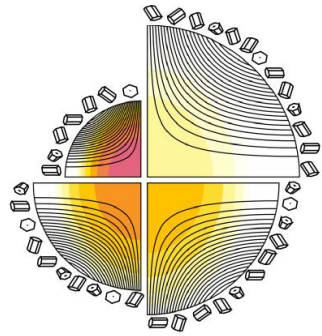
Amplitude of bell-like shape

$\oplus$   $\Delta^{45^\circ}$





# Monte Carlo Results

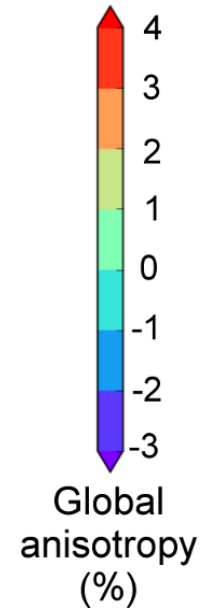
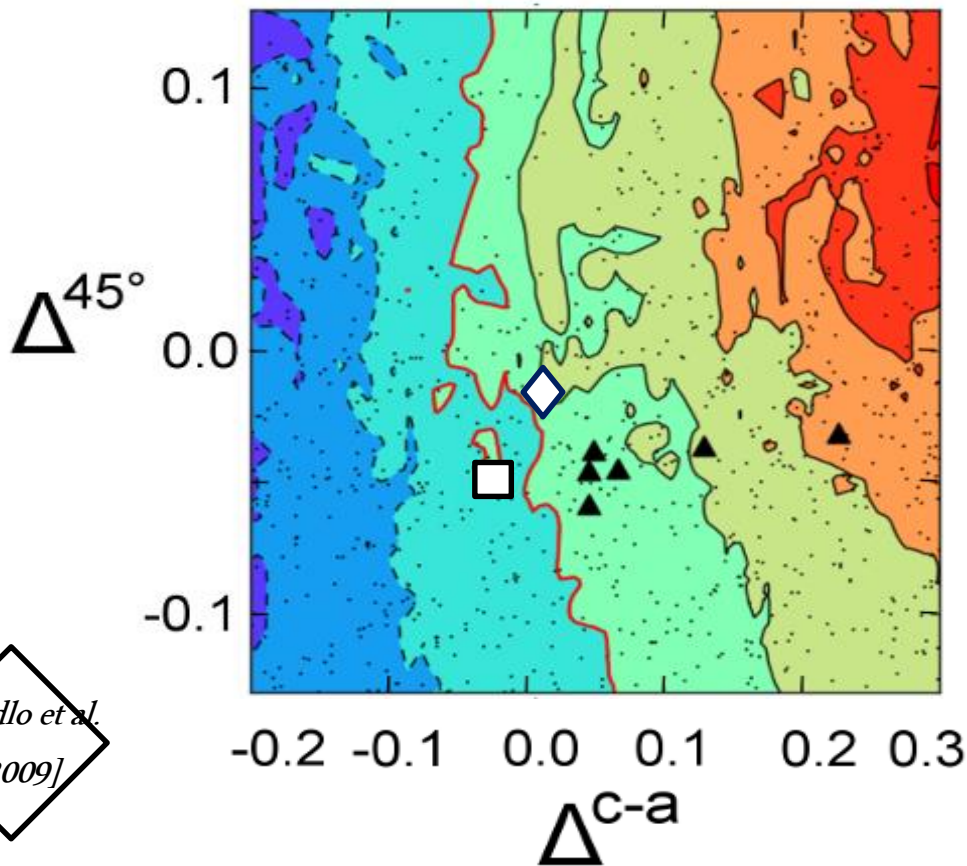


Pyramidal  
<c+a>  
slip

*Vocadlo et al.*  
[2009]

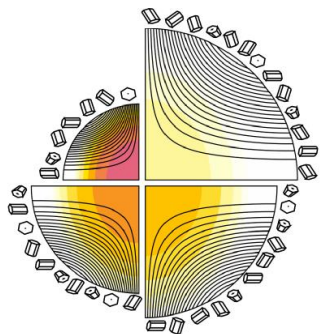
*Sha et*  
*Cohen [2010]*

## Equatorial growth



*Martorell et al [2013]*

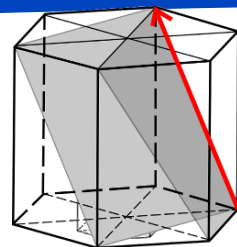
# Influence of the slip system



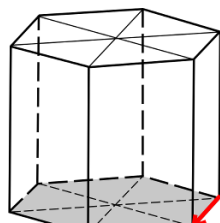
Pyramidal slip system is prone to align c axis along the NS axis.

It requires fast velocities along c-axes

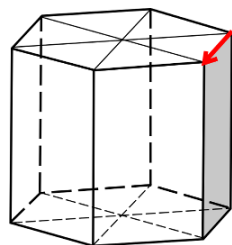
Global anisotropy is 5 to 10 times smaller than the single crystal anisotropy.



Pyramidal  
<c+a>  
slip



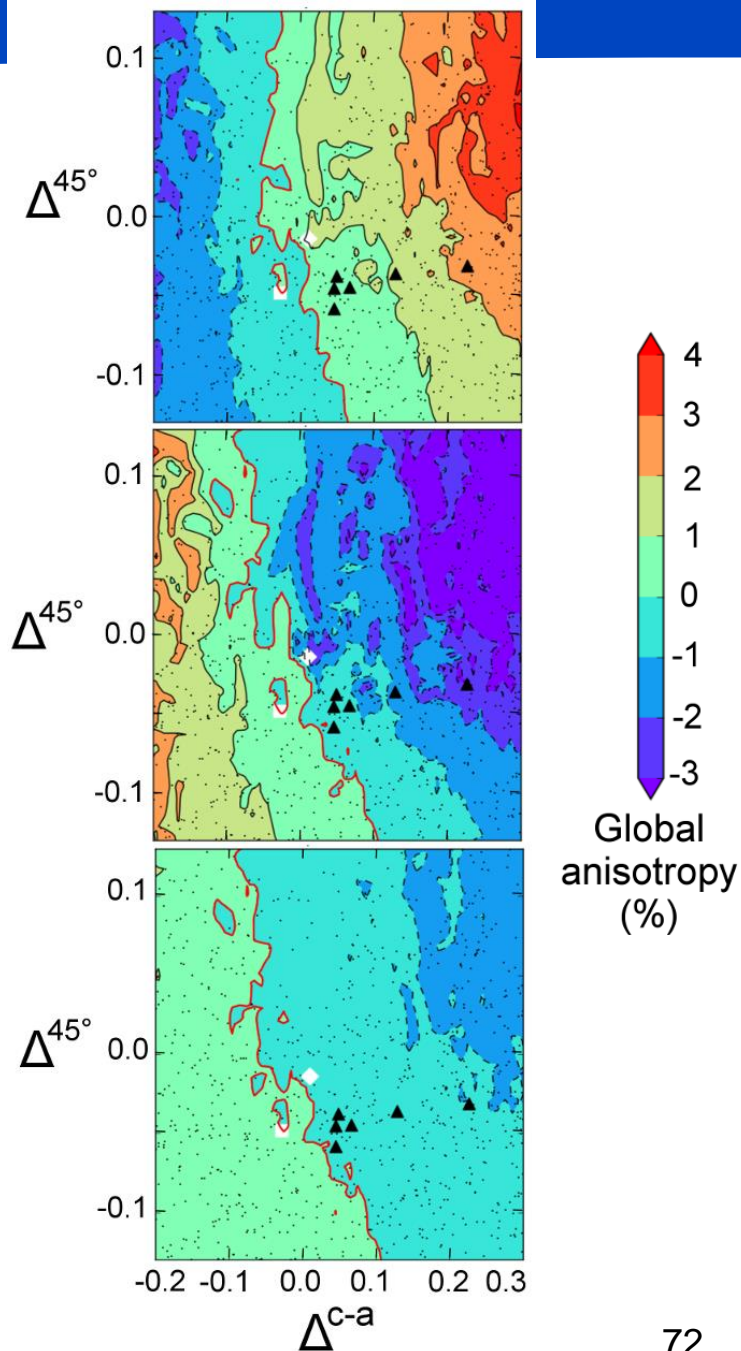
Basal  
slip



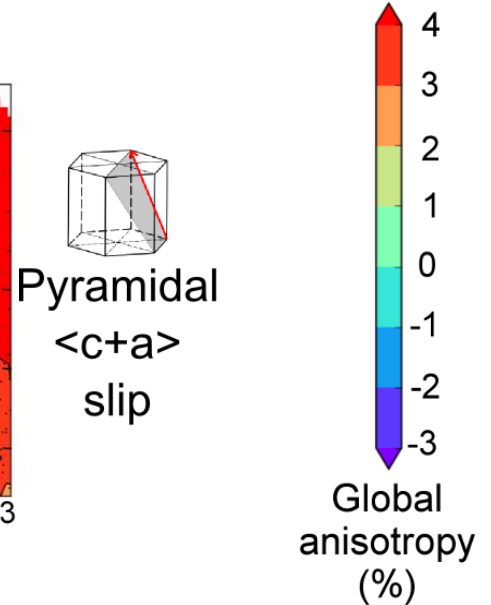
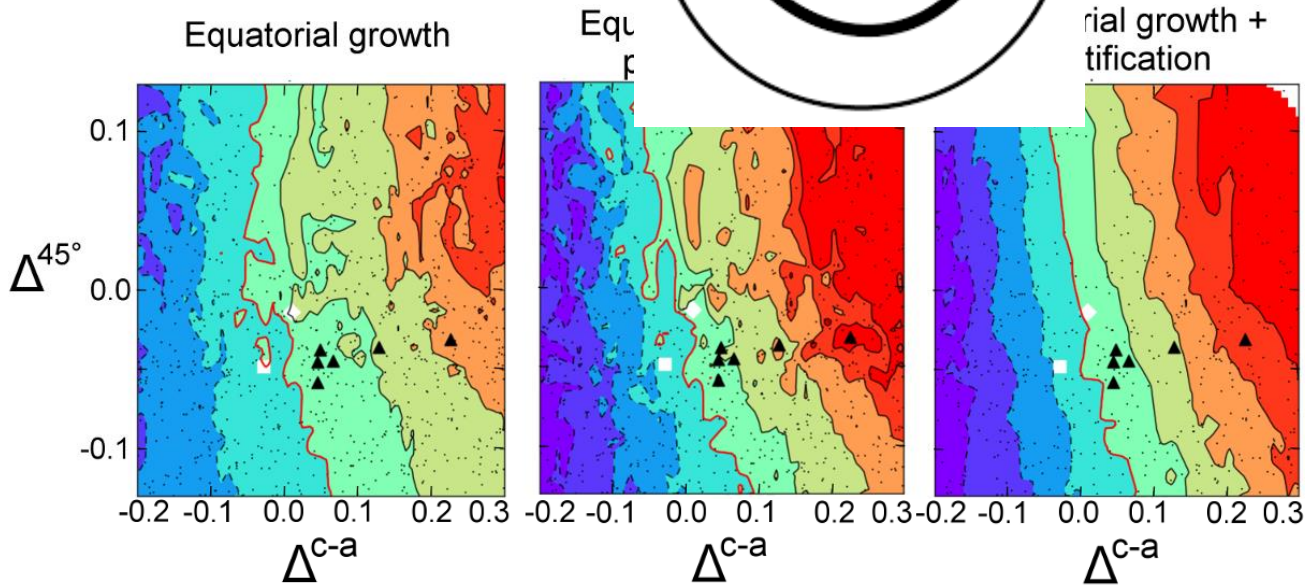
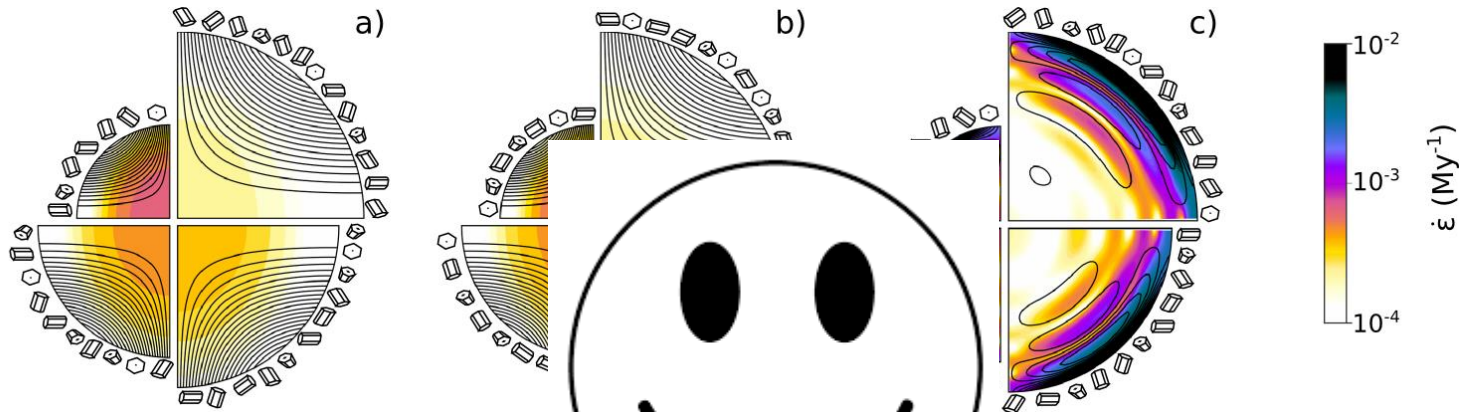
Prismatic  
slip

La graine terrestre

Equatorial growth



# Enhancement of global anisotropy



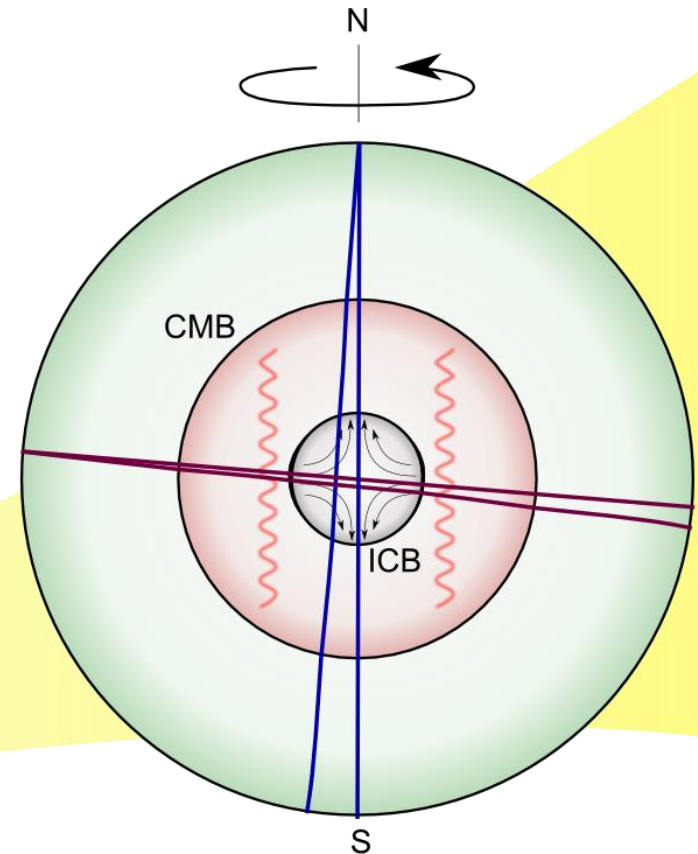
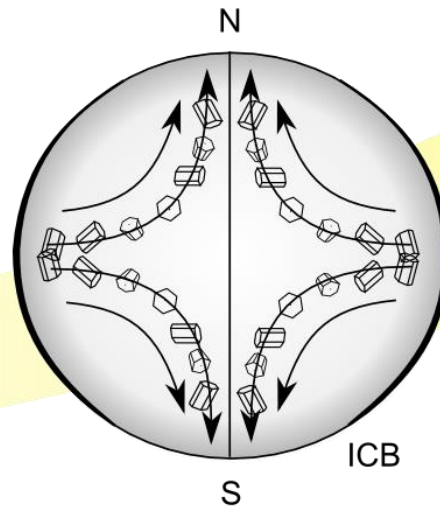
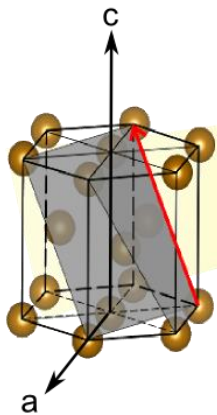


# Multi scale self consistent model

- N-S 3% global anisotropy

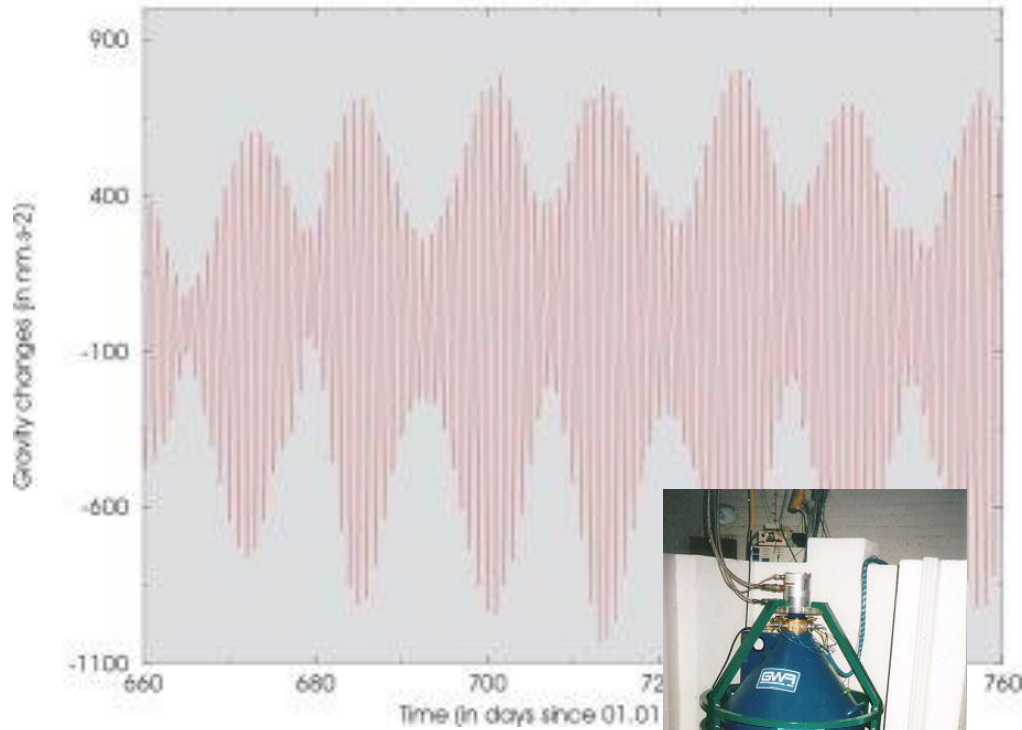
- Large scale
- N S axis

- Hcp Fe
- Pyramidal  $\langle c+a \rangle$
- $V_{pc} > V_{pa}$
- No cubic phase

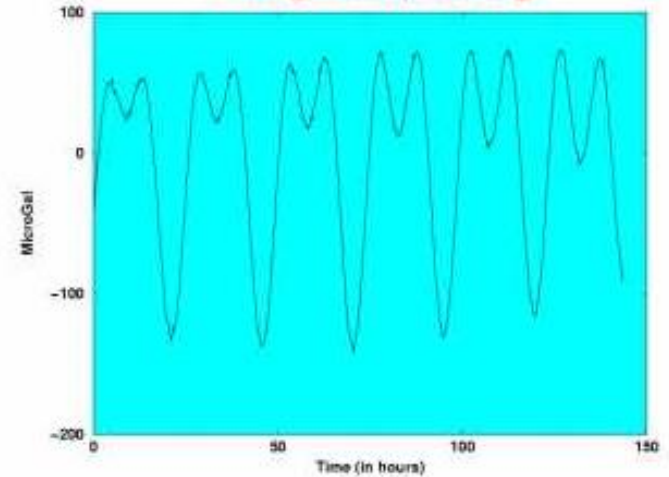


# Données gravimétriques

Gravity changes observed by SG 0026  
Strasbourg station (100 day duration)

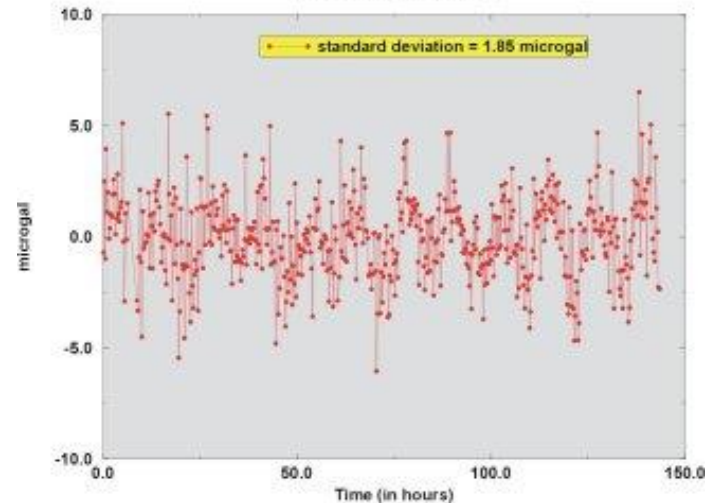


Gravity changes observed by FG5#206  
4-10 August 1998 (Strasbourg)

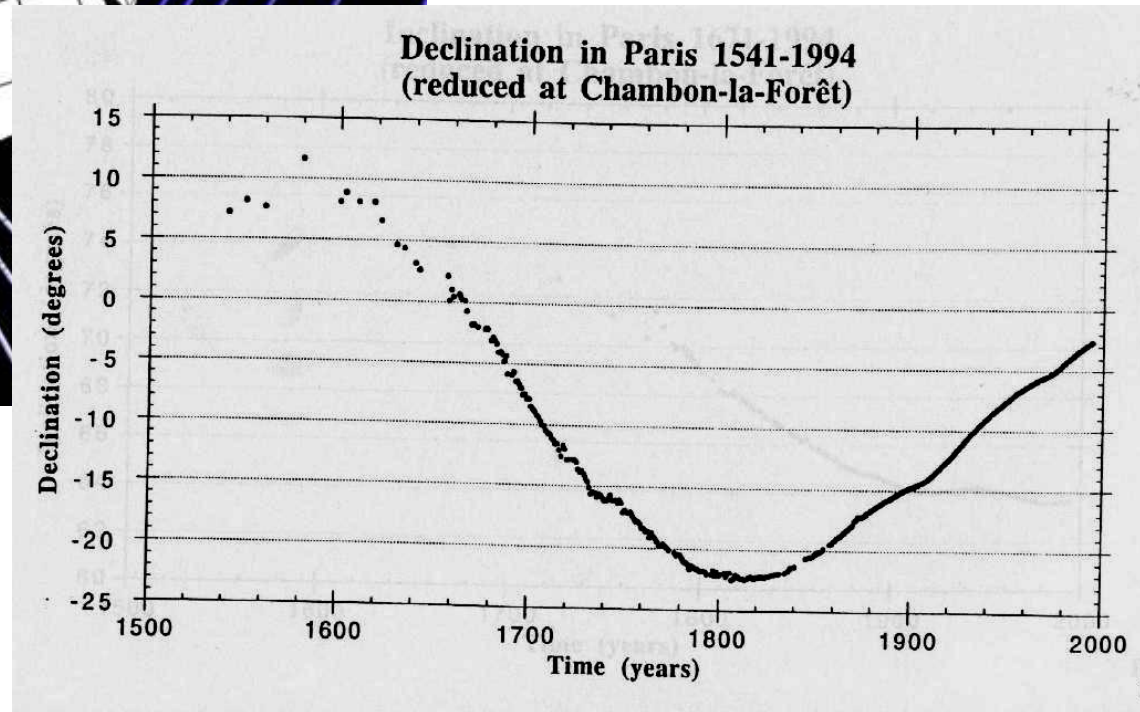
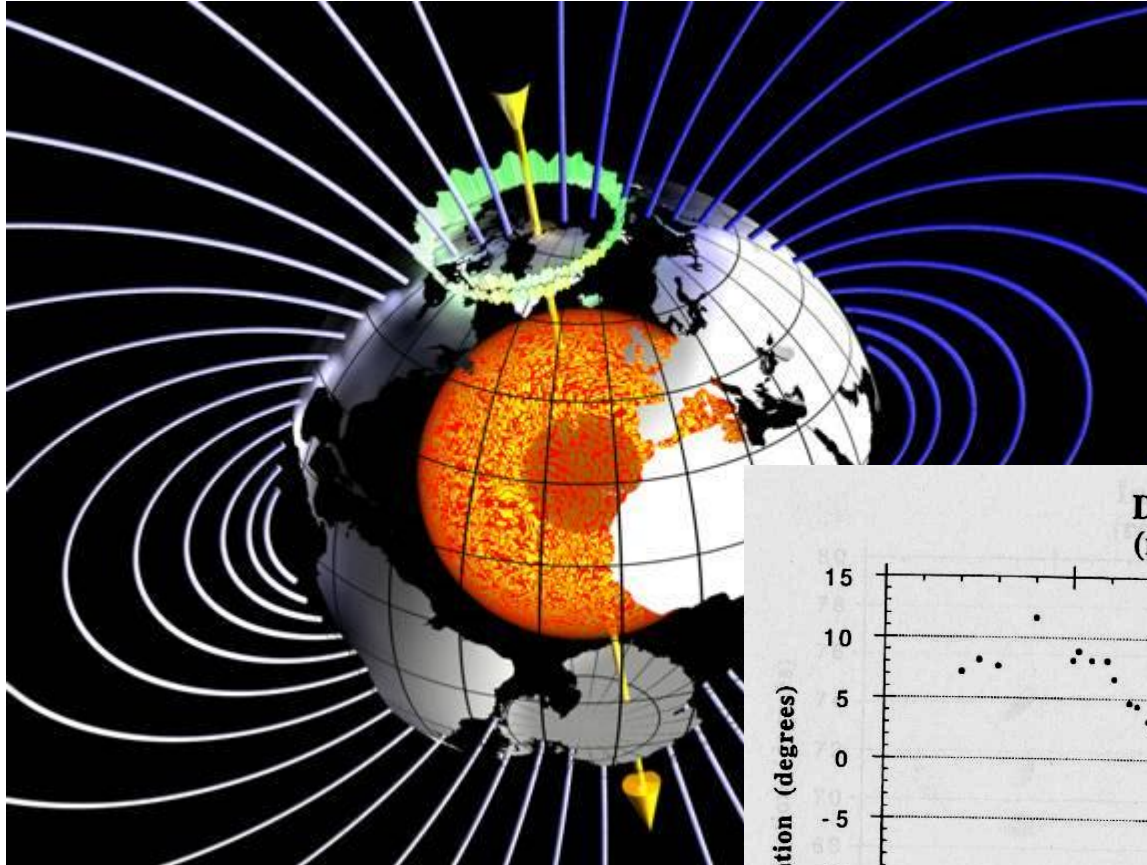


Marées terrestres et océaniques,  
pression atmosphérique, rotation de la  
Terre

Example of Single Set Mean values (AG FG5-206)  
4-10 August 1998



# Données magnétiques



# Paléointensités magnétiques et nucléation de la graine

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Published: 07 October 2015

## Palaeomagnetic field intensity variations suggest Mesoproterozoic inner-core nucleation

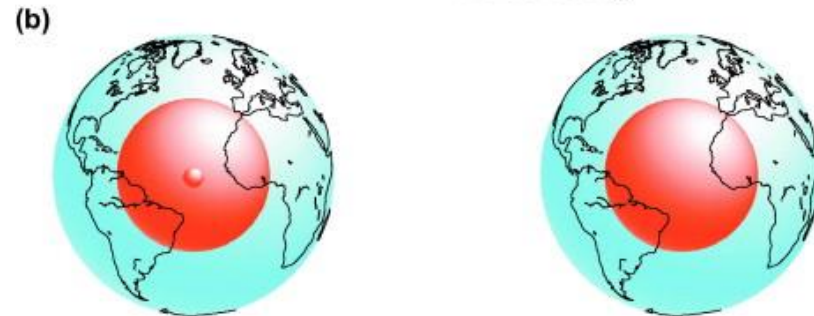
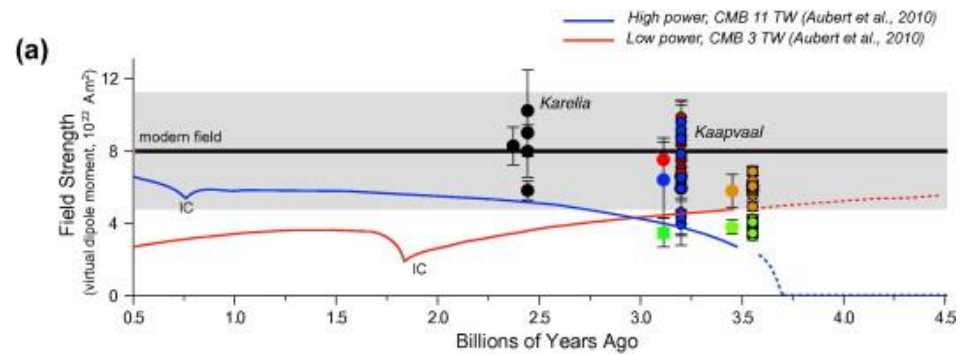
[A. J. Biggin](#) , [E. J. Piispa](#), [L. J. Pesonen](#), [R. Holme](#), [G. A. Paterson](#), [T. Veikkolainen](#) & [L. Tauxe](#)

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### Abstract

The Earth's inner core grows by the freezing of liquid iron at its surface. The point in history at which this process initiated marks a step-change in the thermal evolution of the planet. Recent computational and experimental studies<sup>1,2,3,4,5</sup> have presented radically differing estimates of the thermal conductivity of the Earth's core, resulting in estimates of the timing of inner-core nucleation ranging from less than half a billion to nearly two billion years ago.



Aubert, Labrosse, Poitou, 09

# Anisotropie?

- La graine est-elle anisotrope?
- Quelle phase minéralogique?
- Dynamique de la Graine?
- Son histoire?
- Son âge?